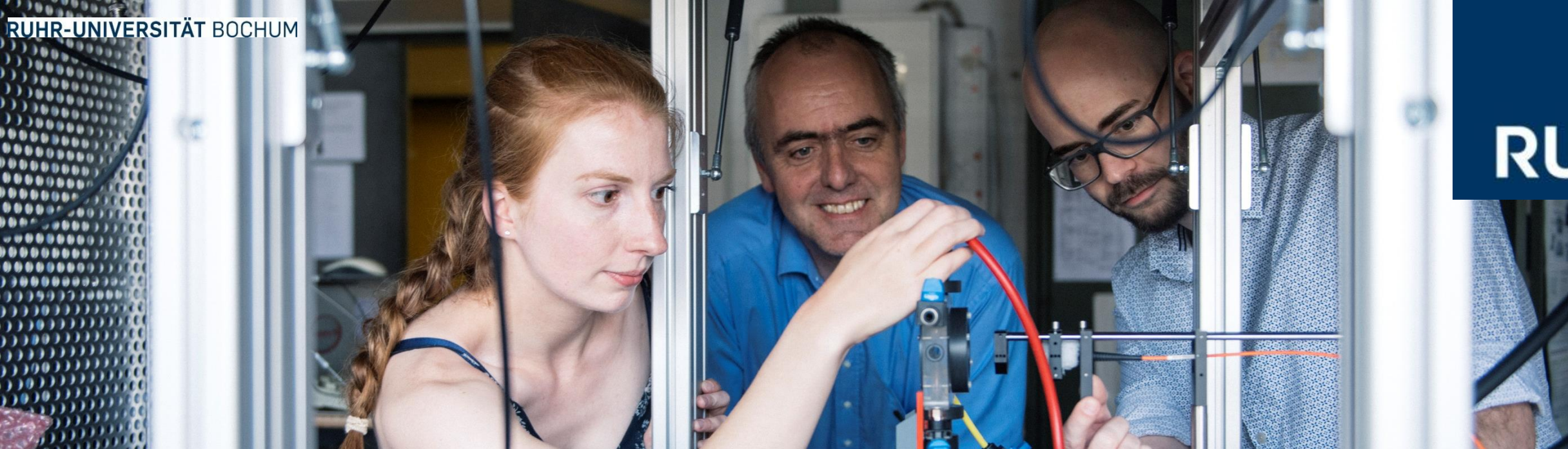




Nanosecond Plasmas in Liquids – Dynamic Plasmas at GPa pressures

A. von Keudell, K. Grosse, J. Held, V. Schulz-von der Gathen, M. Kai,
C. Nenbangkao, F. Seferoglu, L. Chauvet

Experimental Physics II, Ruhr University Bochum



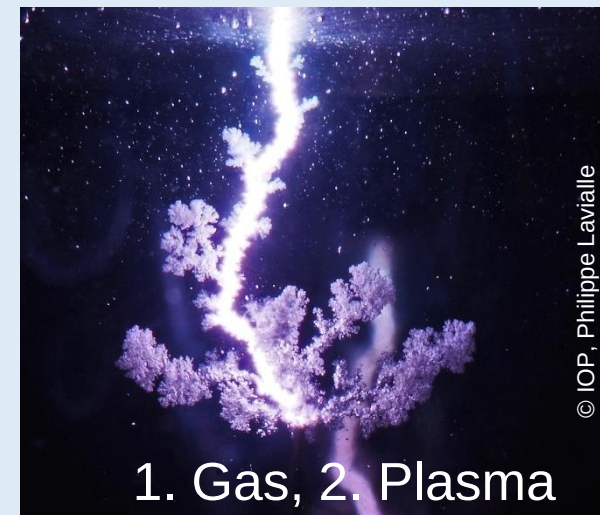
Nanosecond plasmas



- Short nanosecond pulses
- Pulses too short for formation of a gas bubble
- Plasma ignition inside the liquid

