

A MICRODISCHARGE BASED PRESSURE SENSOR*

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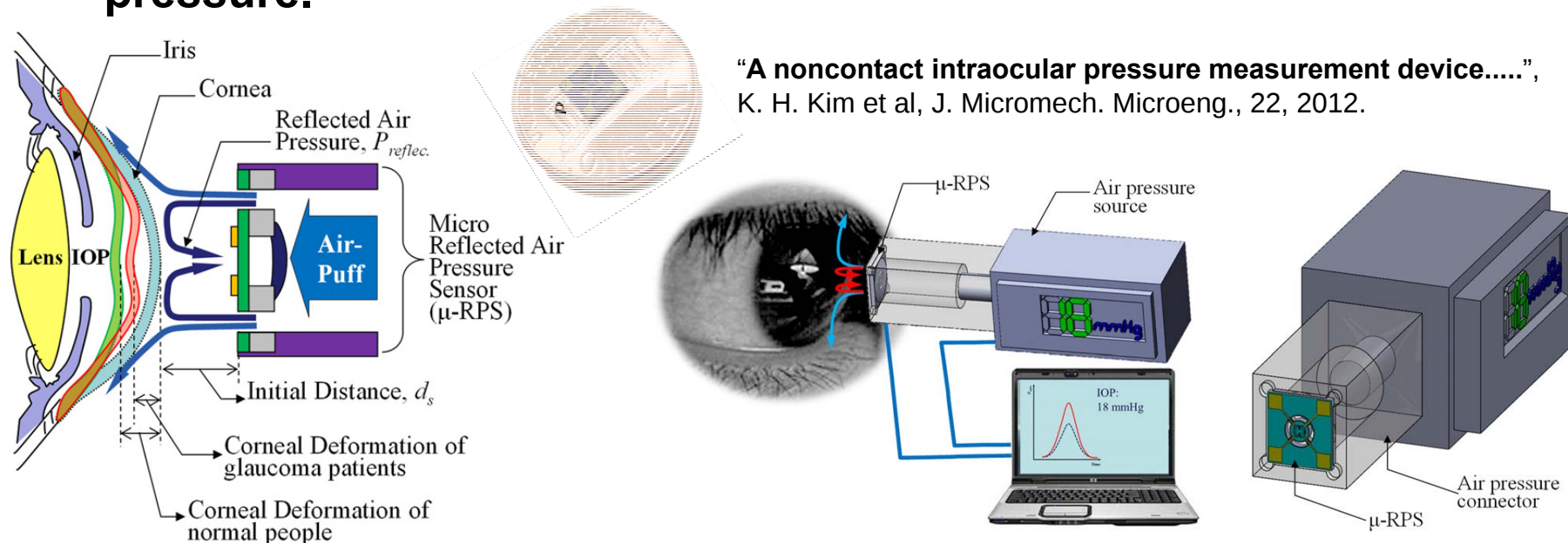
*** Work supported by Advanced Energy Consortium**

AGENDA

- **Introduction to pressure sensors**
 - **Conventional pressure sensors and challenges in harsh environments**
 - **Discharge-based pressure sensors**
- **Description of model**
- **Microplasmas in pressure sensors**
 - **Microplasma sustained in Ar**
 - **Current vs. membrane deflection (external pressure)**
 - **Differential current vs. membrane deflection**
- **Concluding Remarks**

MICROMACHINED PRESSURE SENSORS

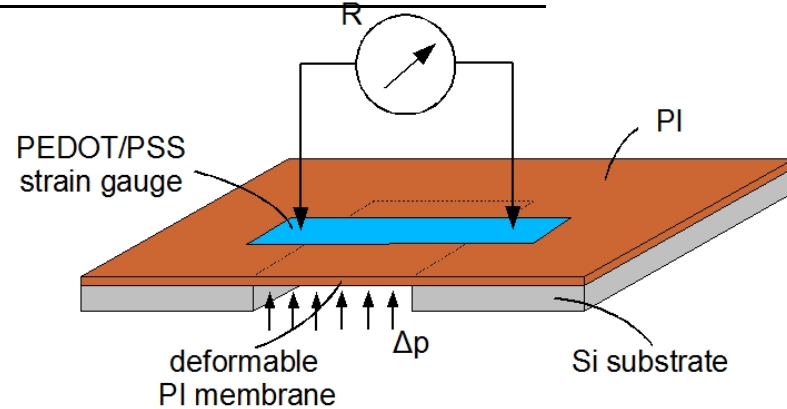
- “Micromachined pressure sensors” are used for automotive, biomedical and industrial applications.
 - Automotive: fuel lines, exhaust gases, tires...
 - Biomedical: ocular, cranial or bowel pressure.
 - Industrial: etching, deposition are sensitive to operating pressure.



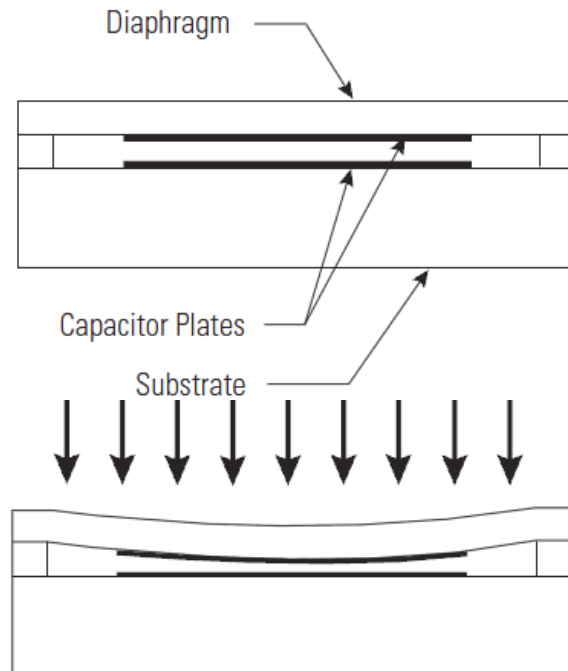
Ref:

- “Micromachined Pressure Sensors: Device, Interface Circuits, and Performance Limits”, by Y. B. Gainchandani et al.

Piezoresistive method



Capacitive method



Ref:

- www.zfm.ethz.ch/alumni/lang/page21.htm
- www.sensata.com/download/ipt_tech-note_1.pdf

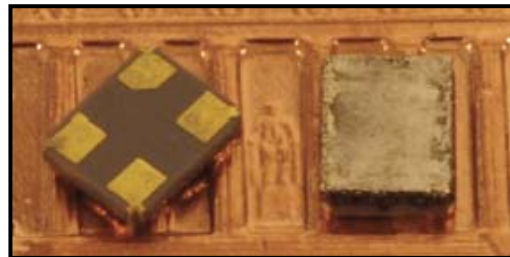
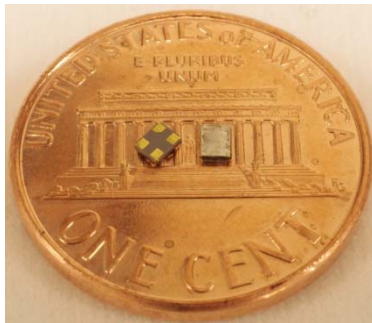
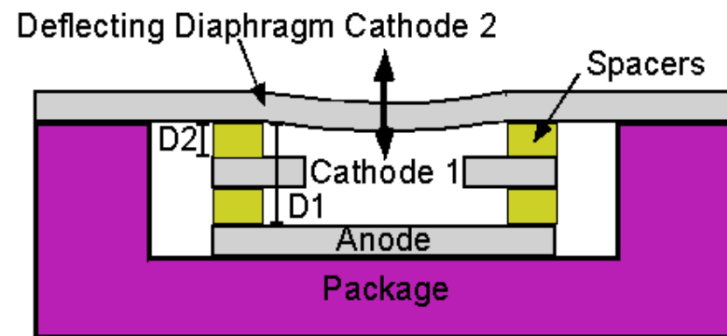
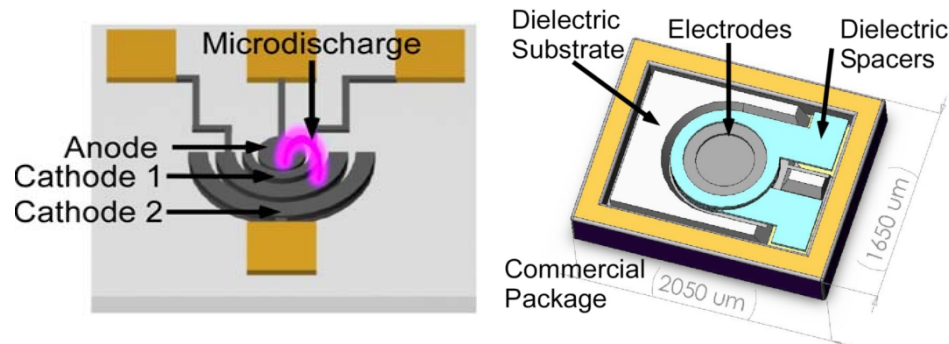
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MICROMACHINED PRESSURE SENSOR

- Microscale pressure sensors (100's μm) are based on deflection of a membrane.
- Piezoresistive materials (membrane) change resistance as deformed by pressure.
- Capacitance between electrodes changes as the membrane is deflected by pressure.
- Harsh environments (eg., oil borehole) are challenging:
 - High temperature ($> 100\text{ }^{\circ}\text{C}$).
 - high pressure (50-100 Mpa, 1 Mpa $\approx 9.87\text{ atm.}$).
 - Tight constraints for device volume.

