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P. Tzeferacos, C. Graziani, D. Lamb (Chicago),

F. Rincon (Toulouse), F. Califano (Pisa), F. Valentini (Calabria),

M. Kunz, J. Stone (Princeton), S. Melville (Harvard),

P. Helander (Greifswald), M. Strumik (Oxford)



Rincon, Califano, AAS, Valentini, PNAS in press (2016) [arXiv:1512.06455] Melville, AAS, Kunz, MNRAS in press (2016) [arXiv:1512.08131]

Rincon, AAS, Cowley, MNRAS 447, L45 (2015)

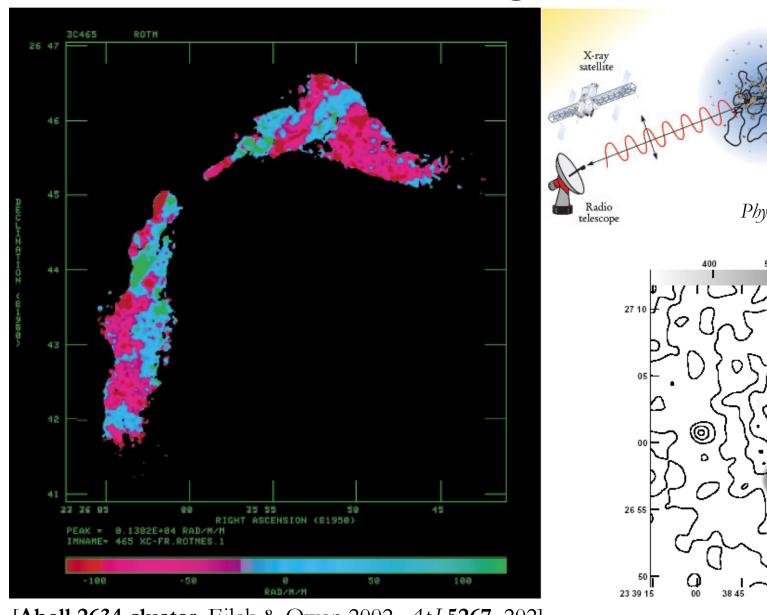
Kunz, AAS & Stone, PRL 112, 205003 (2014)

AAS et al., PRL 100, 184501 (2008); Rosin et al., MNRAS 413, 7 (2011)

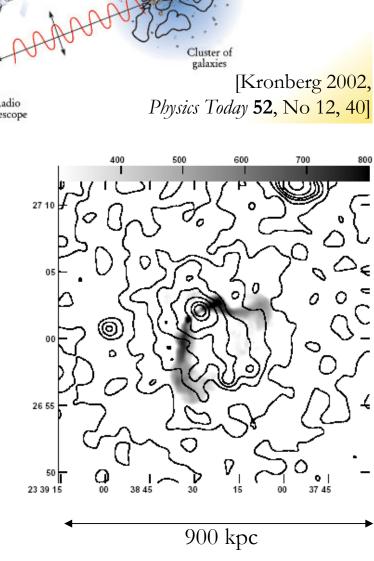
Tzeferacos et al., in preparation (2016); Meinecke et al., PNAS 112, 8211 (2015)

AAS et al., NJP 9, 300 (2007); AAS et al., ApJ 612, 276 (2004)

Cosmic Magnetism

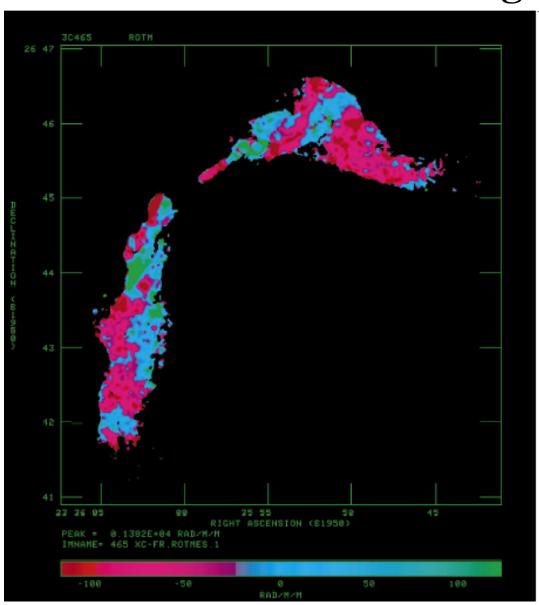


[Abell 2634 cluster, Eilek & Owen 2002, ApJ 5267, 202]



Radio galaxy

Cosmic Magnetism



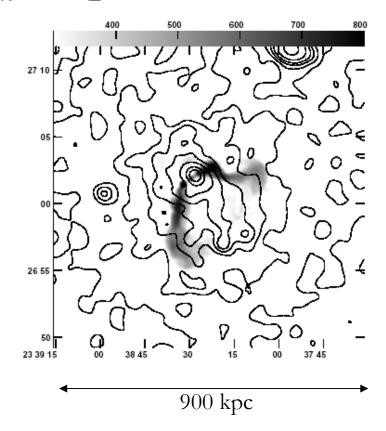
[Abell 2634 cluster, Eilek & Owen 2002, ApJ 5267, 202]

Typically,

$$B \sim 10^{-6} \text{ G}, \quad \beta \sim 10^2$$

Crucially (imho),

$$\frac{B^2}{8\pi} \sim \frac{\rho u^2}{2}$$



Turbulence Makes the Field

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{u} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$

This equation is linear in **B**, so field will either decay to zero or grow to dynamical strength. Probably the latter.

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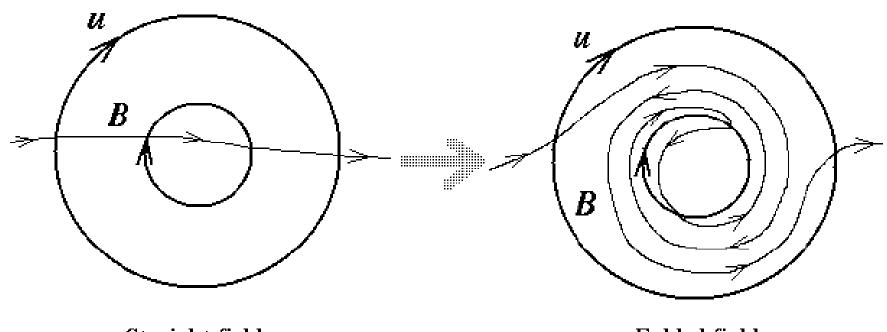
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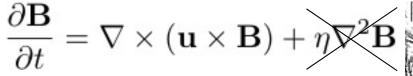
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Straight field

Folded field



All you need is a

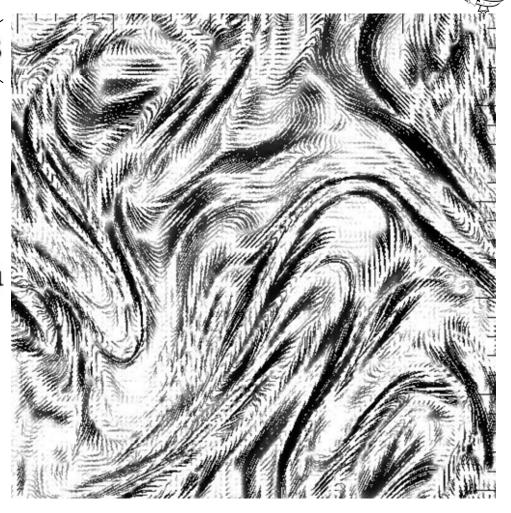
chaotic flow

Basic idea:

$$\frac{\mathrm{d}\mathbf{B}}{\mathrm{d}t} \equiv \frac{\partial \mathbf{B}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{B} = \mathbf{B} \cdot \nabla \mathbf{u}$$

$$\frac{\mathrm{d}B}{\mathrm{d}t} = (\mathbf{b}\mathbf{b} : \nabla \mathbf{u})B \equiv \gamma B$$

$$\ln B \sim \int^t \mathrm{d}t' \, (\mathbf{b}\mathbf{b} : \nabla \mathbf{u})(t')$$



So, roughly, field in Lagrangian frame accumulates as random walk

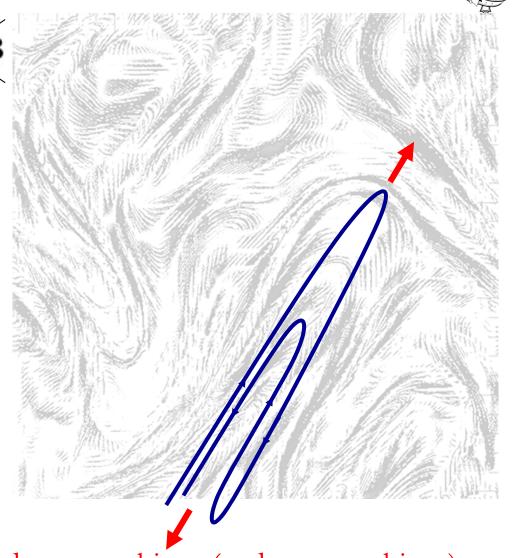
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Key effect: a succession of random stretchings (and un-stretchings)

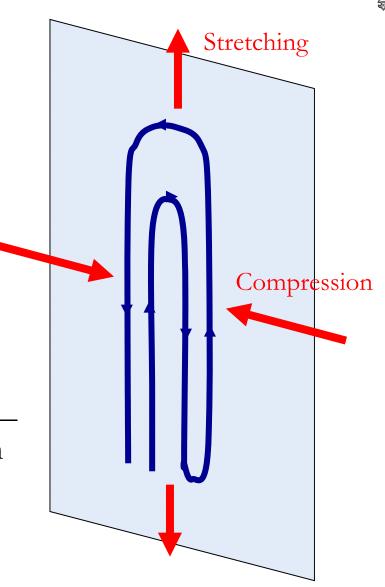


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Nuance: naïve stretching-compression scenario would lead to destruction of the field (and does, in 2D)



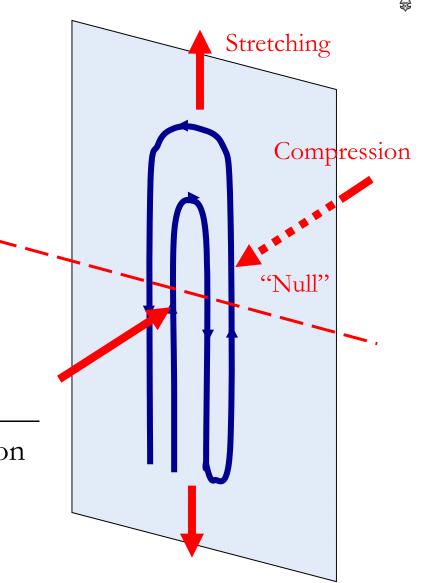


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Nuance: naïve stretching-compression scenario would lead to destruction of the field (and does, in 2D) In 3D, surviving folds are in the stretching-null plane [Zeldovich et al. 1984, *JFM* **144**, 1] AAS et al., *ApJ* **612**, 276 (2004)



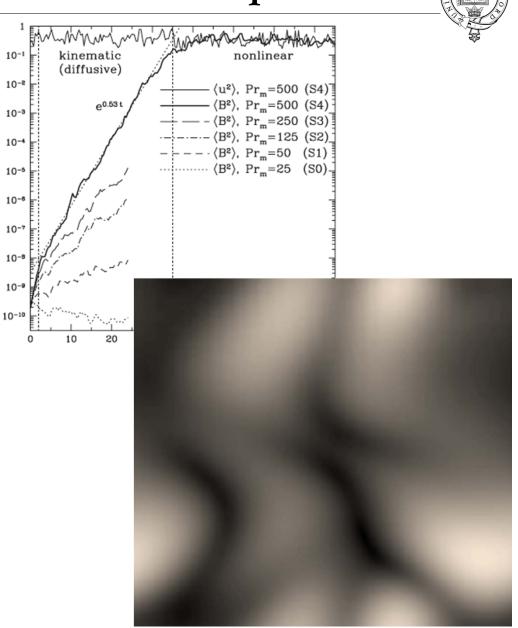
Turbulent Dynamo: Numerical Experiment

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{u} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$

All you need is a chaotic flow (and large enough Rm)

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The bottom line is that turbulent dynamo works if $Rm > Rm_c \sim 50$ to 200 (depending on Re)



AAS et al., NJP 9, 300 (2007)

AAS et al., *ApJ* **612**, 276 (2004)

Turbulent Dynamo: Numerical Experiment



$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{u} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$

First evidence was in 1981:

All you need is a chaotic flow (and large enough Rm)

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Volume 47, Number 15

PHYSICAL REVIEW LETTERS

12 October 1981

Helical and Nonhelical Turbulent Dynamos

M. Meneguzzi

Centre National de la Recherche Scientifique and Section d'Astrophysique, Division de la Physique, Centre d'Etudes Nucléaires de Saclay, F-91191 Gif-Sur-Yvette, France

and

U. Frisch

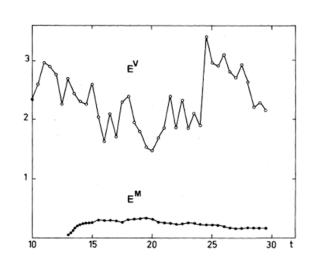
Centre National de la Recherche Scientifique, Observatoire de Nice, F-06007 Nice, France

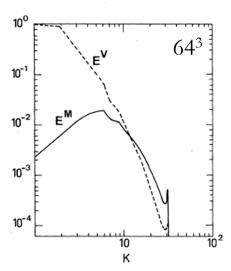
and

A. Pouquet^(a)

Centre National de la Recherche Scientifique, Observatoire de Meudon, F-92190 Meudon, France (Received 13 April 1981)

Direct numerical simulations of three-dimensional magnetohydrodynamic turbulence with kinetic and magnetic Reynolds numbers up to 100 are presented. Spatially intermittent magnetic fields are observed in a flow with nonhelical driving. Small-scale helical driving produces strong large-scale nearly force-free magnetic fields.