Extremely high pressures and temperatures
10000 bar, 50000 K

Microsecond plasmas

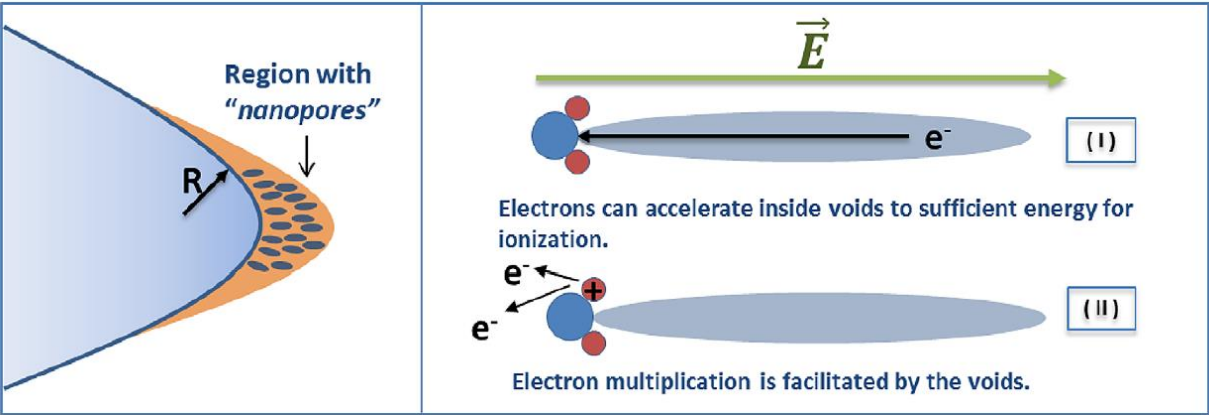


- Long microsecond pulses
- Initial formation of a gas bubble due to Ohmic heating or E-field rupture
- Plasma ignition inside the water vapor in the bubble

Moderate high pressures and temperatures
10 bar, 20000 K

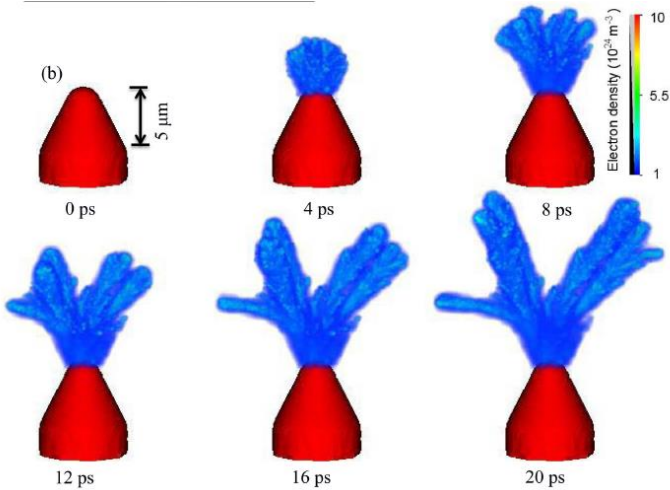
The big puzzle regarding the ignition in ns plasmas in liquids

e^- acceleration in nanopores

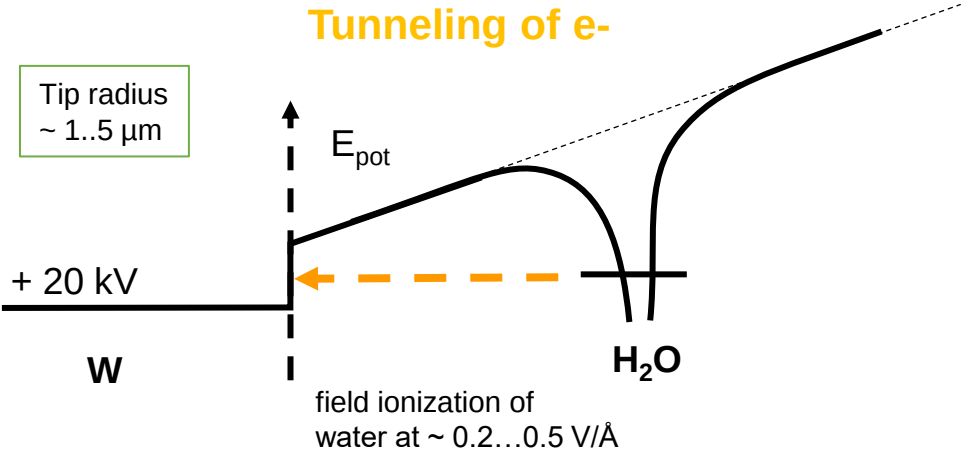


(Dobryn et al. JPD 46, 355201 (2013))