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MICROPLASMA SENSOR



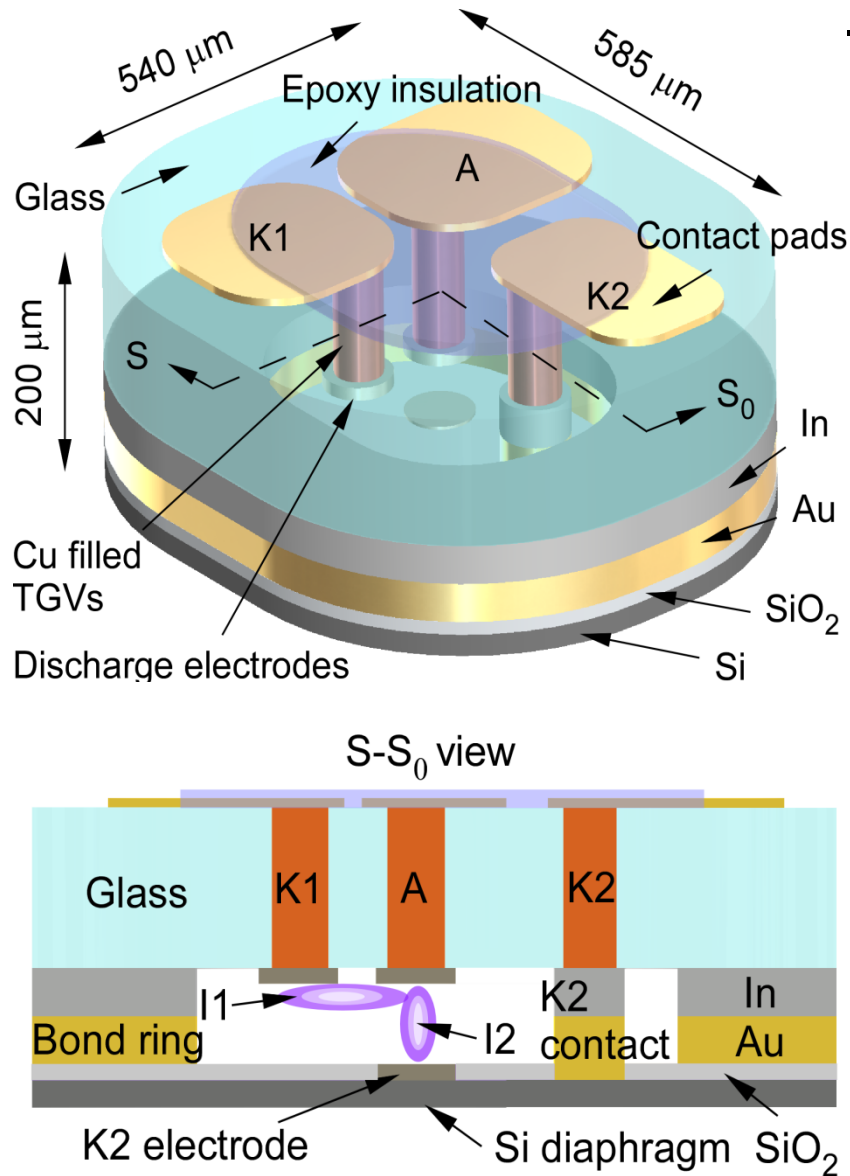
- Microplasma-based pressure sensors are structurally simple.
- External pressure deflects the diaphragm and changes the inter-electrode spacing, which redistributes the current to each of the cathodes.
- λ_{mfp} , E/N can be controlled to optimize the current distribution.
- Potential advantages in harsh environments:
 - Immune to high external temperature.
 - Large inherent signal (relatively simple interface circuits).
 - Small size (10's μm).

Ref: S. Wright and Y.B. Gianchandani, "Discharge-Based Pressure Sensors for High Temperature Applications Using Three-Dimensional and Planar Microstructures," *Journal of Microelectromechanical Systems*, 18(3), pp. 736-743, June 2009

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MICROPLASMA SENSOR



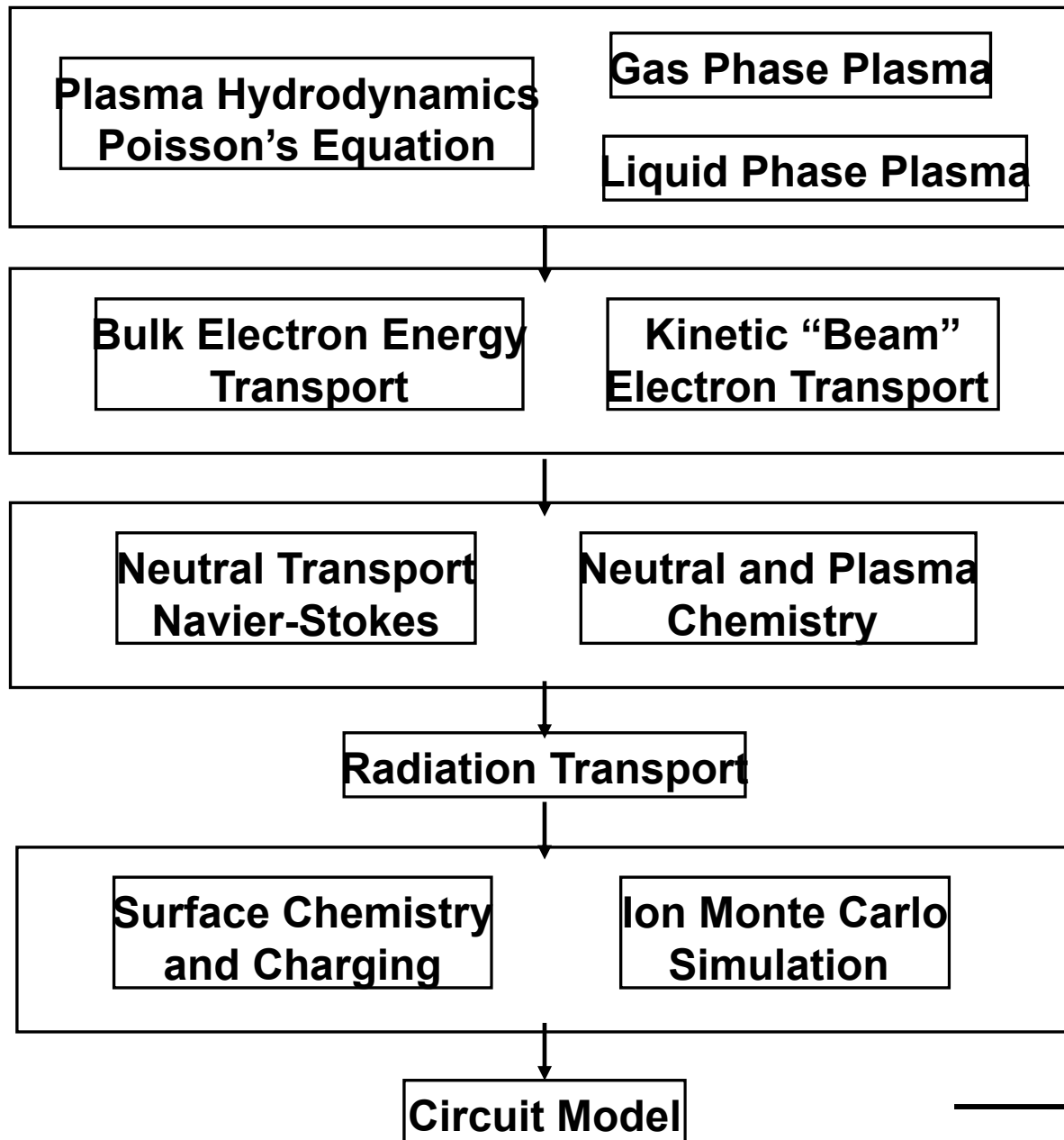
- **Two cathode microdischarge-based pressure sensor:**
 - Cathode 1 (K_1) adjacent to anode (A).
 - Cathode 2 (K_2) below anode (A).
 - Microplasma initiated between A and two competing cathodes (K_1 , K_2).
 - A diaphragm attached to one electrode is deflected by external pressure.
 - The changing inter-electrode spacing redistributes current to two competing cathodes.
- **Modeling will improve fundamental understanding and provide design rules.**

Ref:

• “A Microdischarge-Based Monolithic Pressure Sensor” by Y. B. Gainchandani et al.