Turbulent Dynamo in Laser Lab (G. Gregori)

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{u} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$

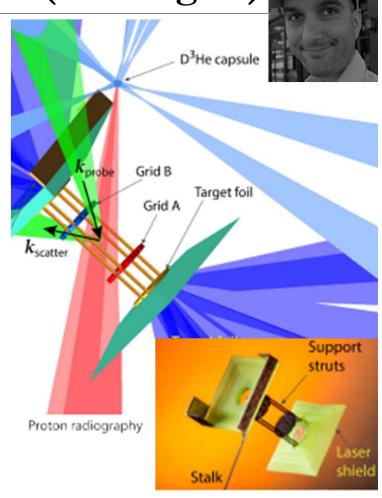
All you need is a chaotic flow (and large enough Rm)

Experiment on Omega laser:

two jet flows pass through grids, collide, give turbulent cloud with Re ~ 5000

The bottom line is that turbulent dynamo works if $Rm > Rm_c \sim 50$ to 200 (depending on Re)

AAS et al., NJP 9, 300 (2007)



Tzeferacos et al., in preparation (2016) Meinecke et al., PNAS 112, 8211 (2015)

Turbulent Dynamo in Laser Lab (G. Gregori)

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Experiment on Omega laser:

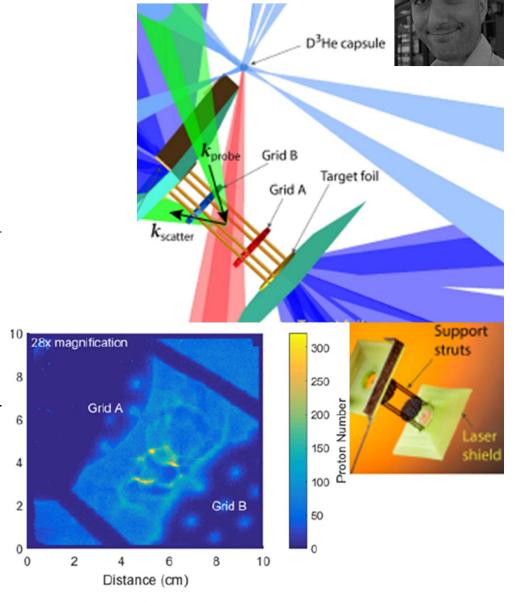
 $Rm \sim 1000 > Rm_c$

field amplified to B ~ 300kG

Details: come to HEDLA-2016!

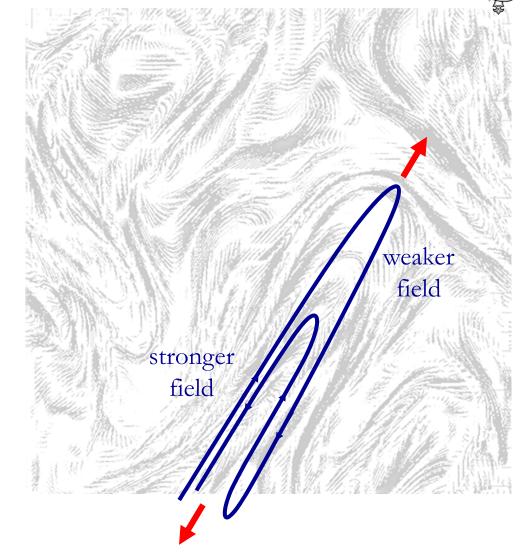
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Tzeferacos et al., in preparation (2016) Meinecke et al., PNAS 112, 8211 (2015)

In Fact, This Is All Irrelevant to Astro...



$$\frac{\mathrm{d}B}{\mathrm{d}t} = (\mathbf{b}\mathbf{b} : \nabla \mathbf{u})B \equiv \gamma B$$

Key effect: a succession of random stretchings (and un-stretchings)

Collisionless Plasma: Adiabatic Constraints

Changing magnetic field causes local pressure anisotropies:

$$\frac{1}{p_{\perp}} \frac{\mathrm{d}p_{\perp}}{\mathrm{d}t} = \frac{1}{B} \frac{\mathrm{dB}}{\mathrm{d}t}$$

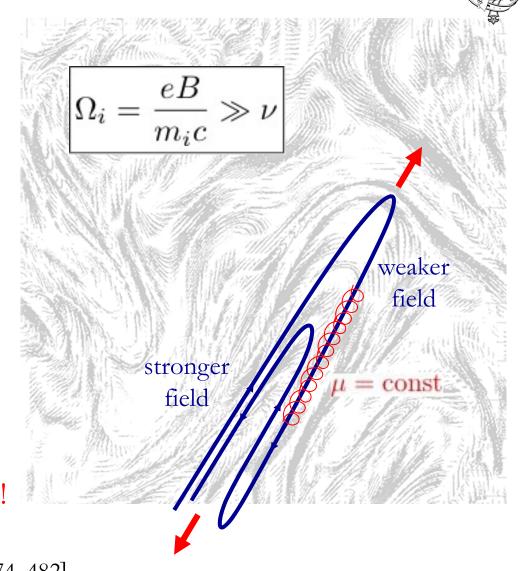
conservation of $\mu = v_{\perp}^2/B$

$$\begin{split} \frac{1}{2p_{\parallel}} \frac{\mathrm{d}p_{\parallel}}{\mathrm{d}t} &= -\frac{1}{B} \frac{\mathrm{dB}}{\mathrm{d}t} \\ \text{conservation of } J &= \oint \mathrm{d}\ell \, v_{\parallel} \\ \frac{\mathrm{d}B}{\mathrm{d}t} &= (\mathbf{b}\mathbf{b} : \nabla \mathbf{u})B \equiv \gamma B \end{split}$$

It is very hard to change *B* in the face of these constraints!

[CGL supports no dynamo action:

Santos-Lima et al. 2011, Proc. IAU No 274, 482]



Helander, Strumik & AAS, in preparation (2016)

Weak Collisions → Pressure Anisotropy

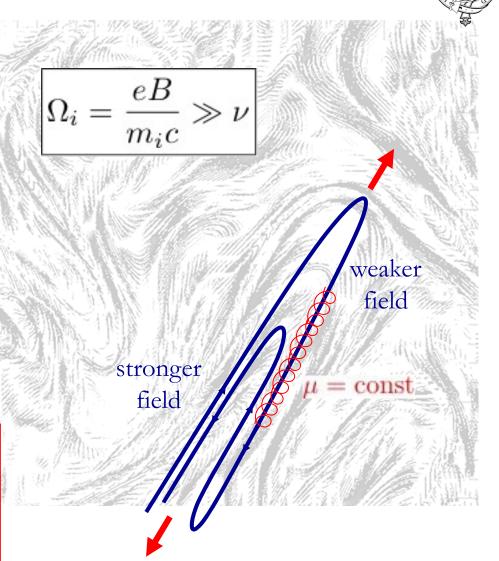
Changing magnetic field causes local pressure anisotropies:

$$\frac{1}{p_{\perp}} \frac{\mathrm{d}p_{\perp}}{\mathrm{d}t} = \frac{1}{B} \frac{\mathrm{dB}}{\mathrm{d}t} - \nu \frac{p_{\perp} - p_{\parallel}}{p_{\perp}}$$

conservation of $\mu = v_{\perp}^2/B$

$$\frac{1}{2p_{\parallel}}\frac{\mathrm{d}p_{\parallel}}{\mathrm{d}t} = -\frac{1}{B}\frac{\mathrm{dB}}{\mathrm{d}t} - \nu \frac{p_{\parallel} - p_{\perp}}{p_{\parallel}}$$
 conservation of $J = \oint \mathrm{d}\ell \, v_{\parallel}$

$$\frac{\mathrm{d}B}{\mathrm{d}t} = (\mathbf{b}\mathbf{b} : \nabla \mathbf{u})B \equiv \gamma B$$



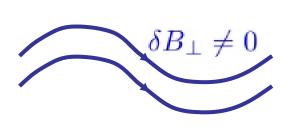
(compressions/rarefactions & heat fluxes are also sources of local pressure anisotropy)

Pressure Anisotropy → Microinstabilities



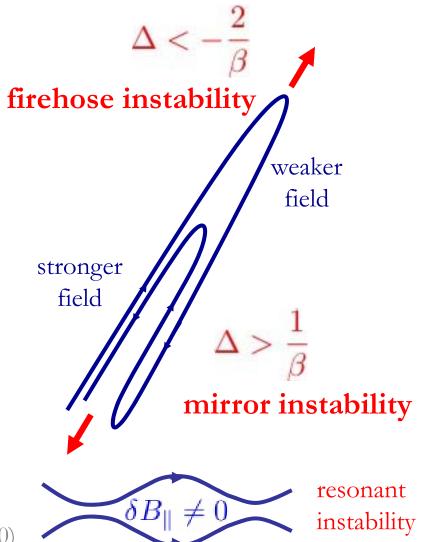
Instabilities are fast, small scale (~Larmor).

They are instantaneous compared to "fluid" dynamics.



destabilised Alfvén wave

$$\frac{\mathrm{d}B}{\mathrm{d}t} = (\mathbf{b}\mathbf{b} : \nabla \mathbf{u})B \equiv \gamma B$$

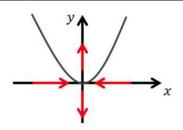


Pressure Anisotropy → Microinstabilities



Scott Melville:

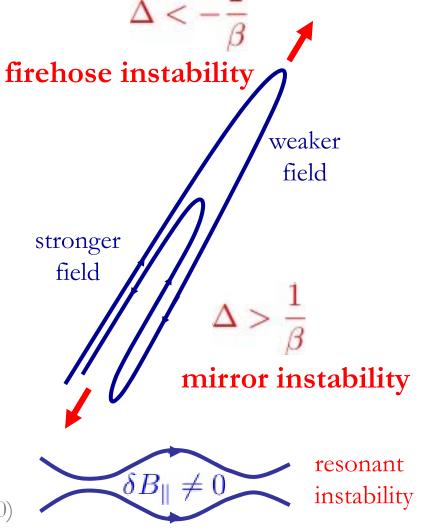
folding field goes firehose-unstable (in a 1D Braginskii model)



Note the square shape of the unstable fold...



$$\Delta \equiv \frac{p_{\perp} - p_{||}}{p} \sim \frac{1}{\nu} \frac{1}{B} \frac{\mathrm{d}B}{\mathrm{d}t} = \frac{\gamma}{\nu}$$



AAS et al., ApJ 629, 139 (2005); MNRAS 405, 291 (2010)

Instabilities in a Box (M. Kunz)

Hybrid kinetic system solved by PEGASUS code (PIC):

$$\left(\frac{\partial}{\partial t} - Sx \frac{\partial}{\partial y}\right) f_{\rm i} + \boldsymbol{v} \cdot \boldsymbol{\nabla} f_{\rm i} +$$

$$\left[\frac{Ze}{m_{\rm i}}\left(\boldsymbol{E} + \frac{\boldsymbol{v}}{c} \times \boldsymbol{B}\right) + Sv_x \hat{\boldsymbol{y}}\right] \cdot \frac{\partial f_{\rm i}}{\partial \boldsymbol{v}} = 0$$

$$\left(\frac{\partial}{\partial t} - Sx\frac{\partial}{\partial y}\right)\boldsymbol{B} = -c\boldsymbol{\nabla} \times \boldsymbol{E} - SB_x\hat{\boldsymbol{y}}$$

$$\boldsymbol{E} = -\frac{\boldsymbol{u}_{\mathrm{i}} \times \boldsymbol{B}}{c} + \frac{(\boldsymbol{\nabla} \times \boldsymbol{B}) \times \boldsymbol{B}}{4\pi Z e n_{\mathrm{i}}} - \frac{T_{\mathrm{e}} \boldsymbol{\nabla} n_{\mathrm{i}}}{e n_{\mathrm{i}}}$$

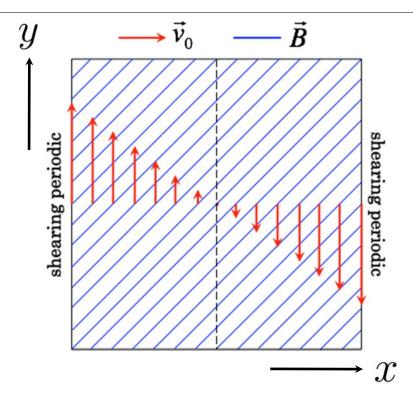


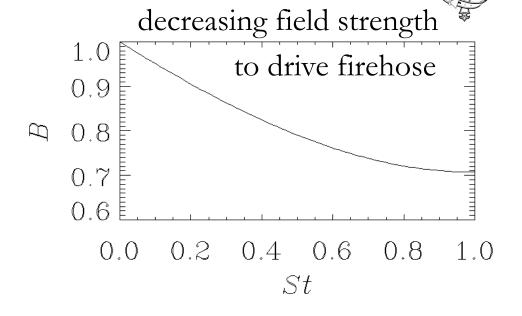
Kunz, Stone & Bai, *JCP* **259**, 154 (2014)

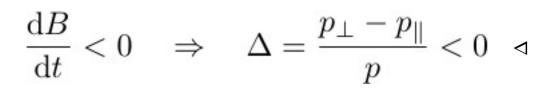
...in a shearing sheet $\mathbf{u} = -Sx\hat{\mathbf{y}}$

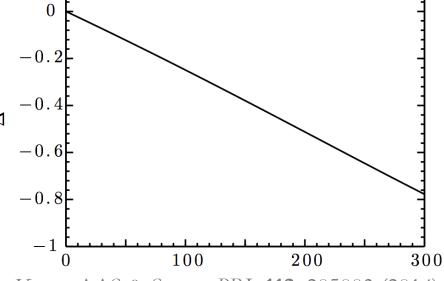


Firehose Instability (M. Kunz)