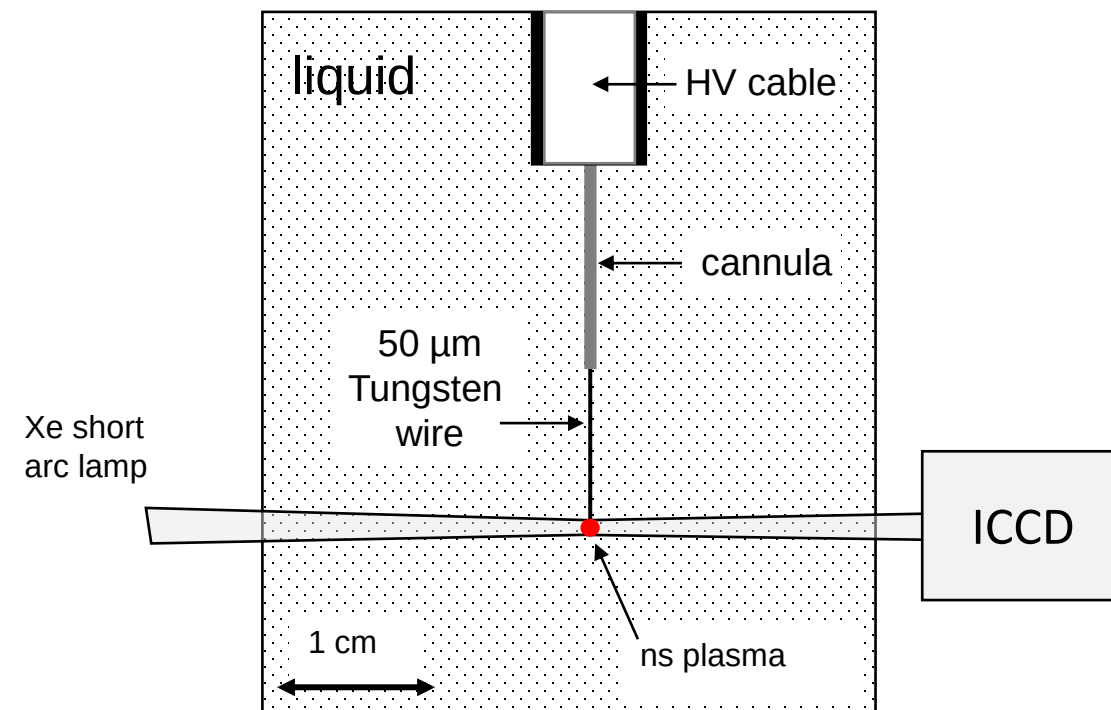
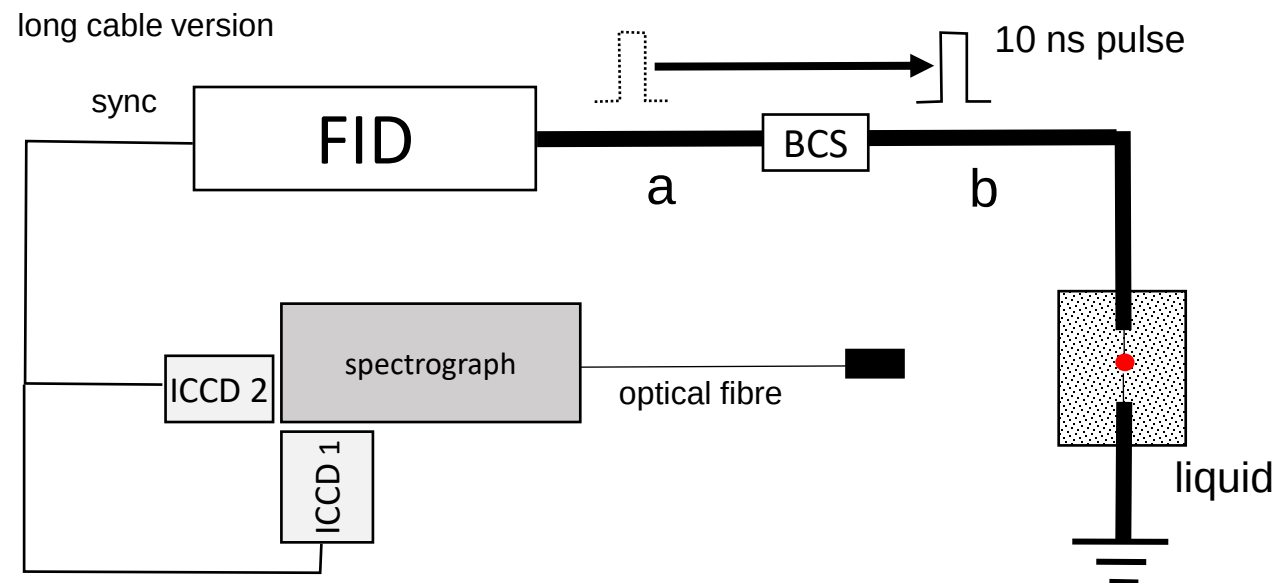
Field emission, field ionization