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MODEL: *nonPDPSIM*

- 2-unstructured mesh with spatial dynamic range of 10^4 .
- Fully implicit plasma transport.
- Time slicing algorithms between plasma and fluid timescales.

MODELING PLATFORM: *nonPDPSIM*

- **Poisson's equation:** $\nabla \cdot (\epsilon \nabla \Phi) = -(\sum_j q_j N_j + \rho_s)$
- **Transport of charged and neutral species:** $\frac{\partial N_j}{\partial t} = -\nabla \cdot \vec{\Gamma}_j + S_j$
- **Surface Charge:** $\frac{\partial \rho_s}{\partial t} = \left[\sum_j q_j (-\nabla \cdot \vec{\Gamma}_j + S_j) - \nabla \cdot (\sigma(-\nabla \Phi)) \right]_{material}$
- **Electron Temperature (transport coefficient obtained from Boltzmann's equation)**

$$\frac{\partial(n_e \epsilon)}{\partial t} = \vec{j} \cdot \vec{E} - n_e \sum_i \Delta \epsilon_i K_i N_i - \nabla \cdot \left(\frac{5}{2} \bar{\phi}_e \epsilon - \bar{\kappa}(T_e) \cdot \nabla T_e \right)$$

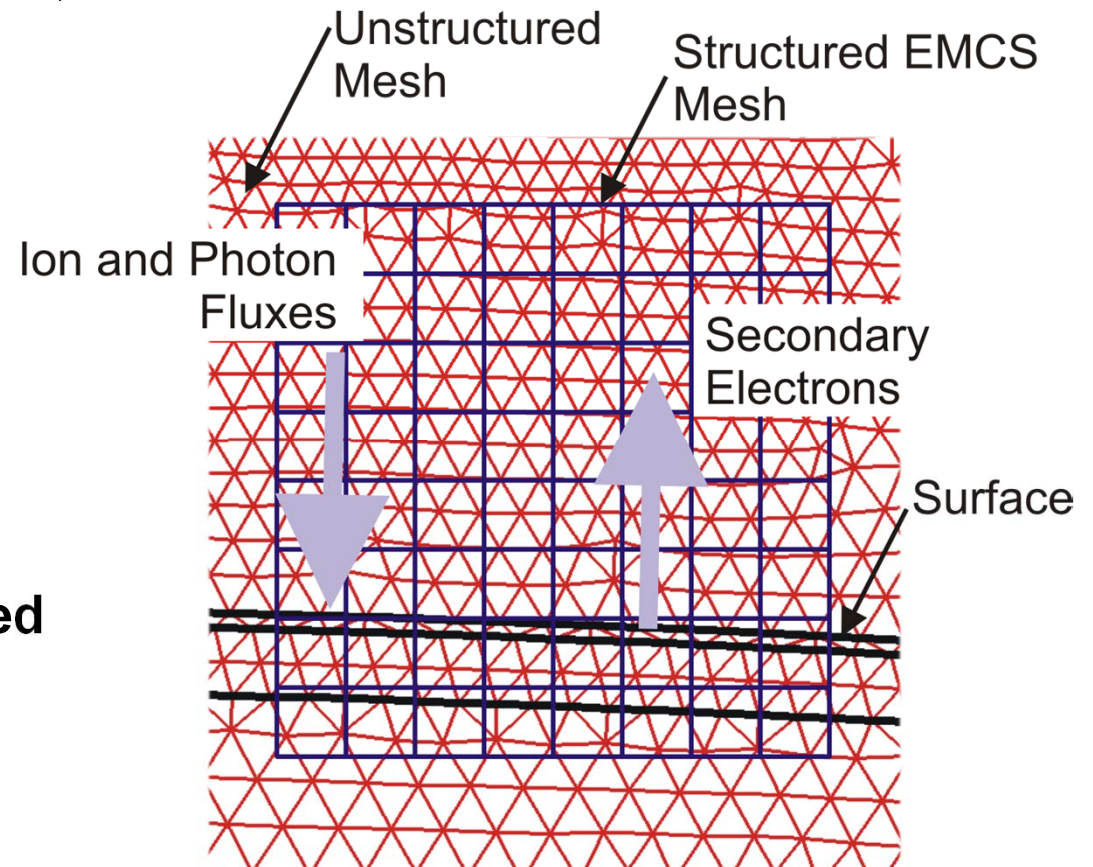
- **Radiation transport and photoionization:**

$$S_m(\vec{r}_i) = N_m(\vec{r}_i) \cdot \sum_k \sigma_{mk} A_k \int N_k(\vec{r}_j') G_k(\vec{r}_j', \vec{r}_i) d^3 \vec{r}_j'$$

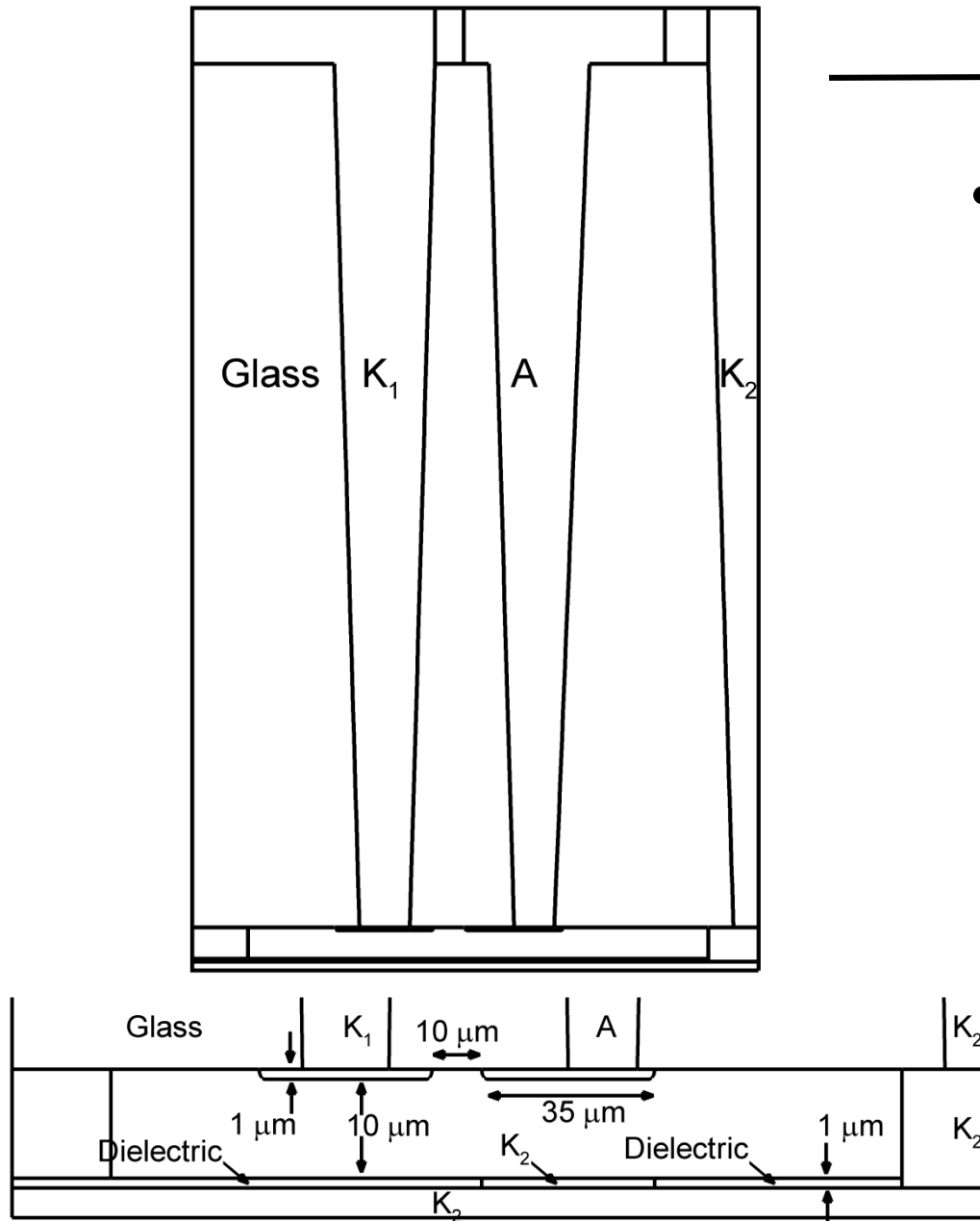
$$G(\vec{r}_j', \vec{r}_i) = \frac{\exp \left(- \sum_l \int_{\vec{r}_j'}^{\vec{r}_i} \sigma_{lk} N_l(\vec{r}_j') d\vec{r}_j' \right)}{4\pi |\vec{r}_j' - \vec{r}_i|^2}$$

SECONDARY ELECTRONS FROM SURFACES

- Using a beam-bulk formulation, an electron Monte Carlo Simulation is used to follow trajectories of secondary electrons from surfaces.
- Structured EMCS mesh overlaid onto unstructured fluid mesh – E-fields interpolated onto mesh.
- Pseudo-particles are launched from sites on surfaces for emission produced by
 - Ion bombardment
 - Photon fluxes
 - Electric field enhanced thermionic emission.