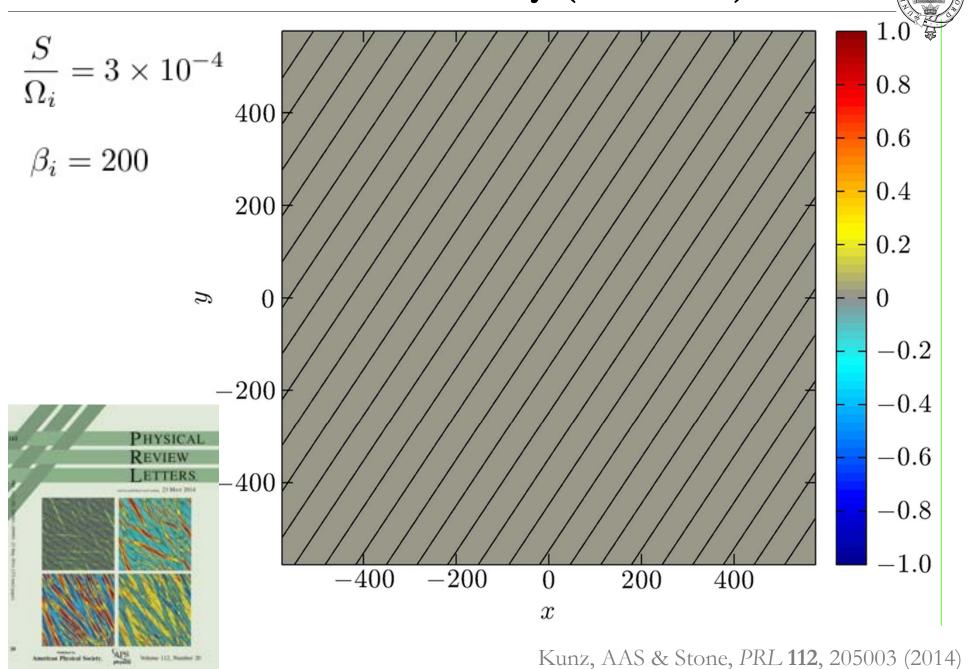




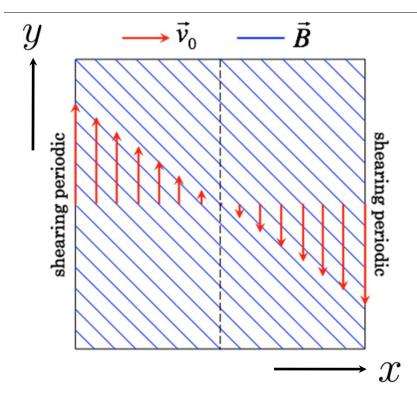


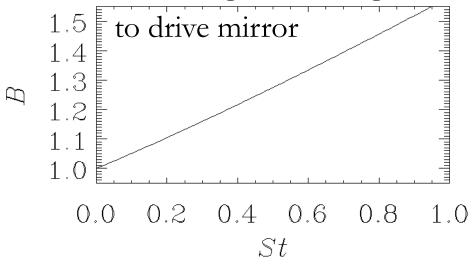
Kunz, AAS & Stone, PRL 112, 205003 (2014)

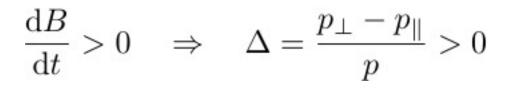
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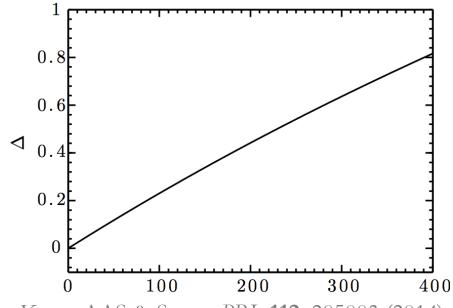


Mirror Instability (M. Kunz)





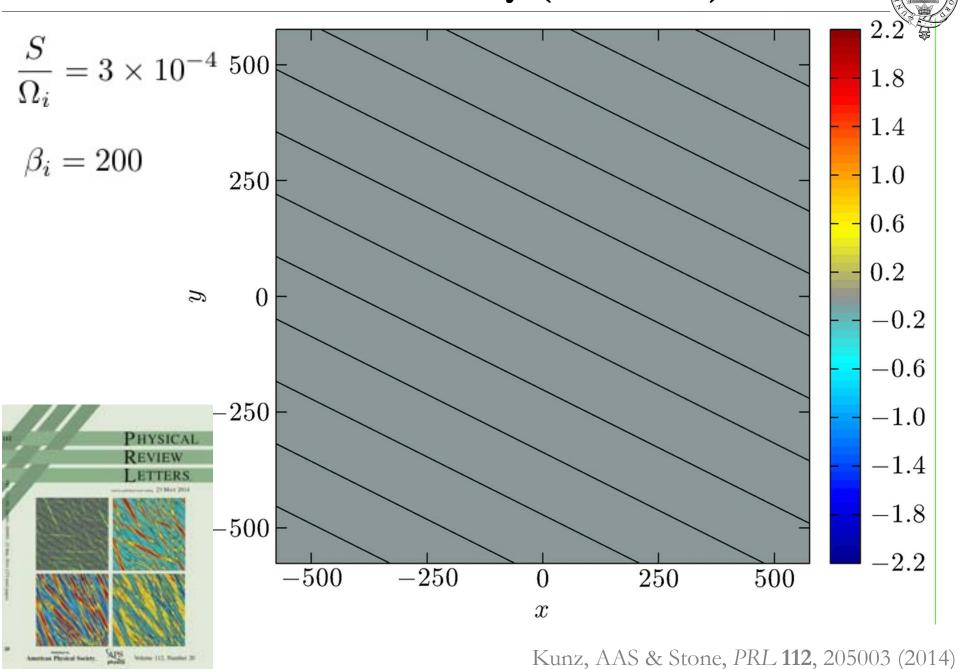






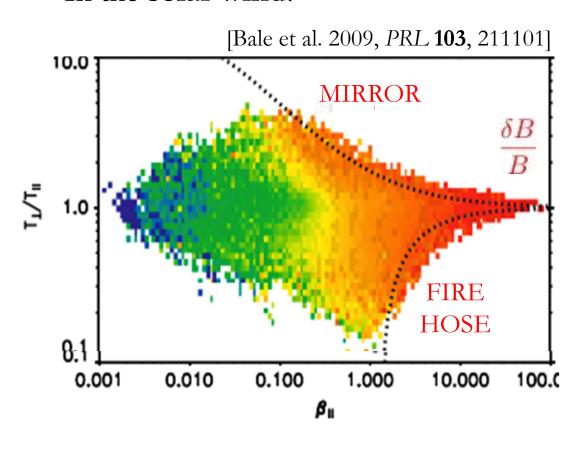
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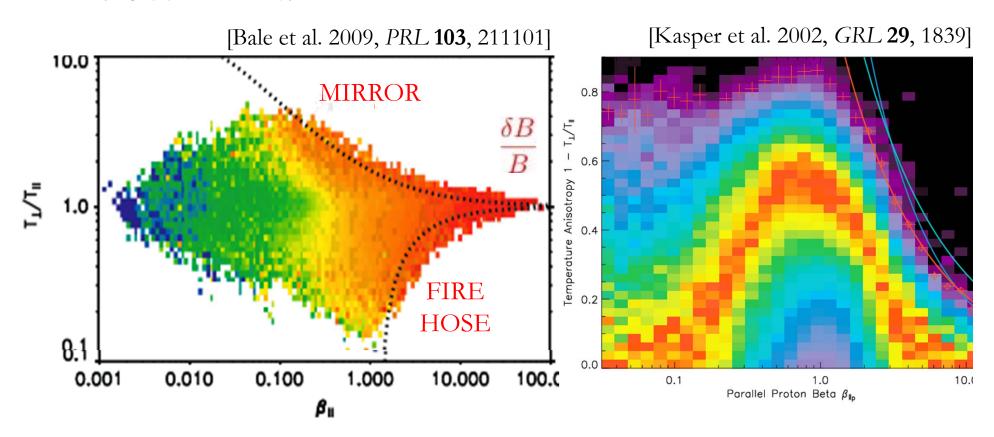
In the solar wind:



$$\Delta \equiv \frac{p_{\perp} - p_{\parallel}}{p} \sim \frac{1}{\nu} \frac{1}{B} \frac{\mathrm{d}B}{\mathrm{d}t} = \frac{\gamma}{\nu} \in \left[-\frac{2}{\beta}, \frac{1}{\beta} \right]$$

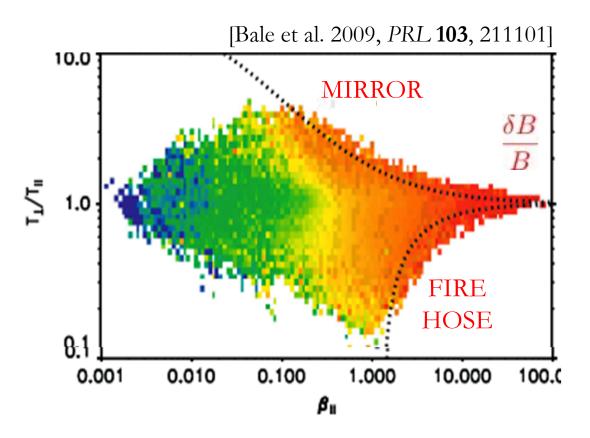


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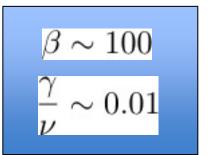
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In the solar wind:

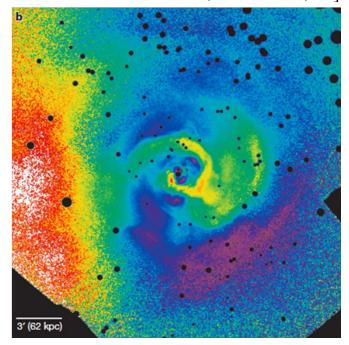


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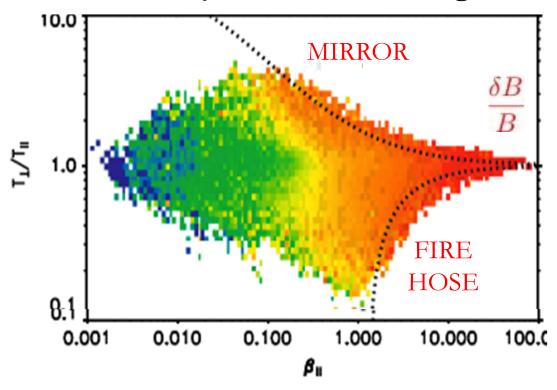
In galaxy clusters:



[Image: Zhuravleva et al. 2014, *Nature* **515**, 85]



How do you evolve the field from small to large while keeping everywhere within marginal stability boundaries?

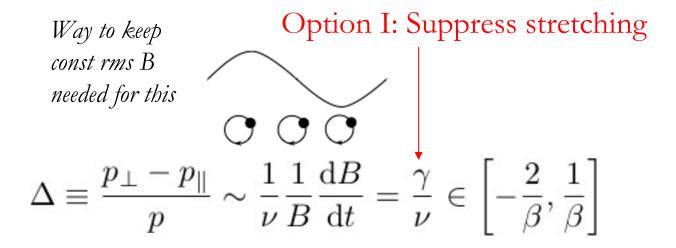


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Mogavero & AAS, *MNRAS* **440**, 3226 (2014)

Effective Closure Options

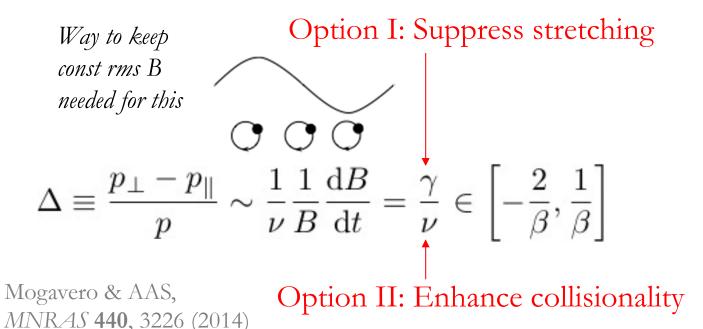
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Mogavero & AAS, *MNRAS* **440**, 3226 (2014)

Effective Closure Options

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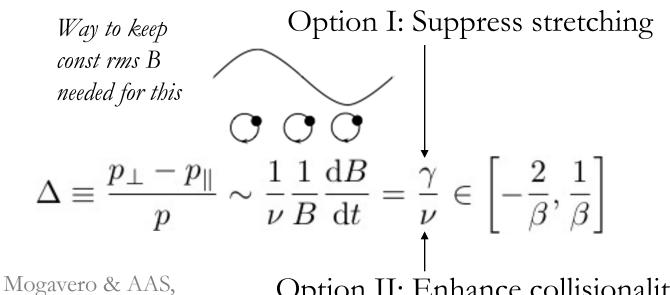


Anomalous scattering of particles by Larmor scale fluctuations needed for this

PLASMA DYNAMO?

How do you evolve the field from small to large while keeping everywhere within marginal stability boundaries?

In view of these complications, does dynamo work in a weakly collisional plasma?