From A. Sun, J. Teunissen, U. Ebert
IEEE Trans. Plas. Sci. 42, 2416 (2014)



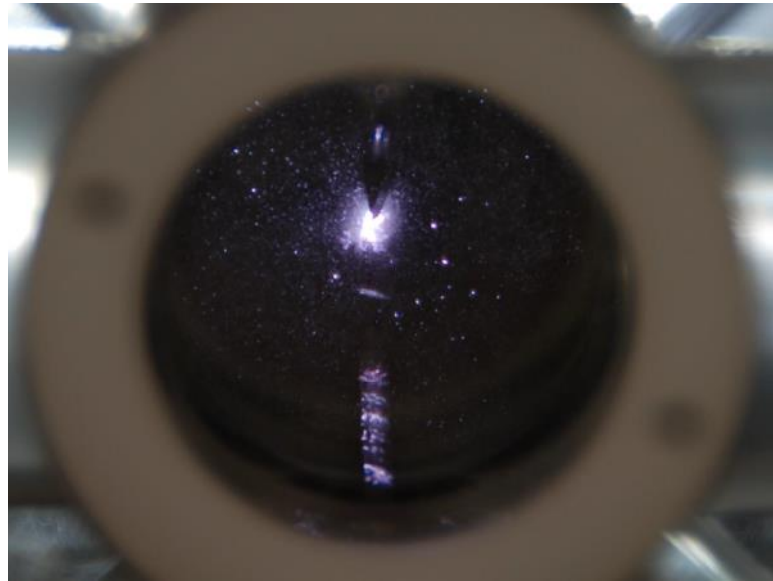
Plasma Chemistry in liquids – example H_2O_2 generation



- 10 ns pulses, 14...30 kV, distilled water
- Shadowgraphy 2 ns ... 70 ns gate widths
- Optical emission spectroscopy with 2ns and 30 ns gate time

Goals:

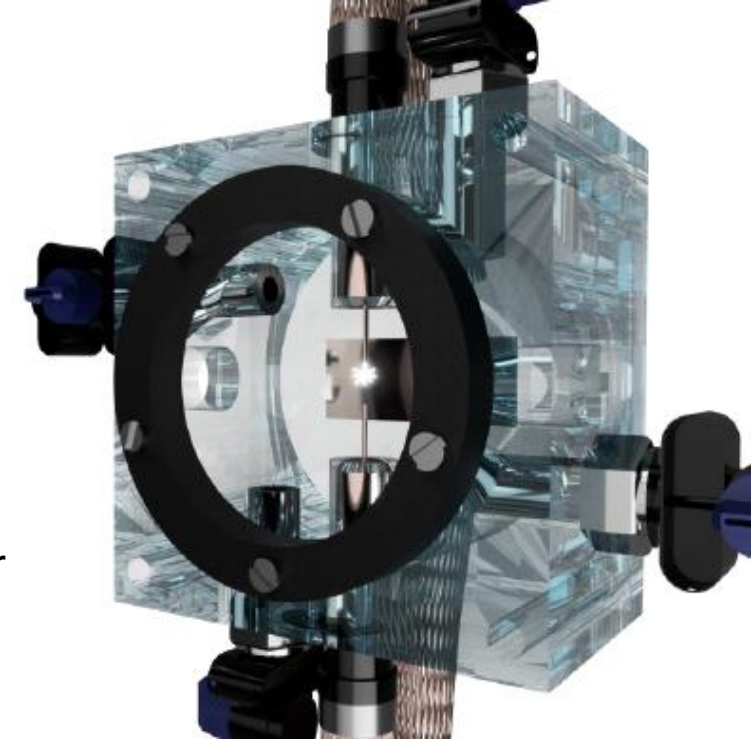
- reactive liquid production
- regeneration of catalysts for plasma enhanced electrolysis