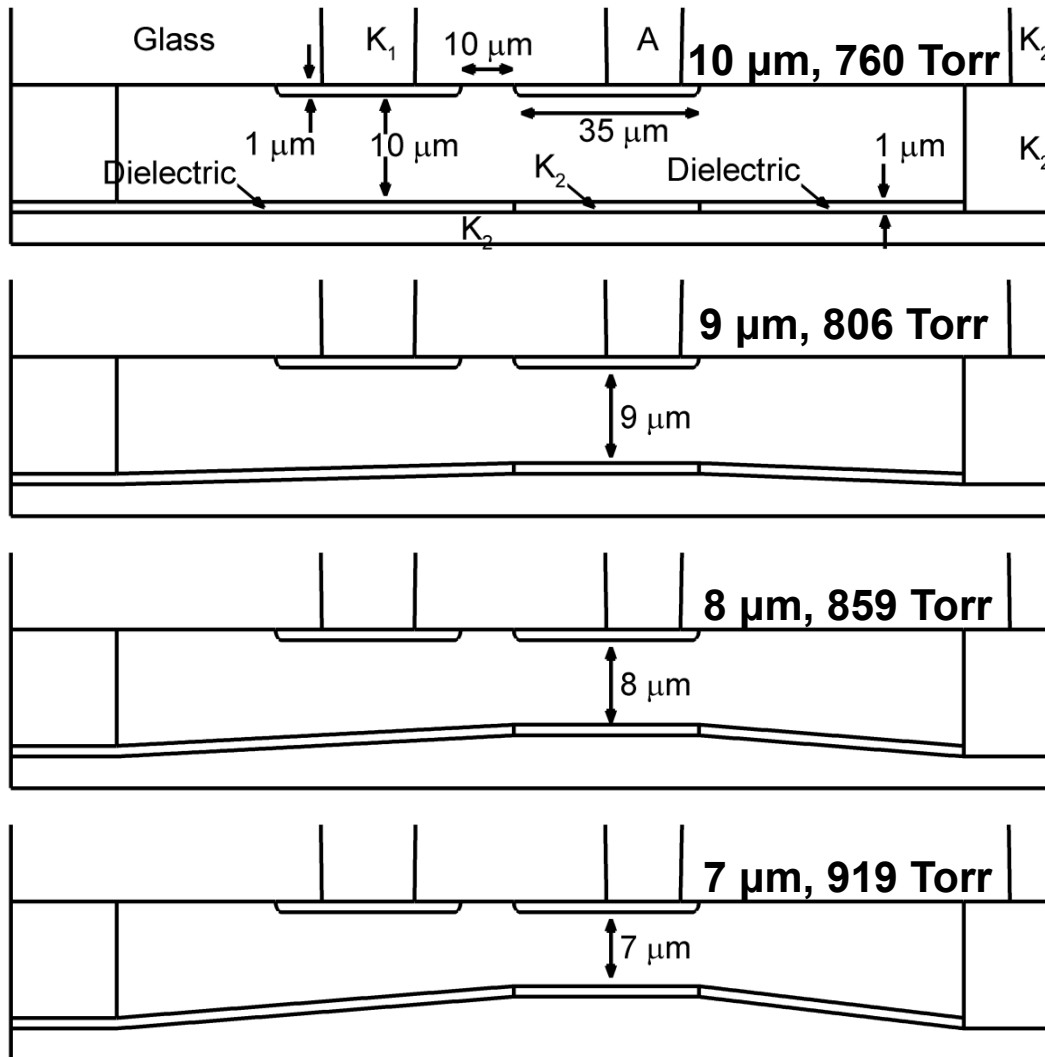
MODEL GEOMETRY



• $X/Y=0.5$

- Three electrodes (two cathode) structure:
 - Inter-electrode spacing: A-K₂, A-K₁ = 10 μm.
 - K₁, K₂: grounded, A: 400 V.
 - Ballast resistor: 100 Ω (K₁, K₂) and 500 Ω (A).
 - Discharge initiated with emission current of 10⁻² A-cm⁻² for 10 ns at cathode corner.
 - 1 atm Ar (Ar, Ar(4s,4p), Ar⁺, Ar₂⁺, Ar₂^{*} and electrons).

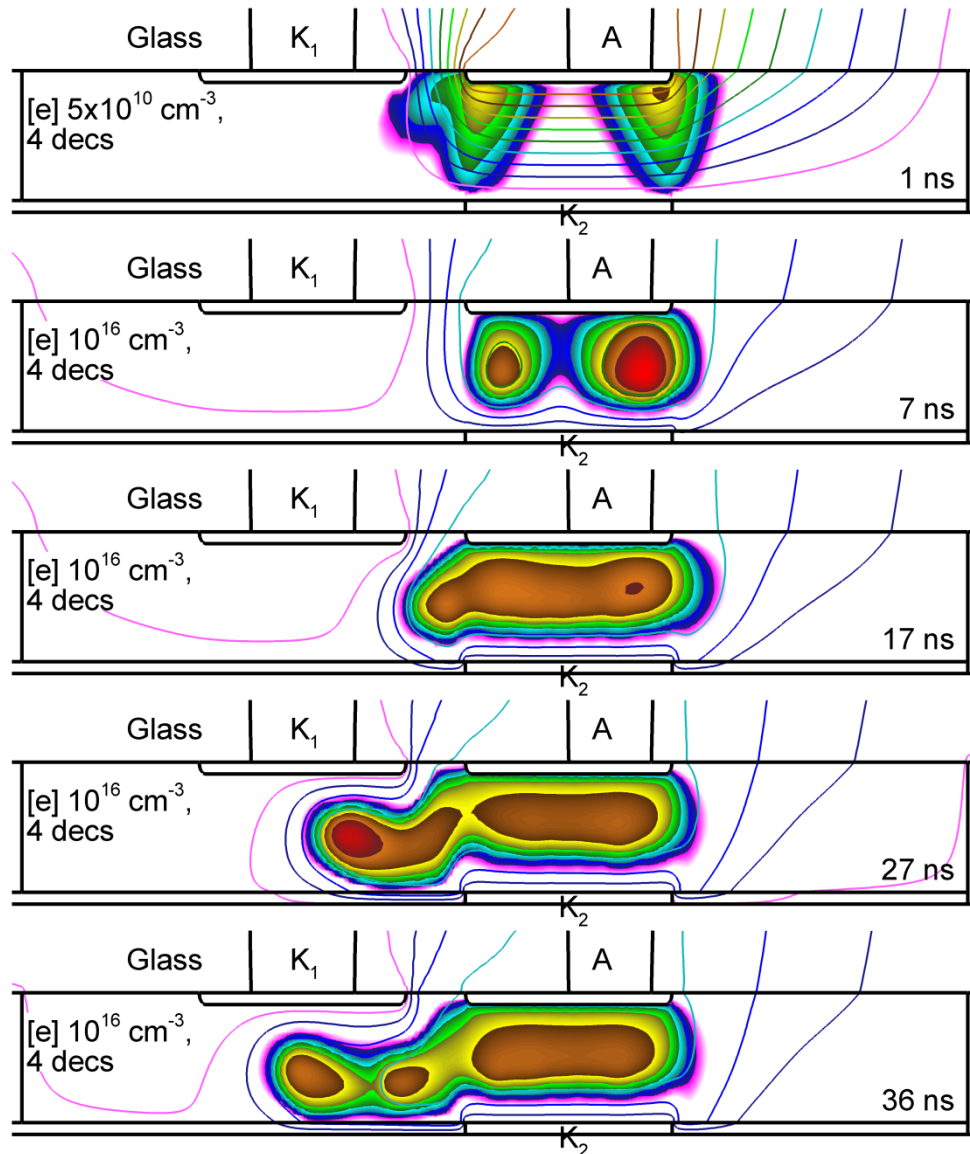
MODEL GEOMETRY



- Three electrodes (two cathodes) pressure sensor structure:
 - $A-K_1 = 10\text{ }\mu\text{m}$.
 - Gap spacing ($A-K_2$) reduced by external pressure.
 - $A-K_2$: $10 - 7\text{ }\mu\text{m}$. (0 – 25 MPa external pressure)
 - Chamber Pressure: 760 – 919 Torr Ar.