Mogavero & AAS, Option II: Enhance collisionality MNRAS 440, 3226 (2014)

Anomalous scattering of particles by Larmor scale fluctuations needed for this



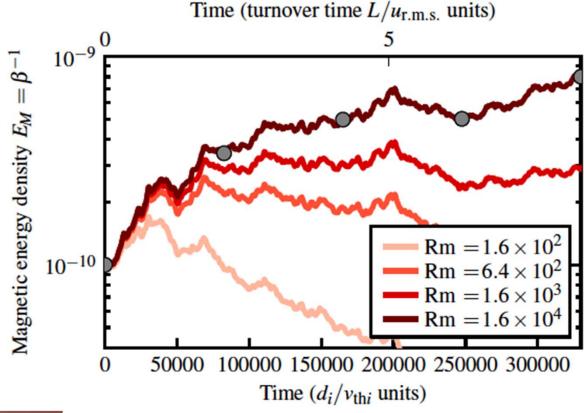
Hybrid kinetic system solved by a Vlasov code (grid):



$$n_e = n_i$$

$$\frac{\partial \mathbf{B}}{\partial t} = -c\nabla \times \mathbf{E}$$





UNMAGNETISED

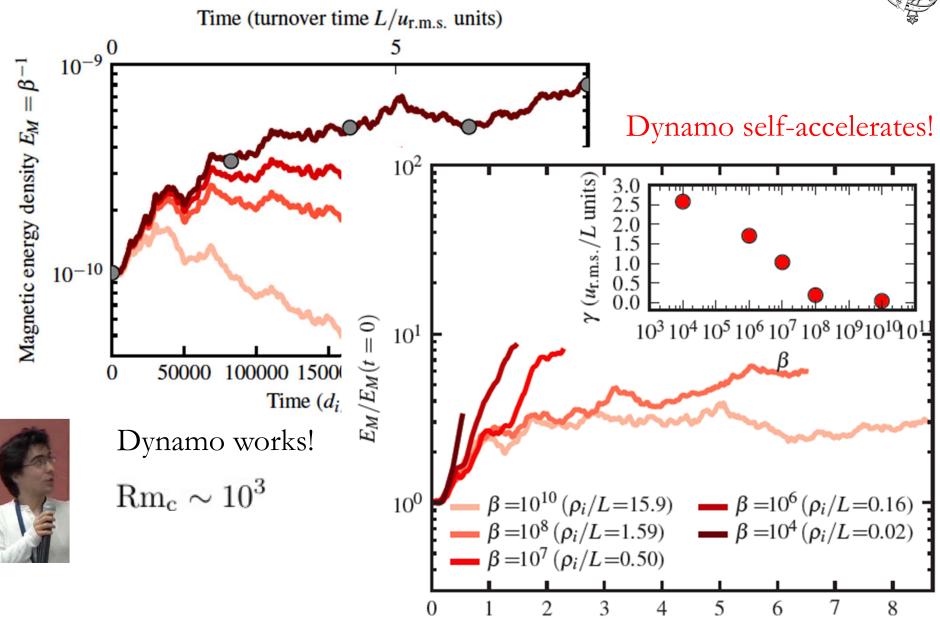
$$\beta = 10^{10} \ \frac{\rho_i}{L} \simeq 16$$



Dynamo works!

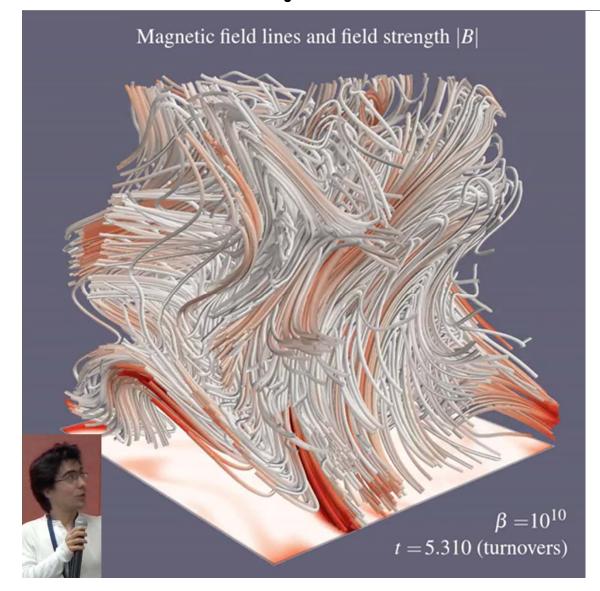
 ${\rm Rm_c} \sim 10^3$





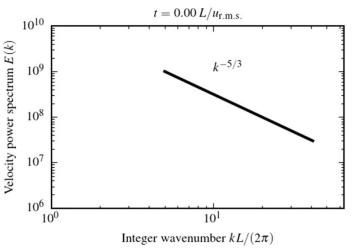
Rincon et al., PNAS in press (2016) [arXiv:1512.06455] Time (turnover time $L/u_{\rm r.m.s.}$ units)

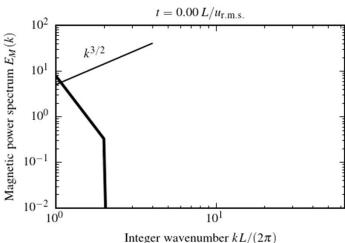




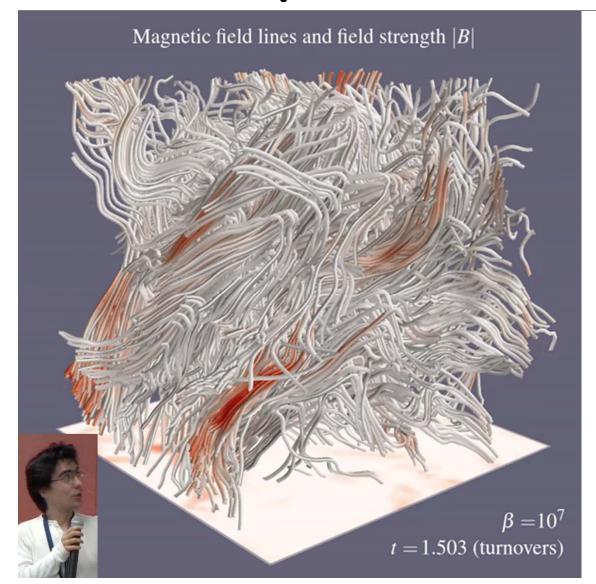
UNMAGNETISED

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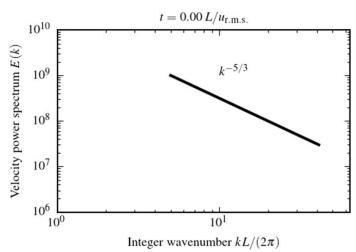


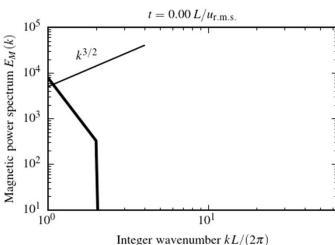
Rincon et al., PNAS in press (2016) [arXiv:1512.06455]



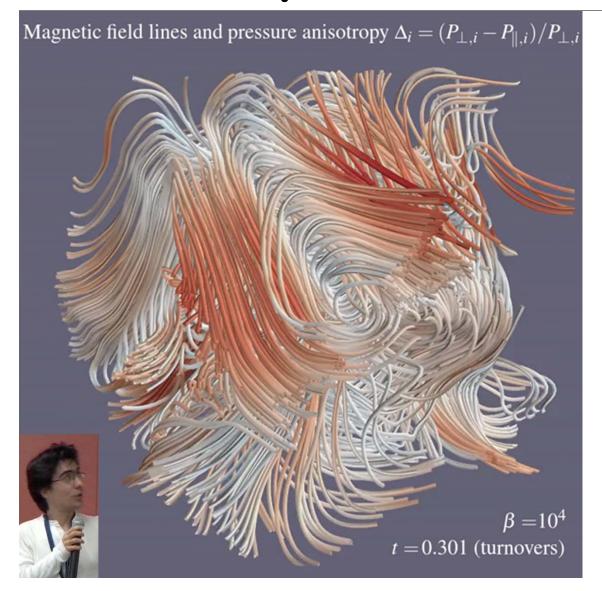
NEARLY MAGNETISED

$$\beta = 10^7 \quad \frac{\rho_i}{L} \simeq 0.5$$



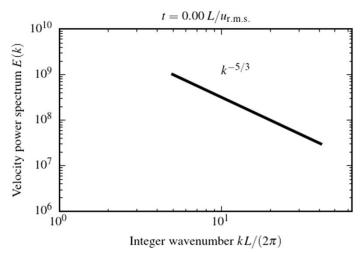


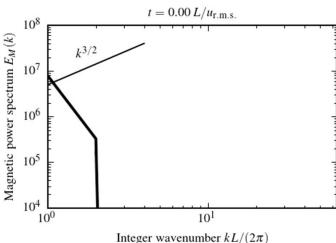
Rincon et al., PNAS in press (2016) [arXiv:1512.06455]



FULLY MAGNETISED

$$\beta = 10^4 \quad \frac{\rho_i}{L} \simeq 0.02$$





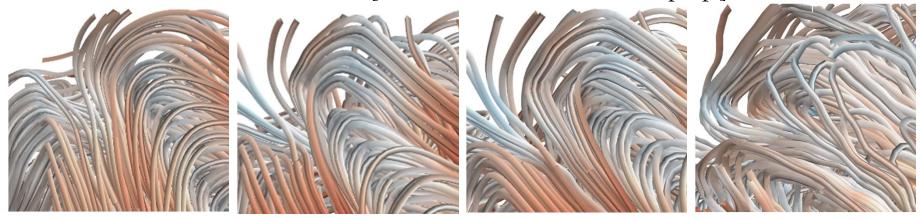
Rincon et al., *PNAS* in press (2016) [arXiv:1512.06455]

Plasma Dynamo Simulations by F. Rincon



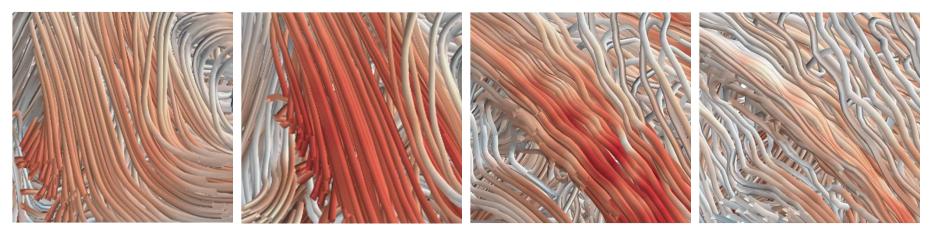
Firehoses in bends: note square bends

[cf. Melville & AAS 2016, in prep.]



Mirrors in stretched folds: "bubbles" filled with trapped particles

[cf. Rincon, AAS & Cowley 2015, MNRAS 447, L45]

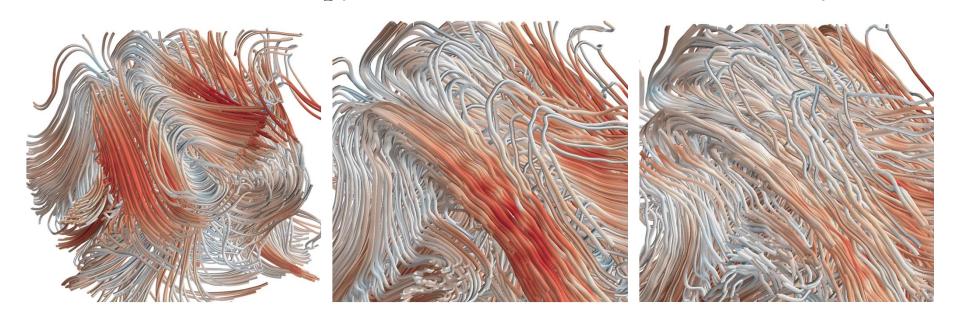


Rincon et al., *PNAS* in press (2016) [arXiv:1512.06455]

Plasma Dynamo Simulations by F. Rincon



Pressure anisotropy relaxes in some self-consistent way:

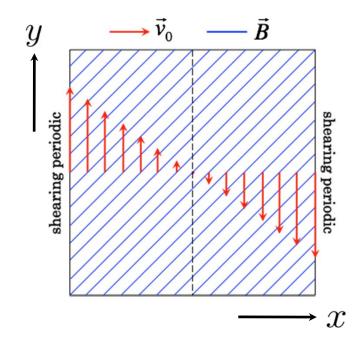


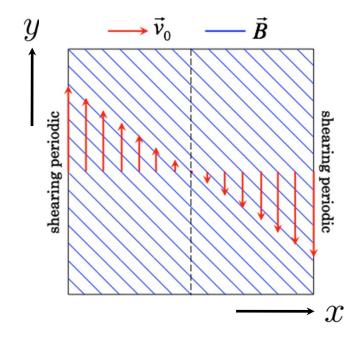
It would be fascinating to follow this dynamo for a long time and see how the macro-micro scale interaction works, how anisotropy adjusts, etc.

But this is currently unaffordable in 3D3V.

Back to Instabilities in a Box (M. Kunz)

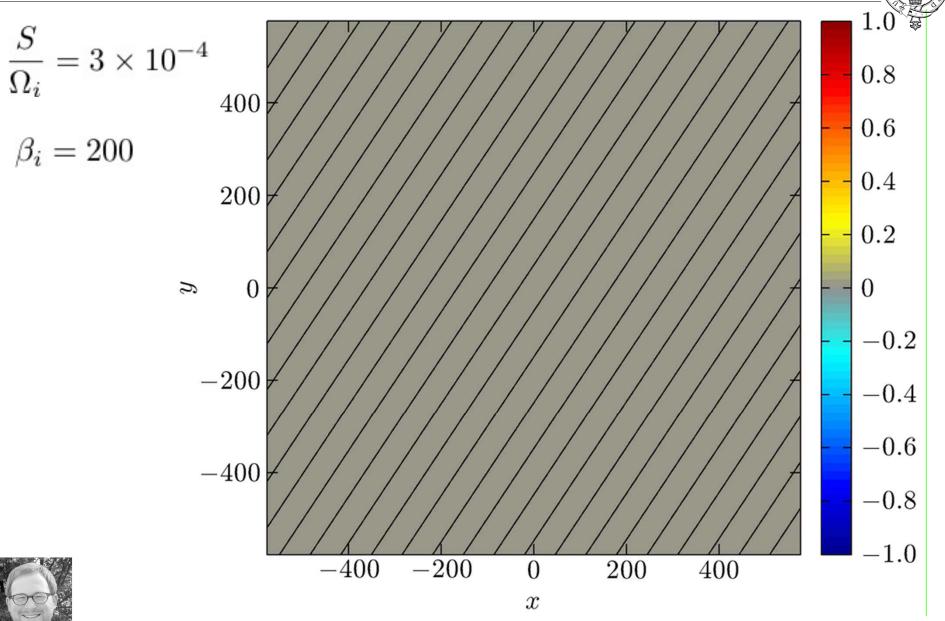








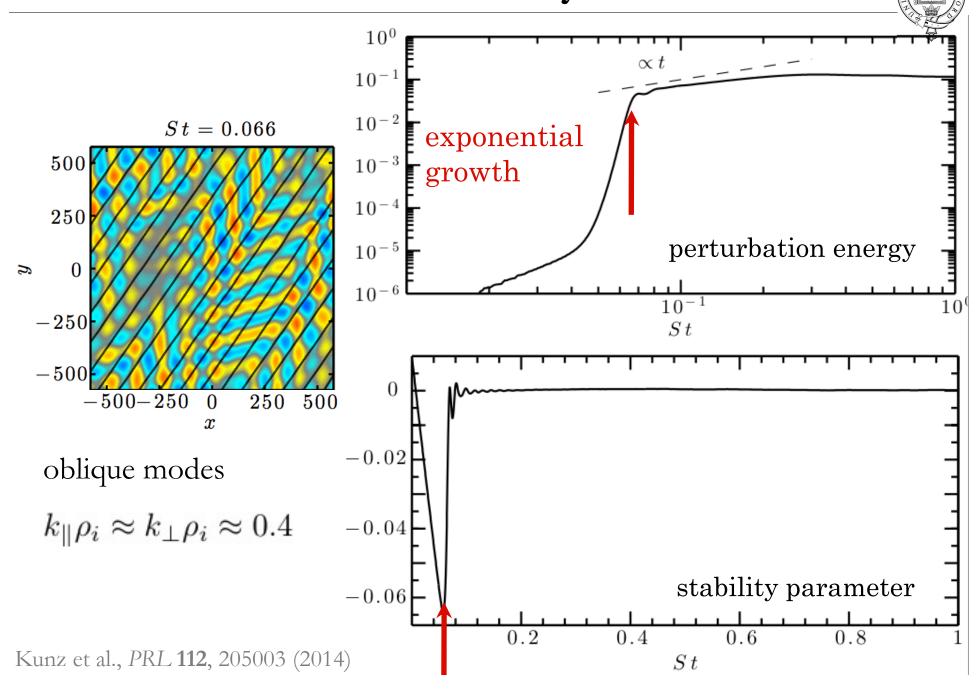
Firehose Instability (M. Kunz)