Temporal evolution of the discharge

4 phases

- Ignition (Streamer)
- Pressure waves propagate
- Conversion of water into plasma and vapor
- Expansion of a cavitation bubble



Ignition
for 10 ns

Pressure waves.

Cavitation

Bubble Collapse

0.5 mm
↑
↓

6 ns

330 ns

30 μs

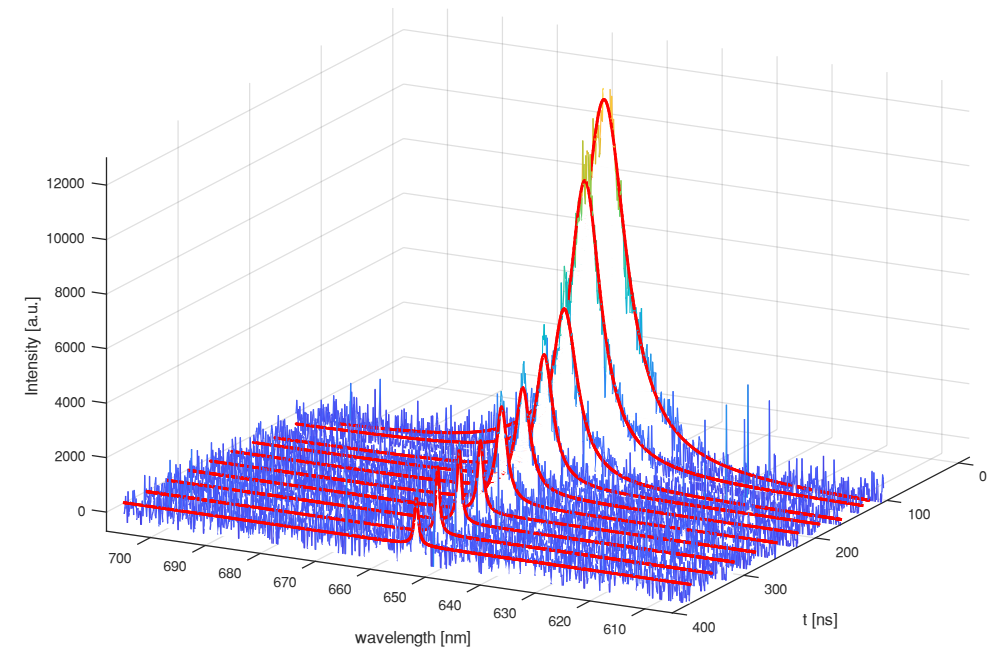
351 μs

Plasma Chemistry in liquids – example H_2O_2 generation

Temporal evolution of the discharge