- $X/Y=0.5$

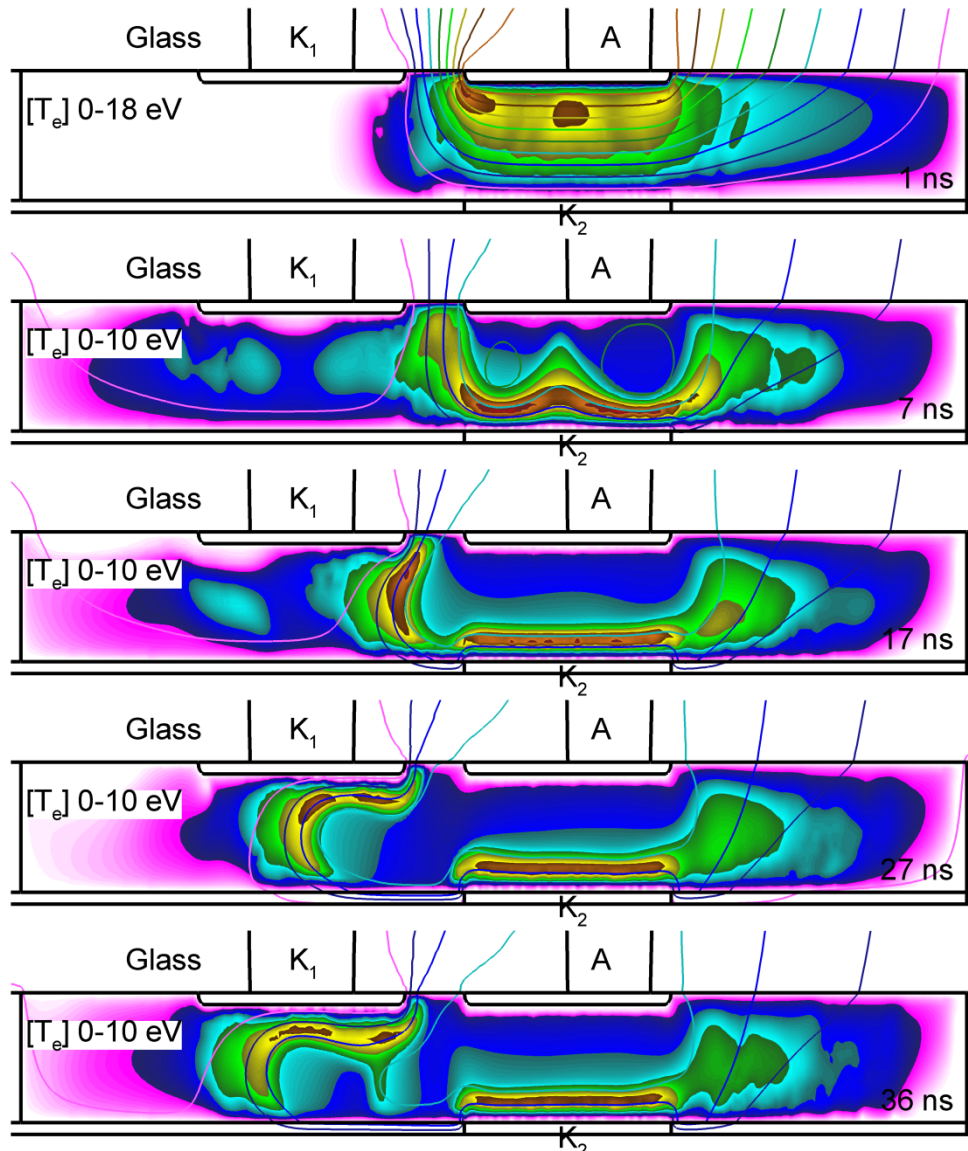
MICROPLASMA DYNAMICS: $[e]$



- Inter-electrode spacing: A-K₂, A-K₁=10 μm .
- A: 400 V, K: 0 V , $\Delta V = 40$ V (Contours).
- 760 Torr Ar.

- Avalanche between edges of cathodes and anode produces a conductive plasma within 10 ns.
- After avalanche, plasma shields out E-field and reduces E/N , T_e , S_e .
- Conductive plasma transfers anode potential to cathodes. T_e and intense ionization peak at K₂ and A-K₁.
- I_{K2} produced by plasma between A-K₂ sustained by K₂.
- Increasing $[e]$ at A-K₂ reduces E/N , T_e and S_e , which reduces $[e]$.
- E/N , T_e and S_e then rebound to produce high density $[e]$. A self-pulsing I_{K2} is then produced.

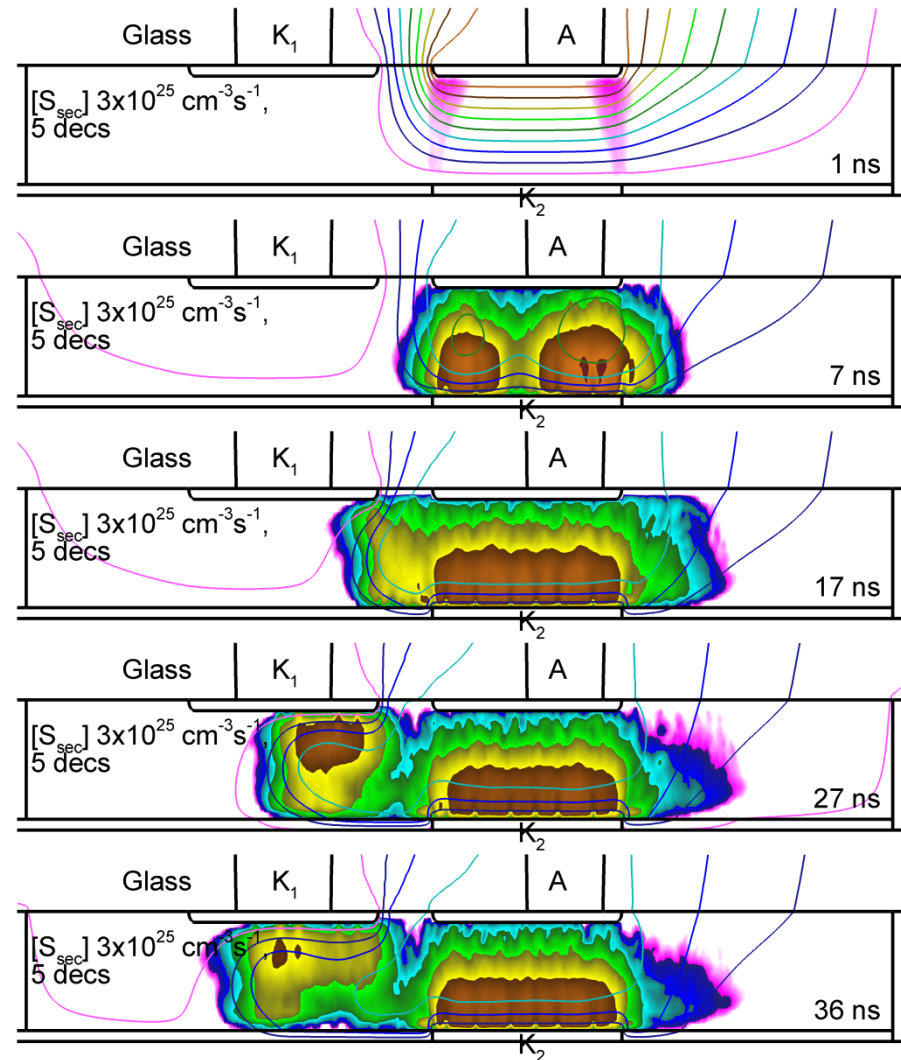
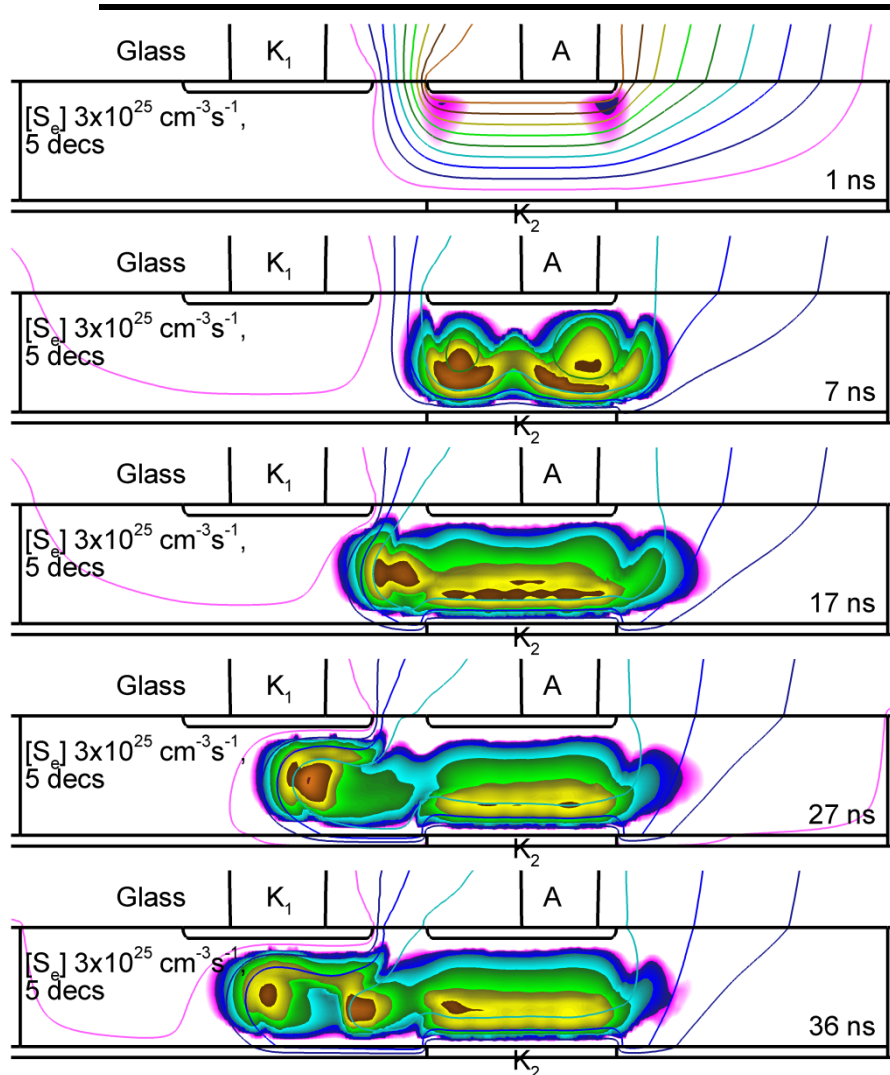
MICROPLASMA DYNAMICS: $[T_e]$



- Inter-electrode spacing: A- K_2 , A- K_1 =10 μm .
- A: 400 V, K: 0 V , ΔV = 40 V (Contours).
- 760 Torr Ar.