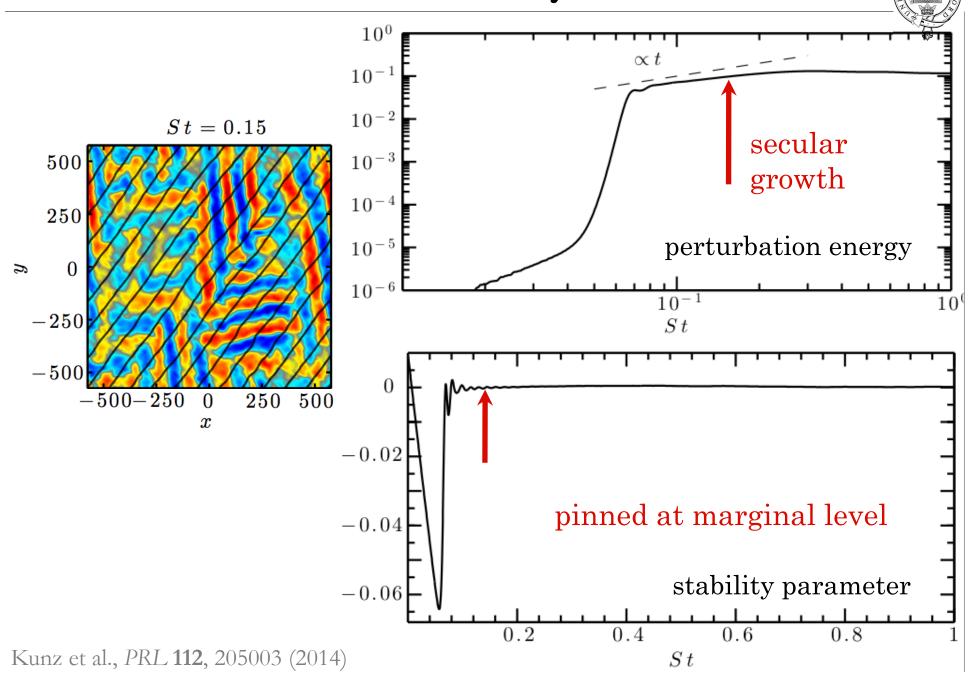




Kunz, AAS & Stone, PRL 112, 205003 (2014)

Firehose Instability: Linear

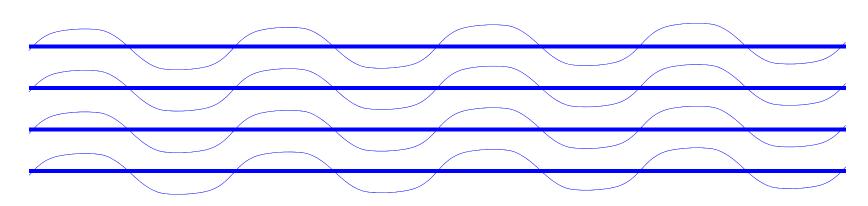






$$\overline{B^2} = \overline{|\mathbf{B}_0 + \delta \mathbf{B}_\perp|^2} = B_0^2 + \overline{|\delta \mathbf{B}_\perp|^2}$$

$$\Delta = 3 \int^t \! \mathrm{d}t' \, \overline{\frac{\mathrm{d} \ln B}{\mathrm{d}t}} = \int^t \! \mathrm{d}t' \left(-3 \left| \frac{\mathrm{d} \ln B_0}{\mathrm{d}t} \right| + \frac{3}{2} \frac{\mathrm{d}}{\mathrm{d}t} \, \overline{|\delta \mathbf{B}_\perp|^2} \right) \to -\frac{2}{\beta}$$
pressure pressure marginal anisotropy anisotropy stability driven by shear from firehose

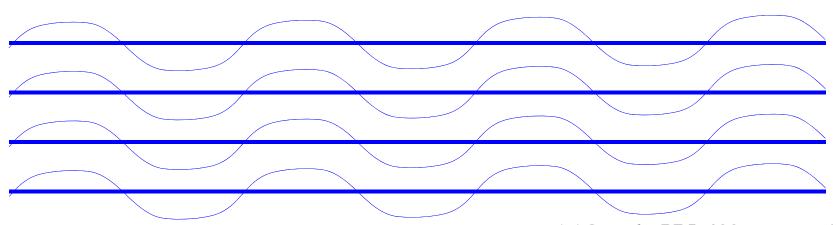


AAS et al., *PRL* **100**, 081301 (2008) Rosin et al., *MNRAS* **413**, 7 (2011)



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pressure pressure pressure marginal anisotropy anisotropy stability driven by shear from firehose



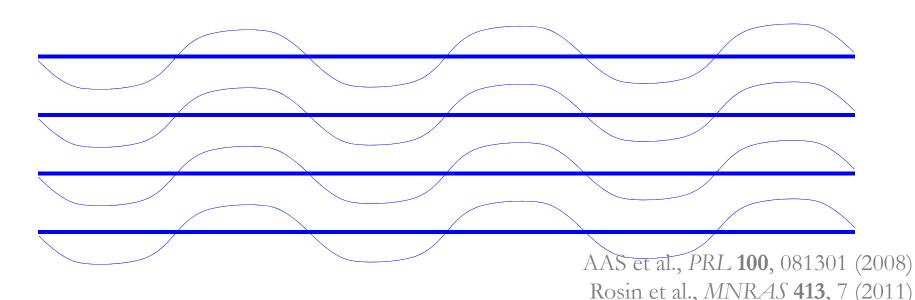
AAS et al., *PRL* **100**, 081301 (2008)

Rosin et al., MNRAS 413, 7 (2011)



$$\overline{B^2} = \overline{|\mathbf{B}_0 + \delta \mathbf{B}_\perp|^2} = B_0^2 + \overline{|\delta \mathbf{B}_\perp|^2}$$

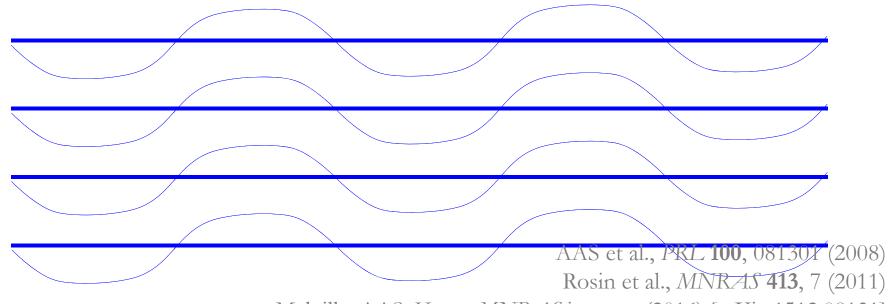
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$$\overline{B^2} = \overline{|\mathbf{B}_0 + \delta \mathbf{B}_\perp|^2} = B_0^2 + \overline{|\delta \mathbf{B}_\perp|^2}$$

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pressure pressure pressure marginal anisotropy anisotropy stability driven by shear from firehose





$$\overline{B^2} = \overline{|\mathbf{B}_0 + \delta \mathbf{B}_\perp|^2} = B_0^2 + \overline{|\delta \mathbf{B}_\perp|^2}$$

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pressure anisotropy driven by shear

pressure anisotropy

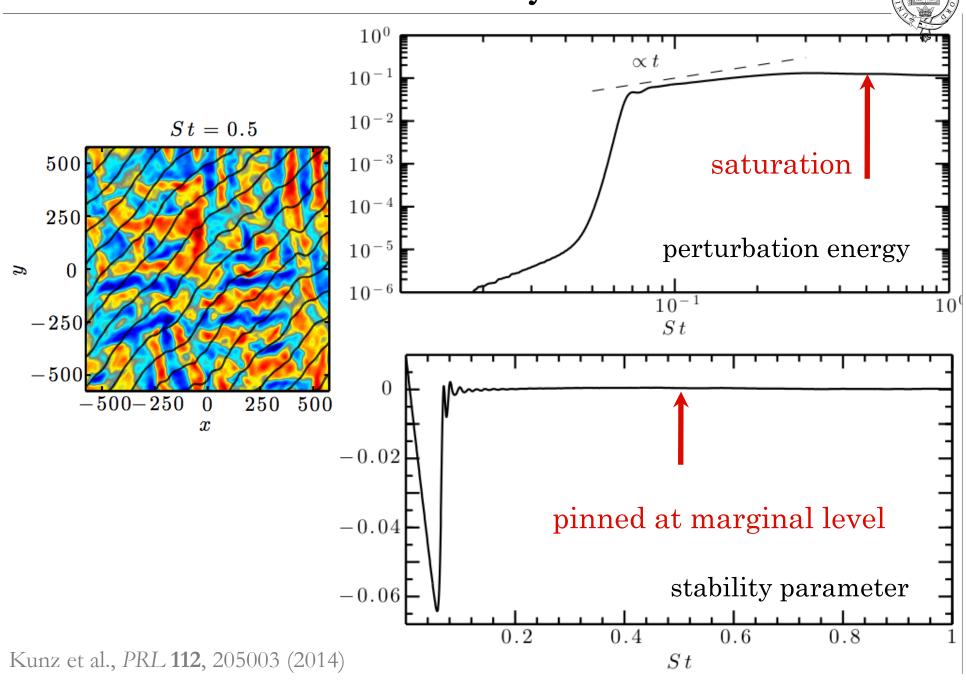
marginal stability

from firehose

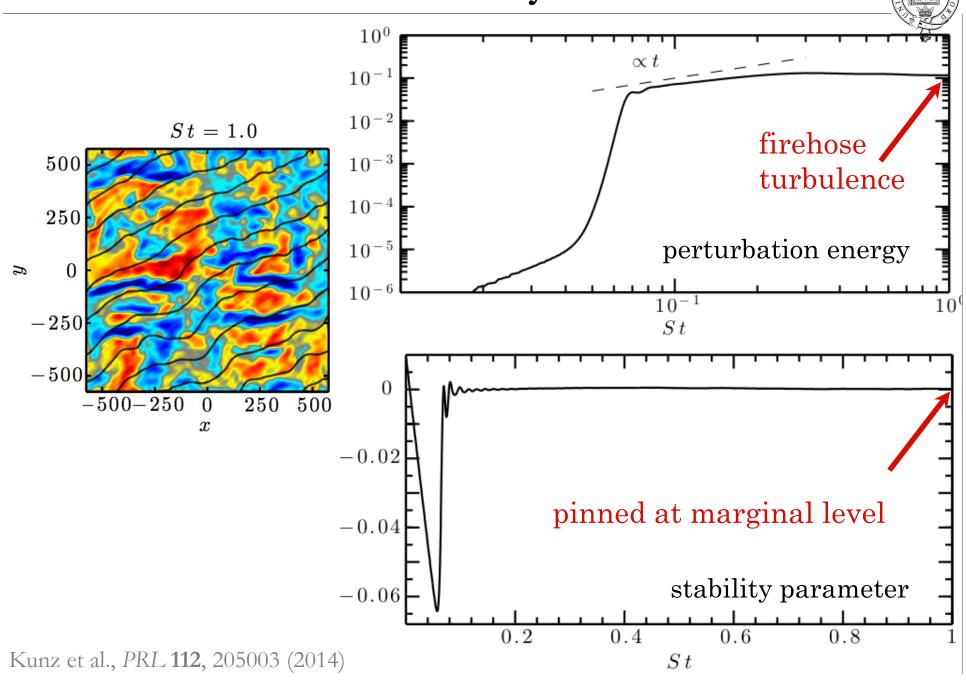
$$\frac{3}{2} \frac{\overline{|\delta \mathbf{B}_{\perp}|^2}}{B_0^2} = 3S \int^t dt' \, \hat{b}_x(t') \hat{b}_y(t') - \frac{2}{\beta} \sim St \quad \text{secular growth}$$

AAS et al., PRL **100**, 081307 (2008) Rosin et al., MNRAS 413, 7 (2011)