- Due to charge separation, high voltage drop at A- K_1 trigger a bullet-like ionization wave (IW).
- IW propagates along K_1 producing current pulses (I_{K1}).
- A striation from A to K_1 is due to the repetitive bullet-like IW.
- Ionization source S_{sec} at cathode sheaths is comparable with S_e from bulk plasma.

MICROPLASMA DYNAMICS: $[S_e]$, $[S_{sec}]$



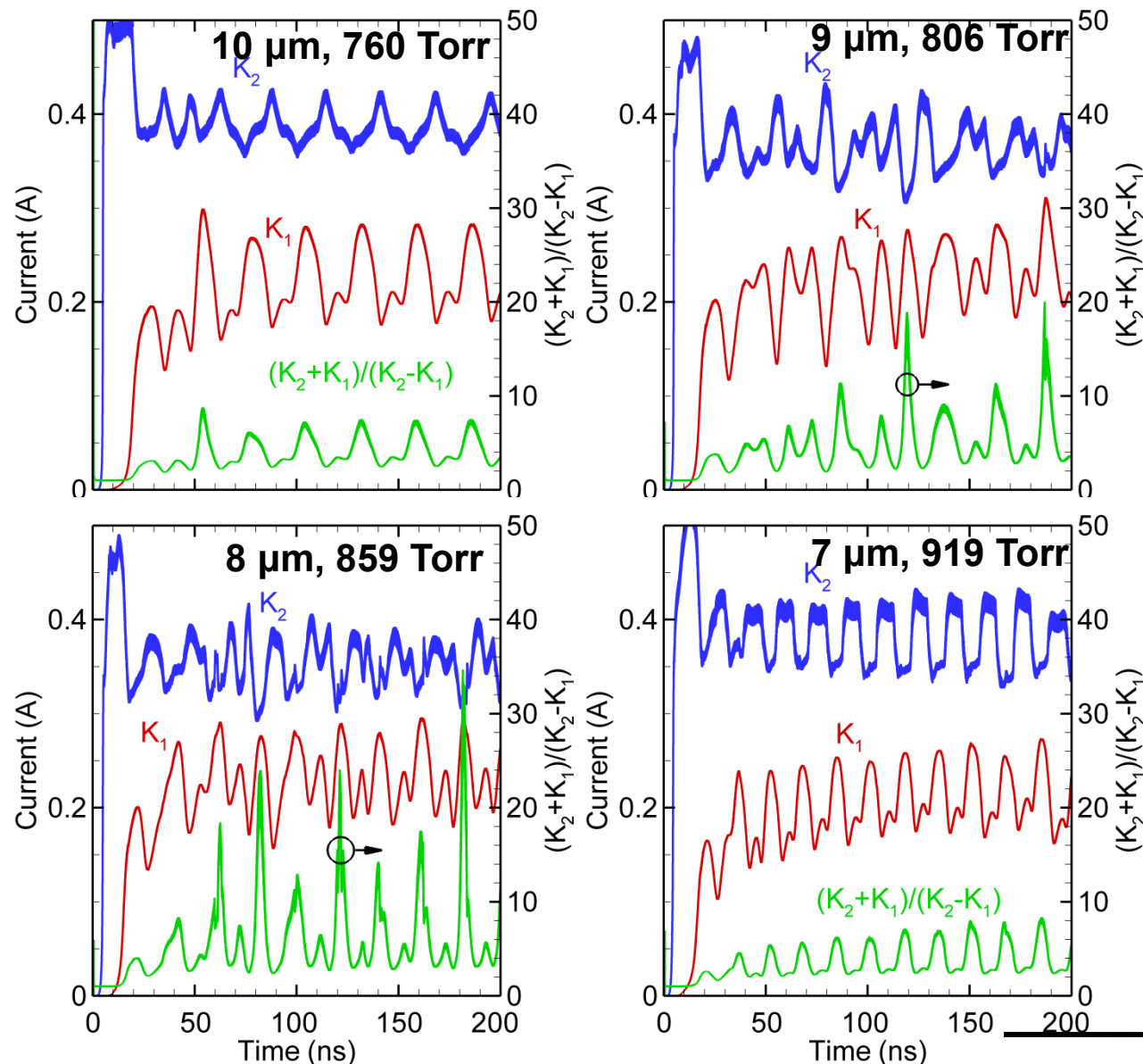
- Inter-electrode spacing: A- K_2 , A- K_1 = 10 μm .
- A: 400 V, K: 0 V, ΔV = 40 V (Contours).
- 760 Torr Ar.

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MIN  MAX

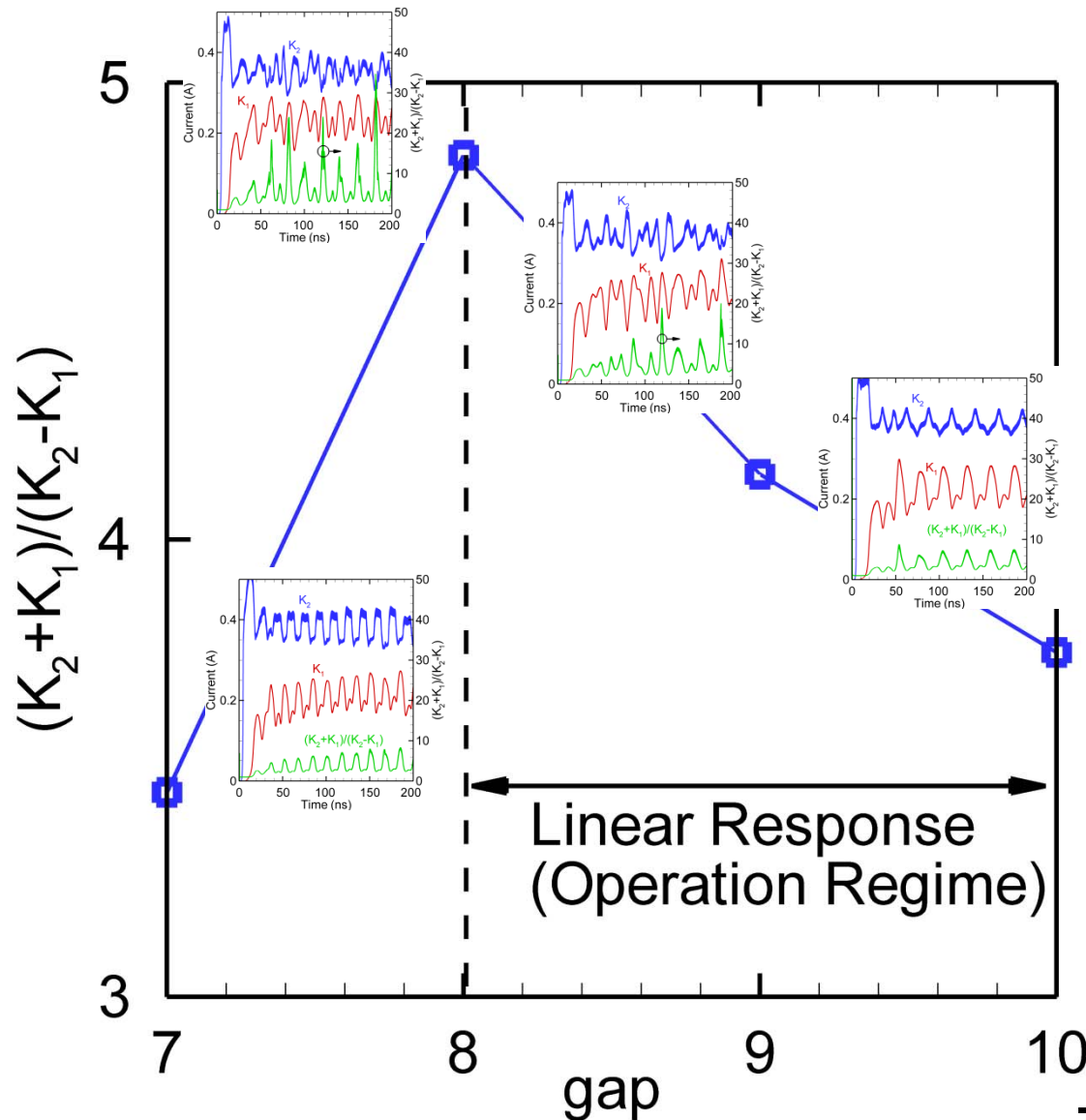
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MICROPLASMA CURRENT ON CATHODES



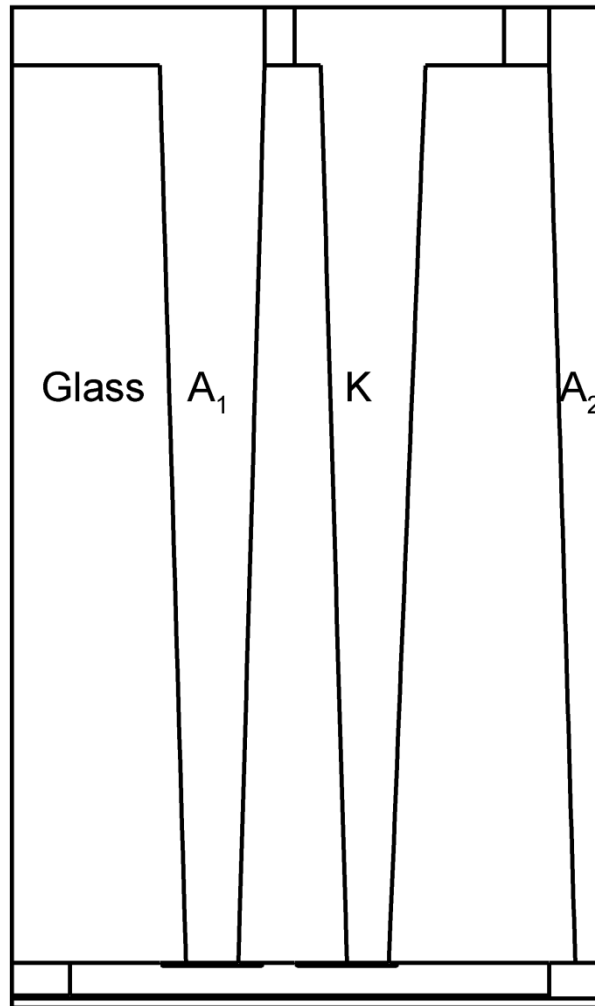
- Gap (A- K_2) spacing: 10-7 μm .
- A: 400 V, K: 0 V.
- 760-919 Torr Ar.
- Self-pulsing results in high frequency oscillation in I_{K_1} and I_{K_2} .
- Averaged $I_{K_2} + I_{K_1} \approx$ constant.
- Averaged $I_{K_2} - I_{K_1}$ decreases with deflection (from 10 – 8 μm).

MICROPLASMA DIFFERENTIAL CURRENT

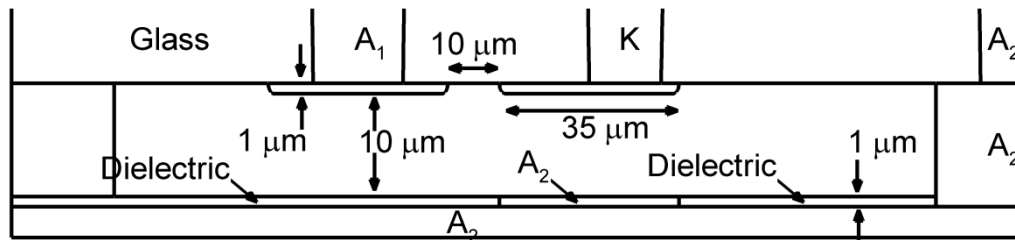


- Gap (A- K_2) spacing: 10-7 μm .
- A: 400 V, K: 0 V.
- 760-919 Torr Ar.
- Averaged $I_{K_2} + I_{K_1} \approx \text{const.}$
- 8 – 10 μm
 - Averaged $I_{K_2} - I_{K_1}$ decreases with deflection.
- Differential current $(K_2 + K_1)/(K_2 - K_1)$ linearly increases with deflection (external pressure).
- Operating regime (8-10 μm deflection or 0-20 Mpa)

MODEL GEOMETRY II

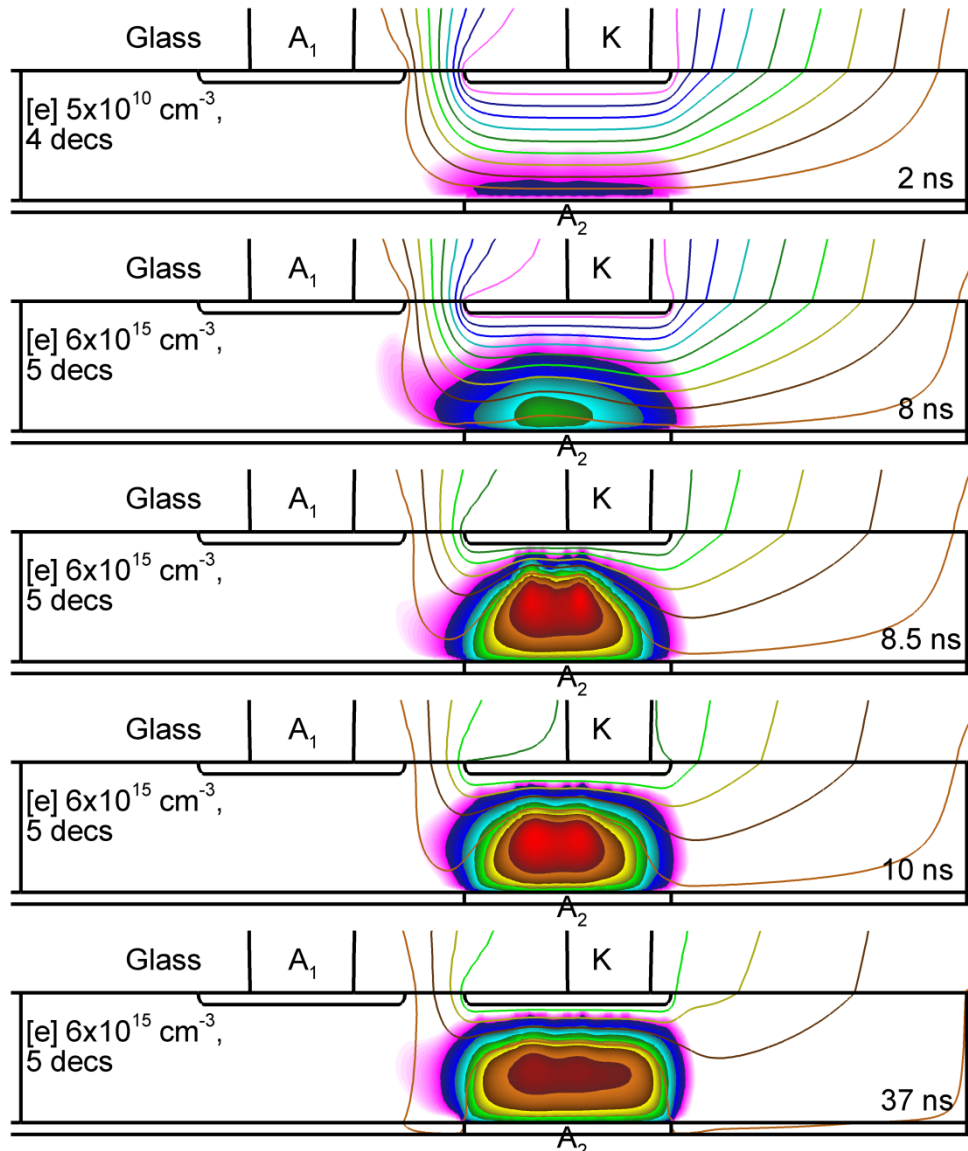


- Three electrodes (two anode) structure:
 - Inter-electrode spacing: K-A₁, K-A₂=10 μm .
 - A₁, A₂: grounded, K: -400 V.
 - Ballast resistor: 100 Ω (A₁, A₂) and 500 Ω (K).
 - Discharge initiated with emission current of $10^{-2} \text{ A-cm}^{-2}$ for 10 ns at cathode corner.
 - 1 atm Ar.