Firehose Instability: Saturated



Firehose Instability: Saturated

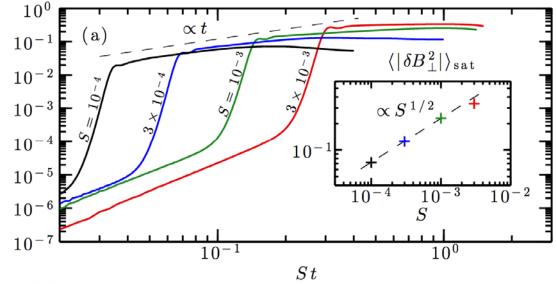


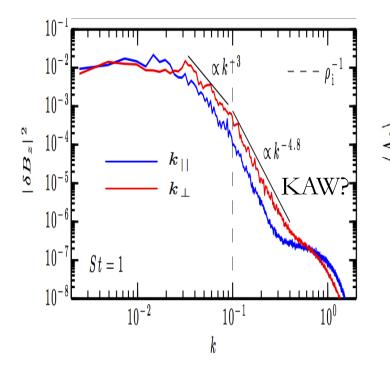
Firehose Saturates at Small Amplitudes

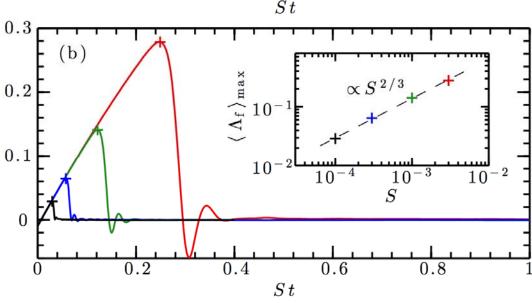


$$\frac{\langle |\delta \mathbf{B}_{\perp}|^2 \rangle}{B_0^2} \propto \left(\frac{S}{\Omega_i}\right)^{1/2} \ll 1$$

small-amplitude Larmor-scale firehose turbulence



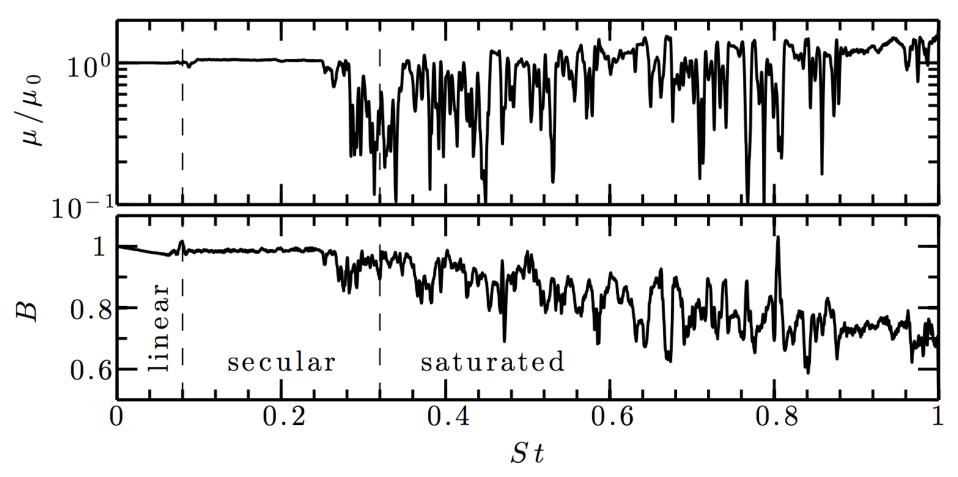




Kunz, AAS & Stone, PRL 112, 205003 (2014)

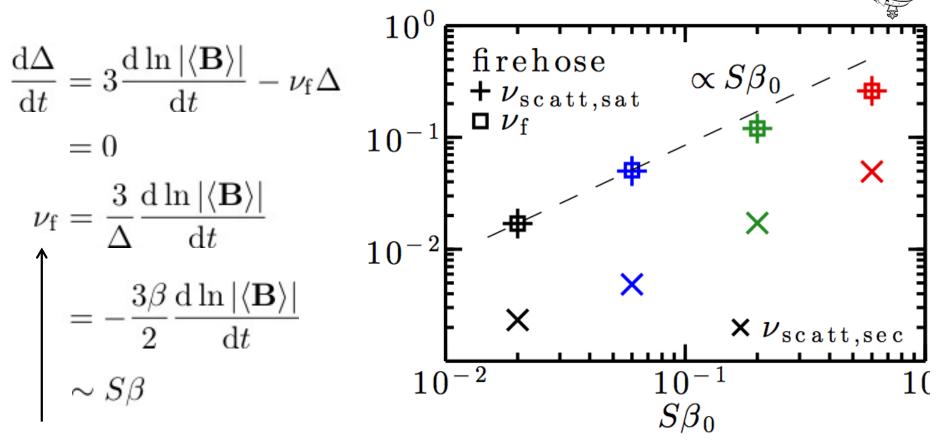
Saturated Firehose Scatters Particles





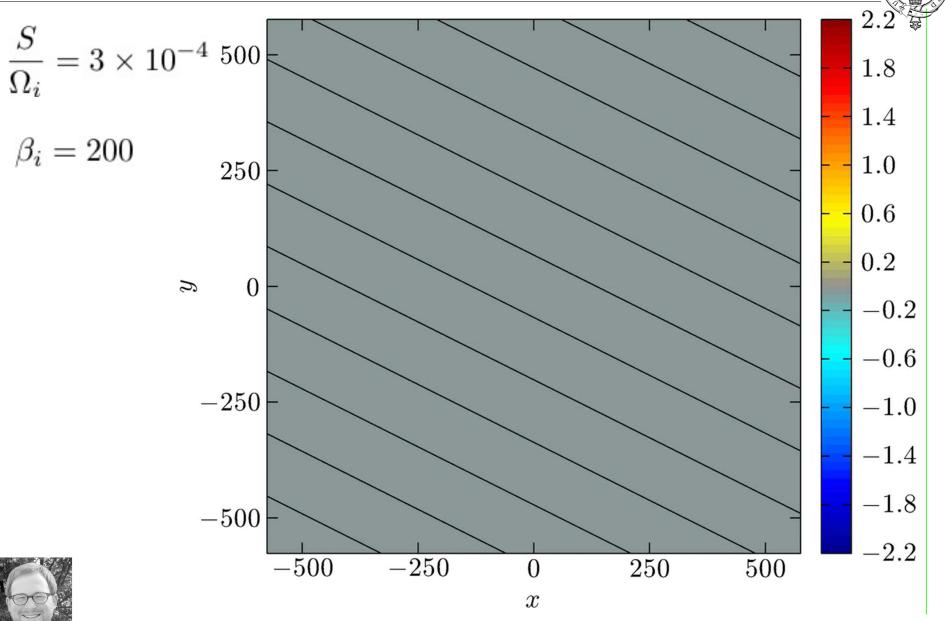
μconservation is broken at long times, firehose fluctuations scatter particles to maintain pressure anisotropy at marginal level

Saturated Firehose Scatters Particles



- effective collisionality required to maintain marginal stability
- + measured scattering rate during the saturated phase
- measured scattering rate during the secular phase

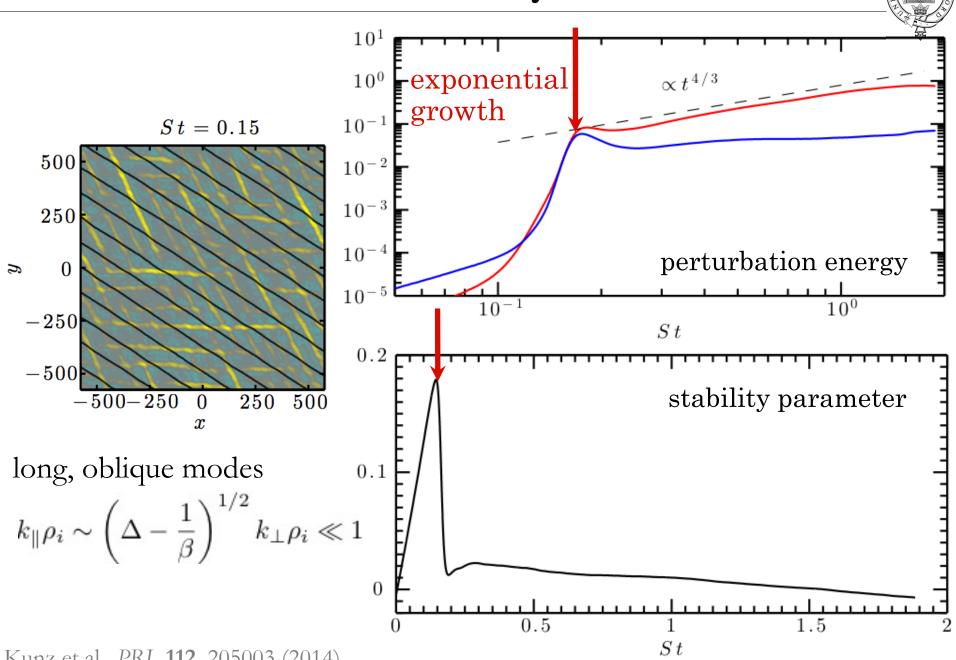
Mirror Instability (M. Kunz)



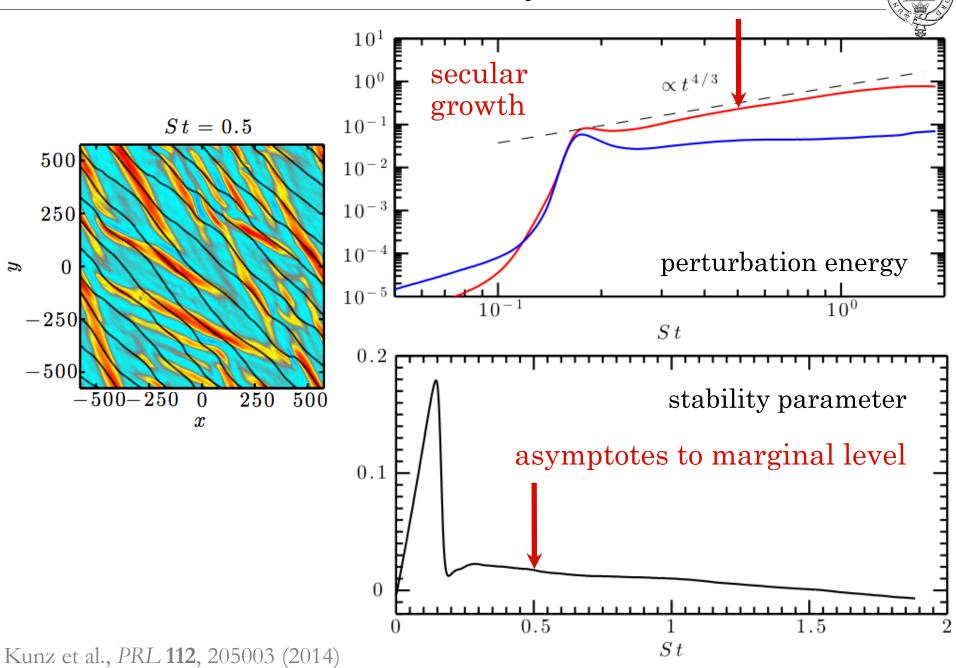


Kunz, AAS & Stone, PRL 112, 205003 (2014)

Mirror Instability: Linear



Kunz et al., PRL 112, 205003 (2014)

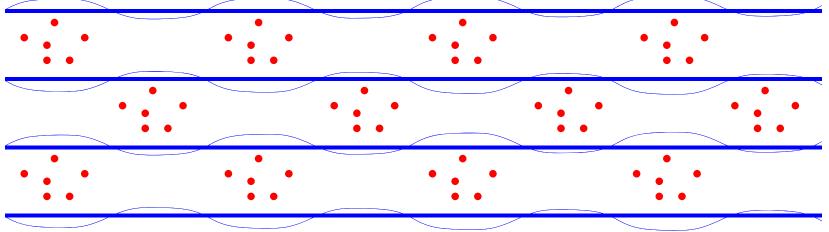




$$\overline{B} = B_0 + \overline{\delta B_{||}}$$

$$\Delta = 3 \int^t \! \mathrm{d}t' \, \overline{\frac{\mathrm{d} \ln B}{\mathrm{d}t}} = 3 \int^t \! \mathrm{d}t' \left(\frac{\mathrm{d} \ln B_0}{\mathrm{d}t} + \frac{\mathrm{d}}{\mathrm{d}t} \, \overline{\frac{\delta B_\parallel}{B_0}} \right) \to \frac{1}{\beta}$$
 pressure pressure marginal anisotropy anisotropy stability driven by shear from mirror-trapped particles in holes

(fraction $\sim |\delta B_{\parallel}/B_0|^{1/2}$)



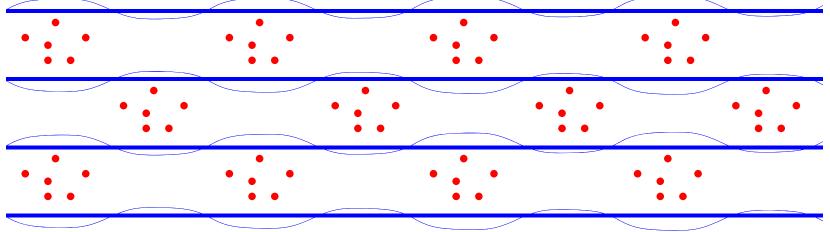


$$\overline{B} = B_0 + \overline{\delta B_{||}}$$

$$\Delta = 3 \int^t \! \mathrm{d}t' \, \overline{\frac{\mathrm{d} \ln B}{\mathrm{d}t}} \sim 3 \int^t \! \mathrm{d}t' \, \left(\frac{\mathrm{d} \ln B_0}{\mathrm{d}t} - \frac{\mathrm{d}}{\mathrm{d}t} \overline{\left| \frac{\delta B_\parallel}{B_0} \right|^{3/2}} \right) \to \frac{1}{\beta}$$
 pressure pressure anisotropy anisotropy stability driven by shear from

mirror-trapped particles in holes

(fraction $\sim |\delta B_{\parallel}/B_0|^{1/2}$)

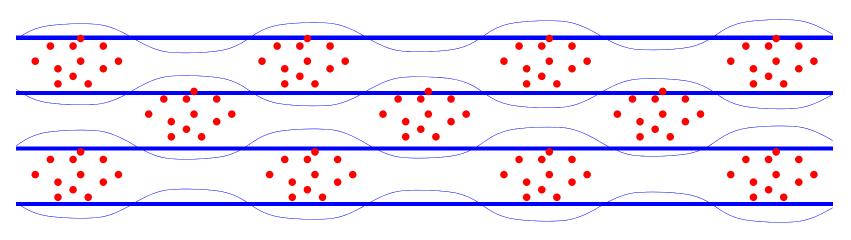




$$\overline{B} = B_0 + \overline{\delta B_{\parallel}}$$

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 pressure pressure anisotropy anisotropy stability driven by shear from

mirror-trapped particles in holes (fraction $\sim |\delta B_{\parallel}/B_0|^{1/2}$)

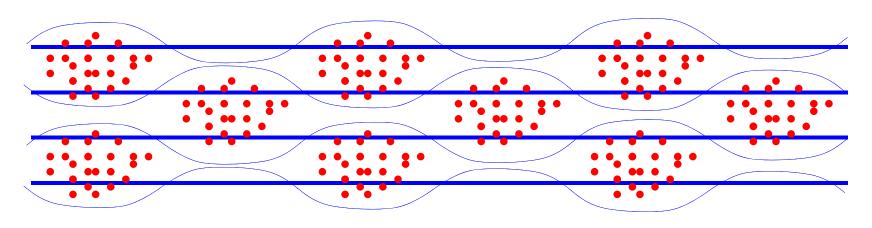




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 pressure anisotropy anisotropy stability driven by shear from mirror-trapped

particles in holes (fraction $\sim |\delta B_{\parallel}/B_0|^{1/2}$)



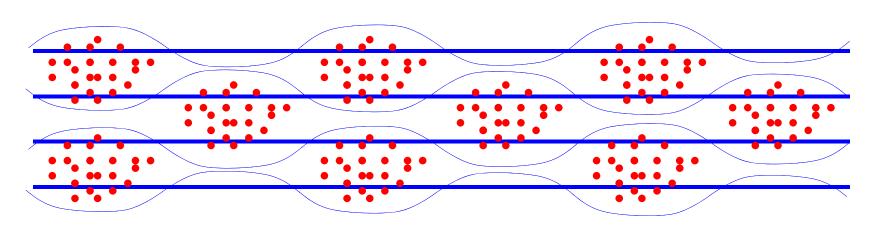


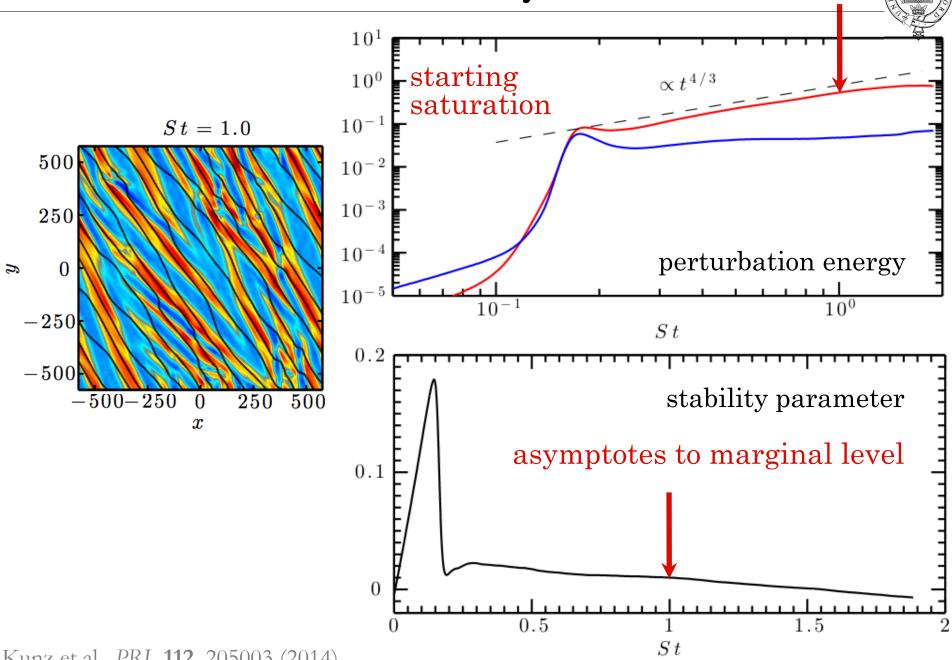
$$\overline{B} = B_0 + \overline{\delta B_{\parallel}}$$

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$$\frac{\left|\frac{\delta B_{\parallel}}{B_{0}}\right|^{3/2}}{\left|B_{0}\right|^{3/2}} = S \int^{t} dt' \, \hat{b}_{x}(t') \hat{b}_{y}(t') - \frac{1}{\beta} \quad \Rightarrow \quad \frac{\delta B_{\parallel}^{2}}{B_{0}^{2}} \sim (St)^{4/3}$$

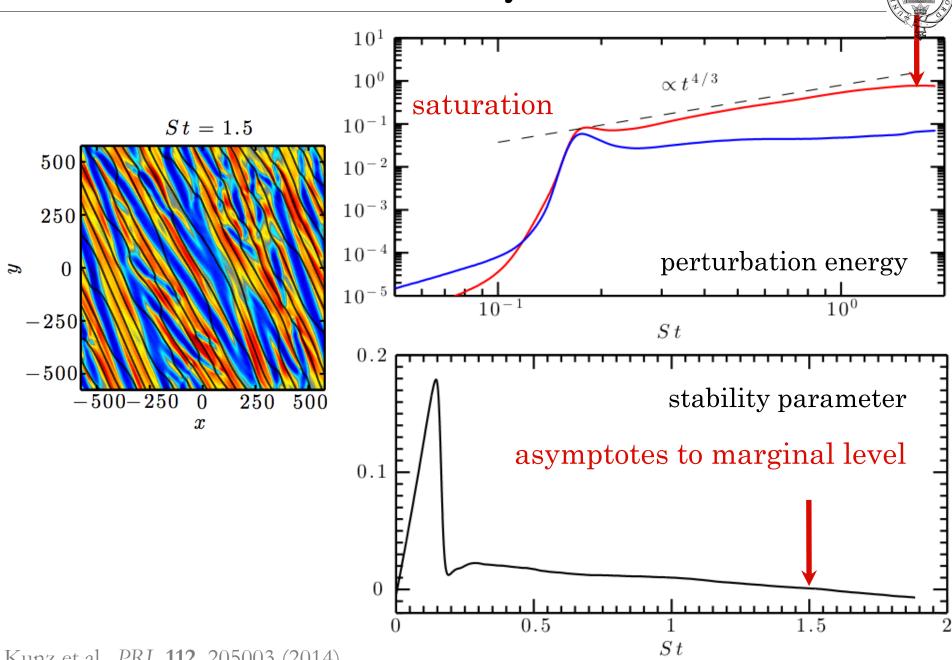
secular growth





Kunz et al., PRL 112, 205003 (2014)

Mirror Instability: Saturated



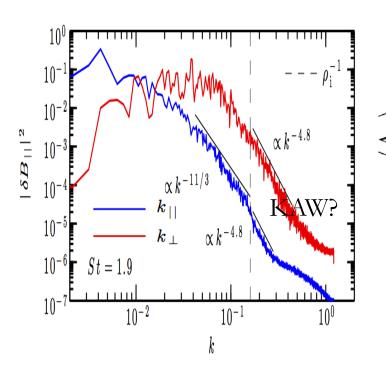
Kunz et al., PRL 112, 205003 (2014)

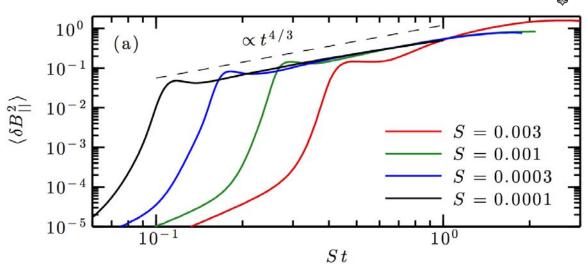
Mirror Saturates at Order-Unity Amplitudes

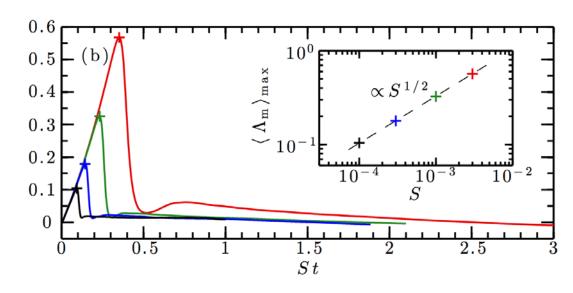


$$\frac{\langle \delta \mathbf{B}_{\parallel}^2 \rangle}{B_0^2} \sim 1$$

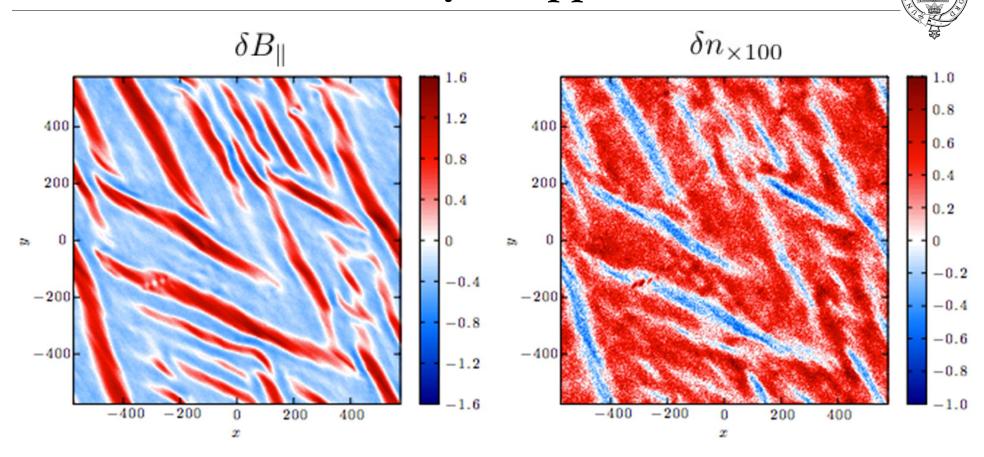
order-unity-amplitude (independent of *S*) long-parallel-scale mirror turbulence







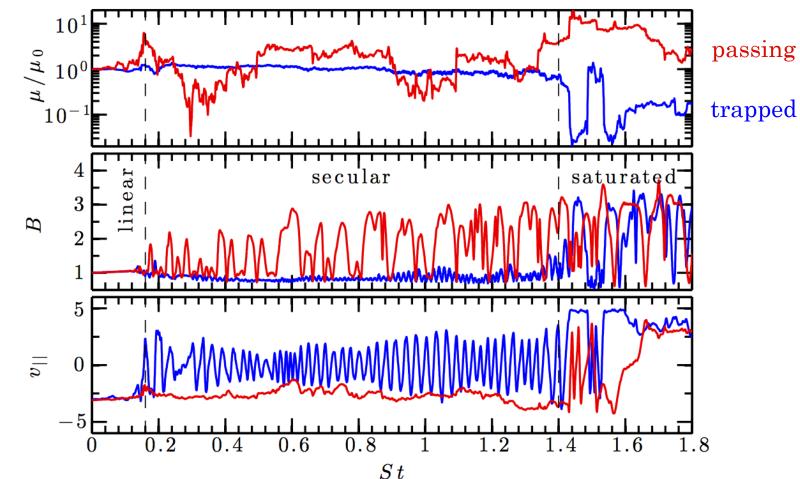
Mirror Instability: Trapped Particles



pressure anisotropy is regulated by trapped particles in magnetic mirrors, where field strength stays constant on average...

Secular Mirror Doesn't Scatter Particles



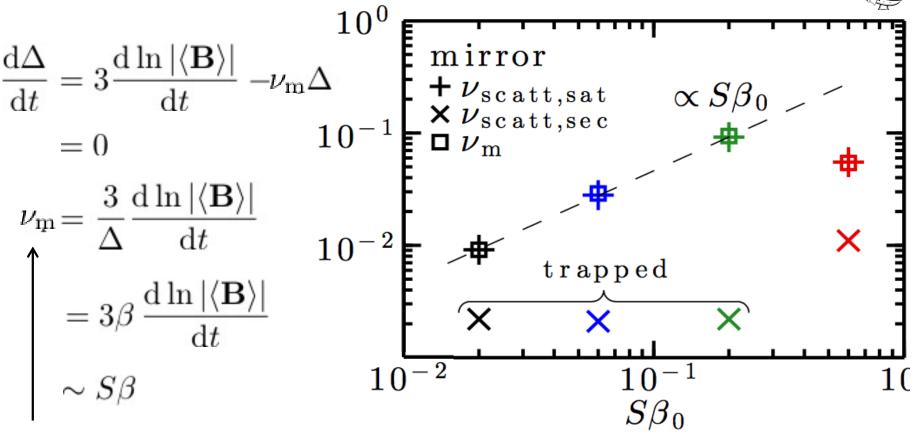


pressure anisotropy is regulated by trapped particles in magnetic mirrors, where field strength stays constant on average...

no particle scattering until (late) saturation (then scattering off mirror edges)

Secular Mirror Doesn't Scatter Particles





- effective collisionality required to maintain marginal stability
- + measured scattering rate during the saturated phase
- measured scattering rate during the secular phase

Effective Closure Options



Option I: Suppress stretching

$$\Delta \equiv \frac{p_{\perp} - p_{\parallel}}{p} \sim \frac{1}{\nu} \frac{1}{B} \frac{\mathrm{d}B}{\mathrm{d}t} = \frac{\gamma}{\nu} \in \left[-\frac{2}{\beta}, \frac{1}{\beta} \right]$$

Melville, AAS & Kunz arXiv:1512.08131

Option II: Enhance collisionality

This in fact also happens for firehoses, at ultra-high beta $\beta > \Omega/S$

This happens for firehoses (also mirrors in saturation & decaying)

Effective Closure Options



Option III: Skew the average towards regions of weaker field by trapping particles