- X/Y=0.5

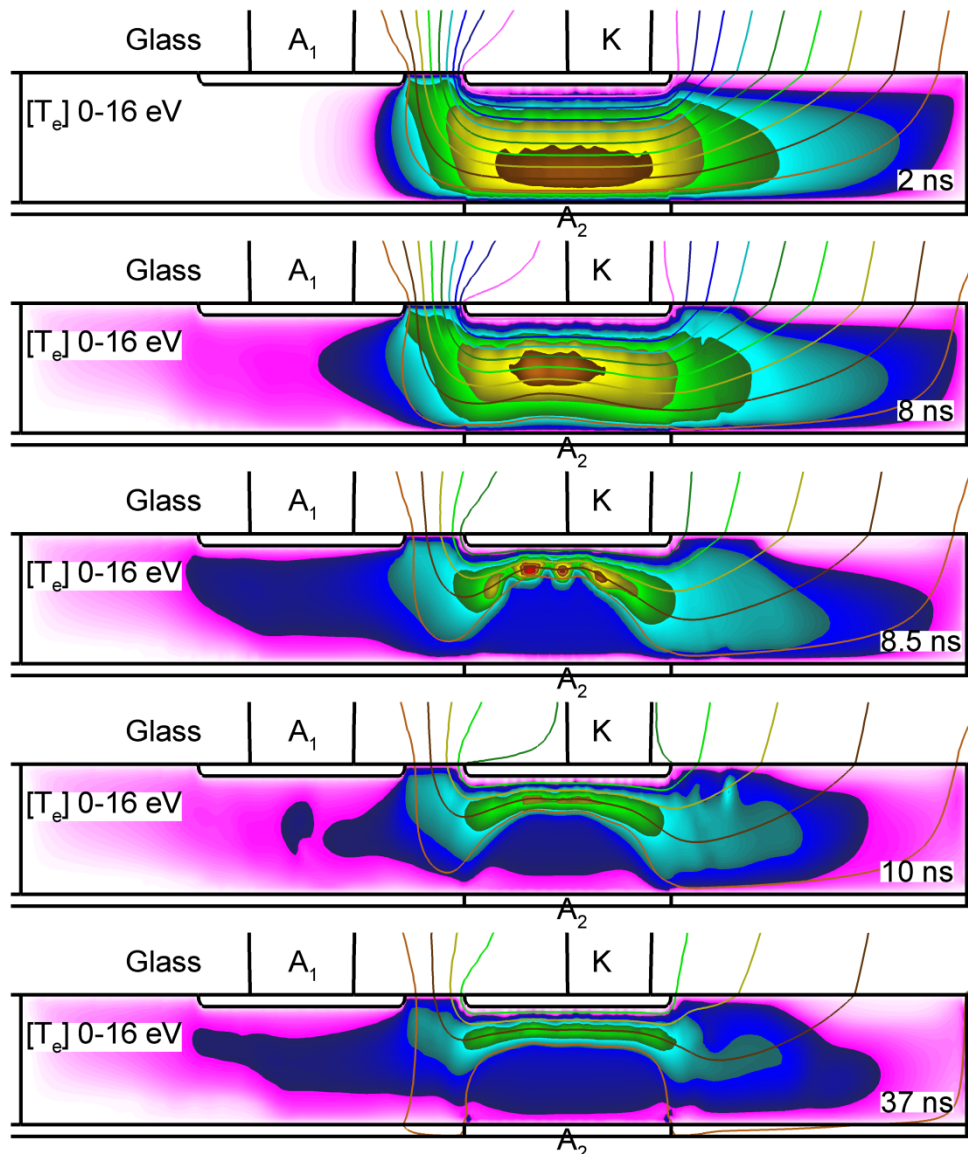
MICROPLASMA DYNAMICS: [e]



- Inter-electrode spacing: K-A₂, K-A₁=10 μm .
- A: 0 V, K: -400 V, $\Delta V = 40$ V (Contours).
- 760 Torr Ar.

- Avalanche between edges of cathode and anodes produces a conductive microplasma at K-A₂ within 10 ns.
- After avalanche, plasma shields out E-field and reduces E/N, T_e, S_e.
- Conductive plasma transfers A₂ potential to cathode. T_e and intense ionization peak at K.

MICROPLASMA DYNAMICS: $[T_e]$



- Inter-electrode spacing: $K-A_2$, $K-A_1=10 \mu\text{m}$.
- A : 0 V, K : -400 V, $\Delta V = 40$ V (Contours).
- 760 Torr Ar.

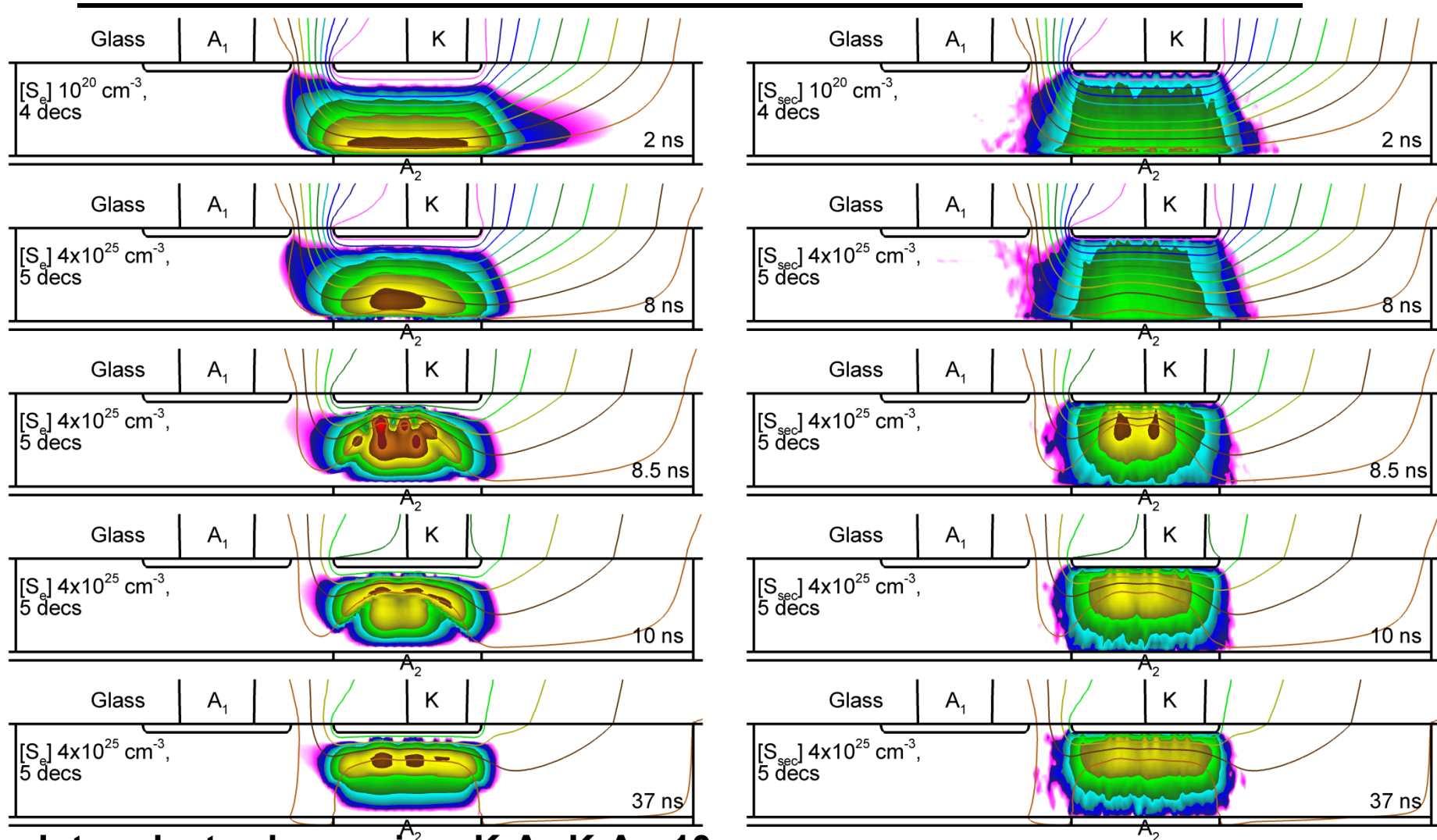
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MIN  MAX

- A large I_{A2} (~ 0.5 A) produced by plasma between $K-A_2$ sustained by K .
- A small I_{A1} (~ 0.5 mA) produced by electron transport from plasma at $K-A_2$.
- 3 orders of magnitude difference in current collection – differential current method is challenged.
- Ionization source S_{sec} at cathodes sheath is comparable with S_e from bulk plasma.

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MICROPLASMA DYNAMICS: $[S_e]$, $[S_{sec}]$



- Inter-electrode spacing: K-A₂, K-A₁=10 μm .
- A: 0 V, K: -400 V, $\Delta V = 40$ V (Contours).
- 760 Torr Ar.

CONCLUDING REMARKS

- Plasma behavior in a microdischarge based pressure sensor is computationally investigated .
- In two cathode structure, after electron avalanche and microplasma generated at A-K₂, conductive plasma transfers anode voltage to cathodes creating a high voltage drop and intense ionization at K₂ and A-K₁.
- I_{K2} produced by self-pulsing plasma at A-K₂ sustained by K₂.
- A repetitive ionization wave propagating from A to K₁ results in a striation on K₁.
- The striation produces a high frequency current pulses on cathodes.
- Differential current $(K_2+K_1)/(K_2-K_1)$ linearly increases with deflection in 10-8 μm deflection regime (0 – 20 MPa external pressure).