This happens for secularly growing mirrors

Option I: Suppress stretching

$$\Delta \equiv \frac{p_{\perp} - p_{\parallel}}{p} \sim \frac{1}{\nu} \frac{1}{B} \frac{\mathrm{d}B}{\mathrm{d}t} = \frac{\gamma}{\nu} \in \left[-\frac{2}{\beta}, \frac{1}{\beta} \right]$$

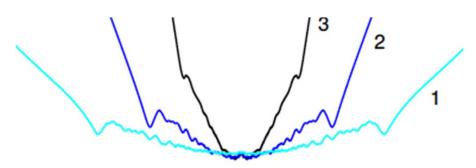
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Option II: Enhance collisionality

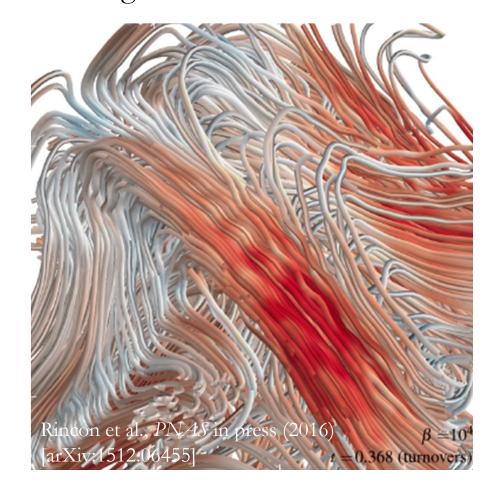
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This happens for firehoses (also mirrors in saturation & decaying)

In firehose regions, anomalous scattering will marginalise anisotropy



➤ It appears that in the stretching regions, B can grow, at the price of "mirror-bubble" infestation (as long as the stretching does not last longer than ~ turnover time



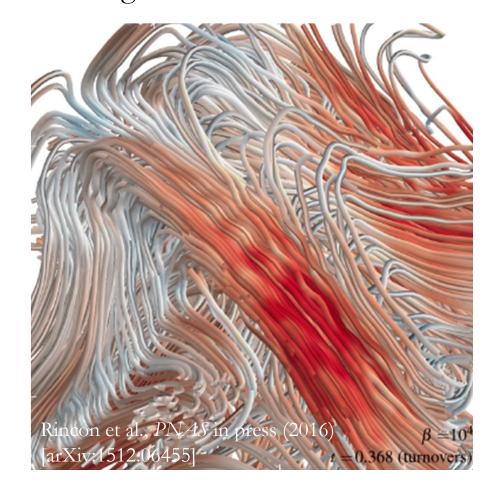
In firehose regions, anomalous scattering will marginalise anisotropy

Eff. collisionality:
$$\nu_{\rm eff} \sim S\beta$$

to keep anisotropy marginal:

$$\Delta \sim \frac{S}{\nu_{\rm eff}} \sim \beta^{-1}$$

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In firehose regions, anomalous scattering will marginalise anisotropy

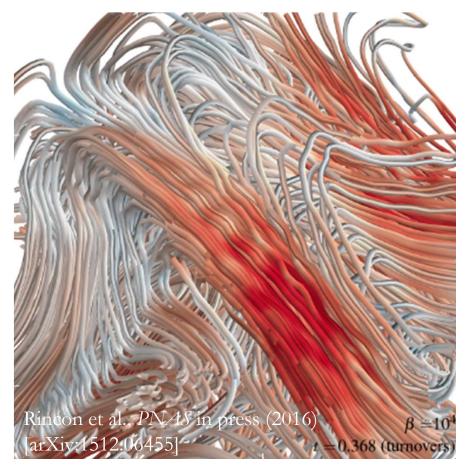
Eff. collisionality:
$$\nu_{\rm eff} \sim S\beta$$

$$n = B^2/8$$

Eff. viscosity:
$$\mu_{ ext{eff}} \sim \frac{p}{
u_{ ext{eff}}} \sim \frac{B^2/8\pi}{S}$$

NB: regions of weaker field are less viscous!

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In firehose regions, anomalous scattering will marginalise anisotropy

Eff. collisionality:
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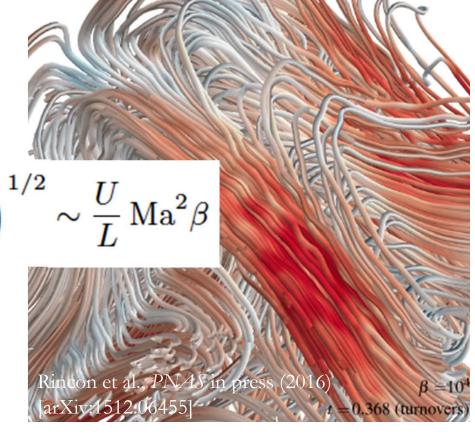
Eff. viscosity:
$$\mu_{\rm eff} \sim \frac{p}{\nu_{\rm eff}} \sim \frac{B^2/8\pi}{S}$$

Energy flux (Kolmogorov):
$$\varepsilon \sim \frac{\rho U^3}{L}$$

Fastest turnover rate:

$$S \sim \left(\frac{\varepsilon}{\mu_{\text{eff}}}\right)^{1/2} \sim \text{Ma}\left(\frac{U}{L}\nu_{\text{eff}}\right)^{1/2} \sim \frac{U}{L} \,\text{Ma}^2 \beta$$

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In firehose regions, anomalous scattering will marginalise anisotropy

Eff. collisionality: $\nu_{ ext{eff}} \sim S eta$

Eff. viscosity: $\mu_{\mathrm{eff}} \sim \frac{p}{\nu_{\mathrm{eff}}} \sim \frac{B^2/8\pi}{S}$

Energy flux (Kolmogorov): $\varepsilon \sim \frac{\rho U^3}{L}$

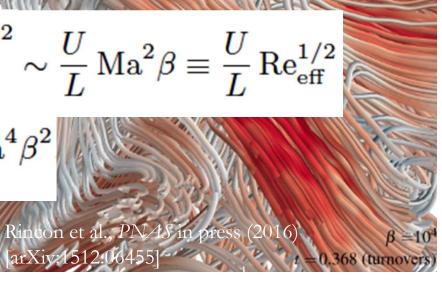
Fastest turnover rate:

$$S \sim \left(\frac{\varepsilon}{\mu_{\rm eff}}\right)^{1/2} \sim {\rm Ma} \left(\frac{U}{L} \nu_{\rm eff}\right)^{1/2} \sim \frac{U}{L} \, {\rm Ma}^2 \beta \equiv \frac{U}{L} \, {\rm Re}_{\rm eff}^{1/2}$$

Effective Reynolds number: $Re_{eff} = Ma^4 \beta^2$

Regions of decreasing field will quickly break up?

➤ It appears that in the stretching regions, *B* can grow, at the price of "mirror-bubble" infestation (as long as the stretching does not last longer than ~ turnover time



> In firehose regions, anomalous scattering will marginalise anisotropy

Eff. collisionality:
$$\nu_{ ext{eff}} \sim S eta$$

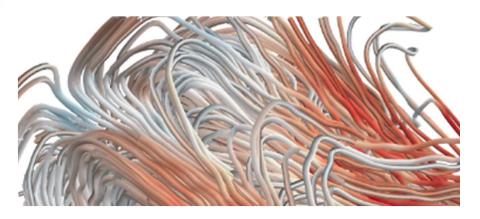
Eff. viscosity:
$$\mu_{\rm eff} \sim \frac{p}{\nu_{\rm eff}} \sim \frac{B^2/8\pi}{S}$$

Energy flux (Kolmogorov):
$$\varepsilon \sim \frac{\rho U^3}{L}$$

Fastest turnover rate:

$$S \sim \left(\frac{\varepsilon}{\mu_{\rm eff}}\right)^{1/2} \sim \frac{\varepsilon}{B^2/8\pi}$$
 NB: faster if the field is weaker

> It appears that in the stretching regions, B can grow, at the price of "mirror-bubble" infestation (as long as the stretching does not last longer than ~ turnover time



So magnetic energy grows in one turnover time from any level:

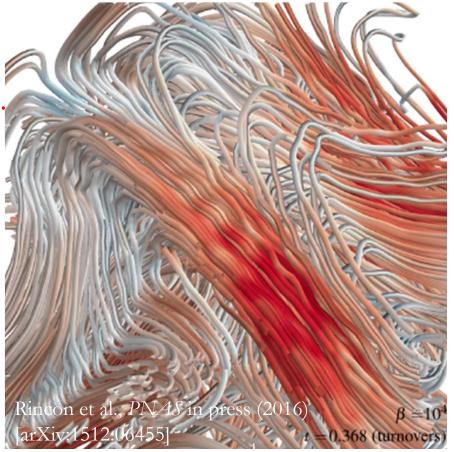
$$\frac{\mathrm{d}}{\mathrm{d}t} \frac{B^2}{8\pi} \sim S \frac{B^2}{8\pi} \sim \varepsilon$$
 (but only if this enhanced collisionality persists)

Mogavero & AAS, MNRAS 440, 3226 (2014)

- In firehose regions, anomalous scattering will marginalise anisotropy
- Regions of decreasing field will quickly break up?

Thus, it is quite difficult to decrease B in a weakly collisional plasma, while growth is OK (and maybe even faster!) Good news for fast plasma dynamo!

➤ It appears that in the stretching regions, B can grow, at the price of "mirror-bubble" infestation (as long as the stretching does not last longer than ~ turnover time



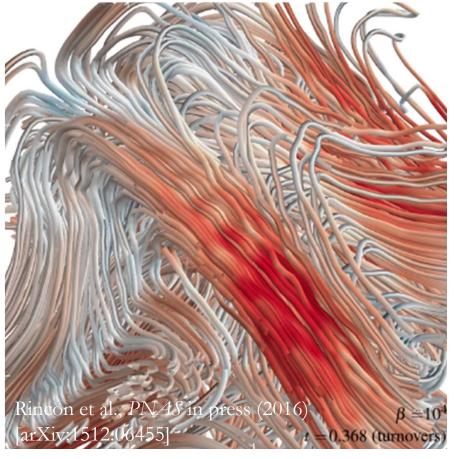
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These are speculations.
Upcoming historic events:

- ❖ Plasma dynamo simulations (F. Rincon, M. Kunz ...)
- ♦ NIF dynamo experiment (G. Gregori, in ~6 months)

➤ It appears that in the stretching regions, B can grow, at the price of "mirror-bubble" infestation (as long as the stretching does not last longer than ~ turnover time



- In firehose regions, anomalous scattering will marginalise anisotropy
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These are speculations. Upcoming historic events:

➤ It appears that in the stretching regions, *B* can grow, at the price of "mirror-bubble" infestation (as long as the stretching does not last longer than ~ turnover time



At any rate, high-beta, weakly collisional

plasma dynamics are interesting and still

to be understood.

- ❖ Plasma dynamo simulations (F. Rincon, M. Kunz et al...)
- **♦ NIF dynamo experiment**

(G. Gregori et al, in \sim 6 months) For astrophysics, paradigm change in the air?

- > In firehose regions, anomalous scattering will marginalise anisotropy
- Regions of decreasing field will quickly break up?

Thus, it is quite difficult to decrease B in a weakly collisional plasma, while growth is OK (and maybe even faster). Good news for fast plasma dynamo!

These are speculations. **Upcoming historic events:**

(as long as the stretching does not last longer than ~ turnover time

> It appears that in the stretching

"mirror-bubble" infestation

regions, B can grow, at the price of







2016: the year of plasma dynamo?

- **♦ Plasma dynamo simulations** (F. Rincon, M. Kunz et al...)
- **♦ NIF dynamo experiment**

At any rate, high-beta, weakly collisional plasma dynamics are interesting and still to be understood.

(G. Gregori et al, in ~6 months) For astrophysics, paradigm change in the air?

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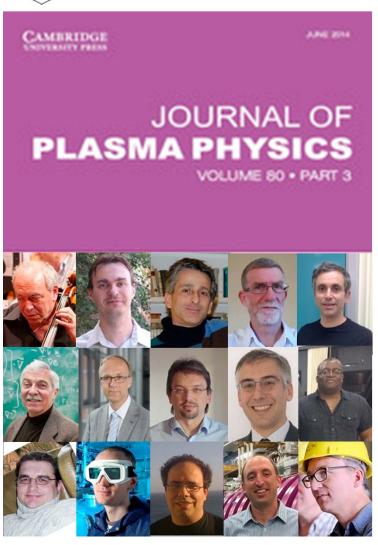
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A 19th Century Programme...

- What is the **viscosity** of a high-beta plasma?
- What is the **thermal conductivity** of a high-beta plasma?



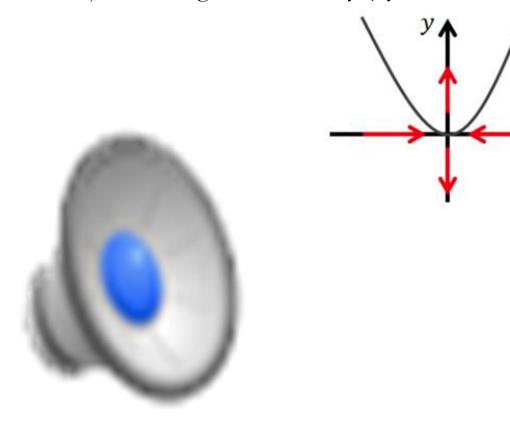
When dining, I had often observed that some particular dishes retained their Heat much longer than others; and that apple-pies, and apples and almonds mixed, - (a dish in great repute in England) - remained hot a surprising length of time. Much struck with this extraordinary quality of retaining Heat, which apples appear to possess, it frequently recurred to my recollection; and I never burnt my mouth with them, or saw others meet with the same misfortune, without endeavouring, but in vain, to find out some way of accounting, in a satisfactory manner, for this surprising matter.

Count Rumford, 1799

WE DON'T REALLY KNOW (YET) HOW MAGNETISED, HIGHβI

Effects of Magnetic Field

Initially parabolic magnetic field line subject to Braginskii viscosity (by Scott Melville)

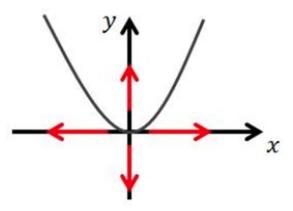


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