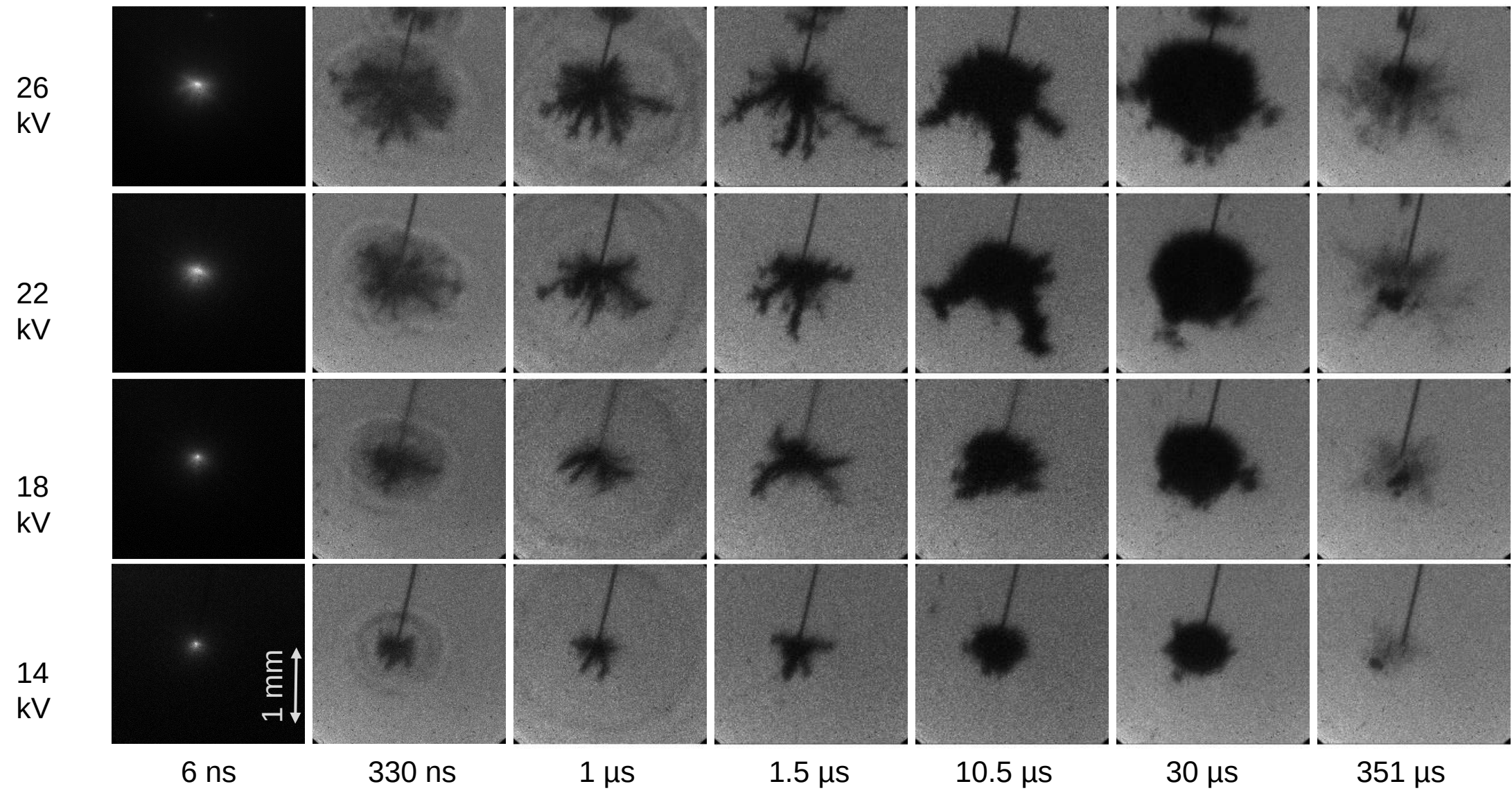


H alpha emission after the plasma pulse



60 ns gate, 30 ns steps

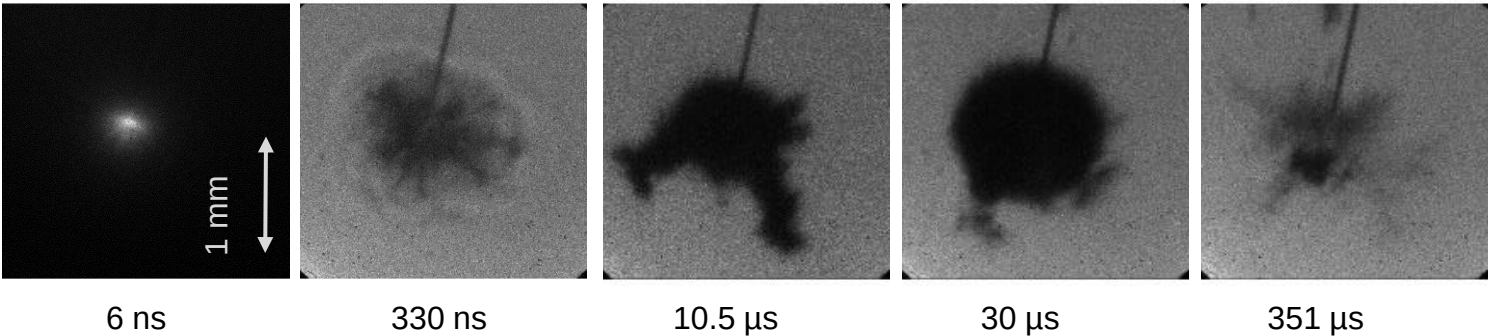
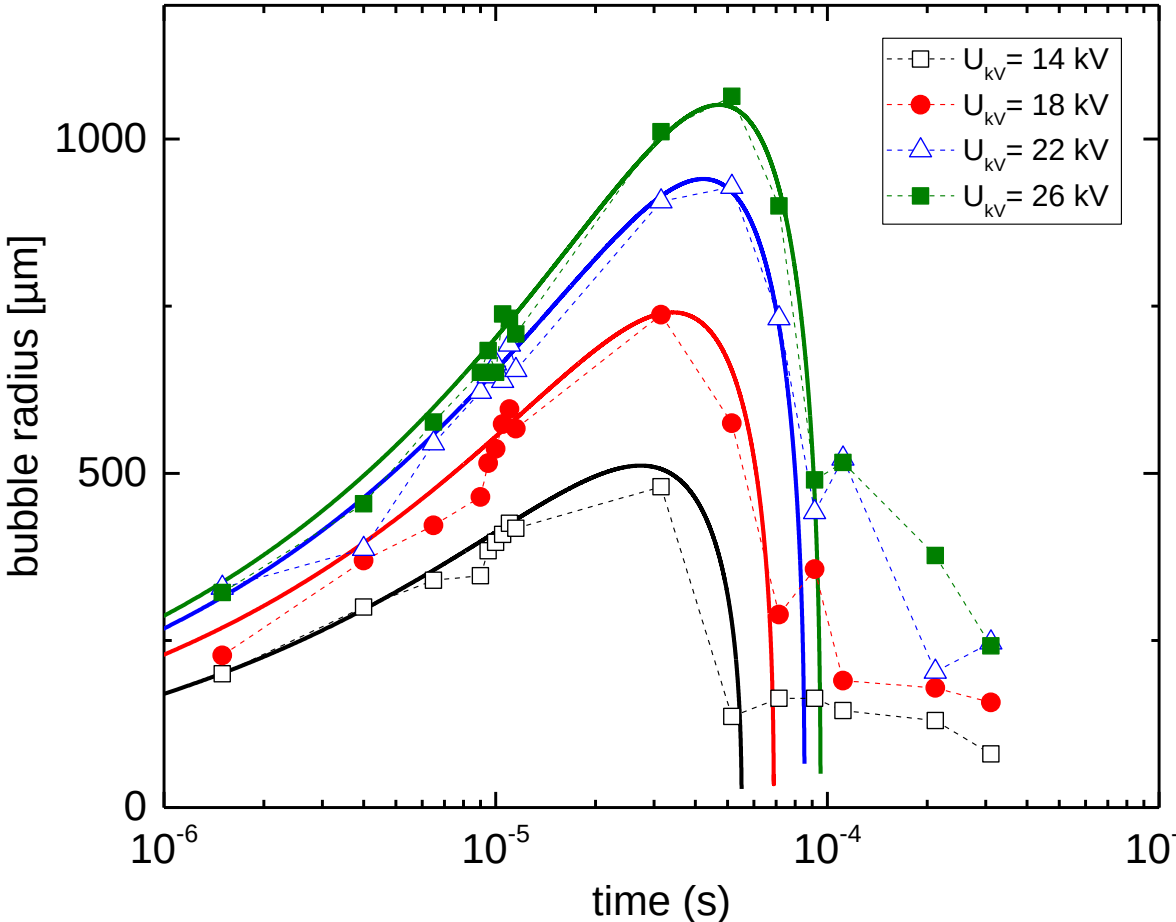
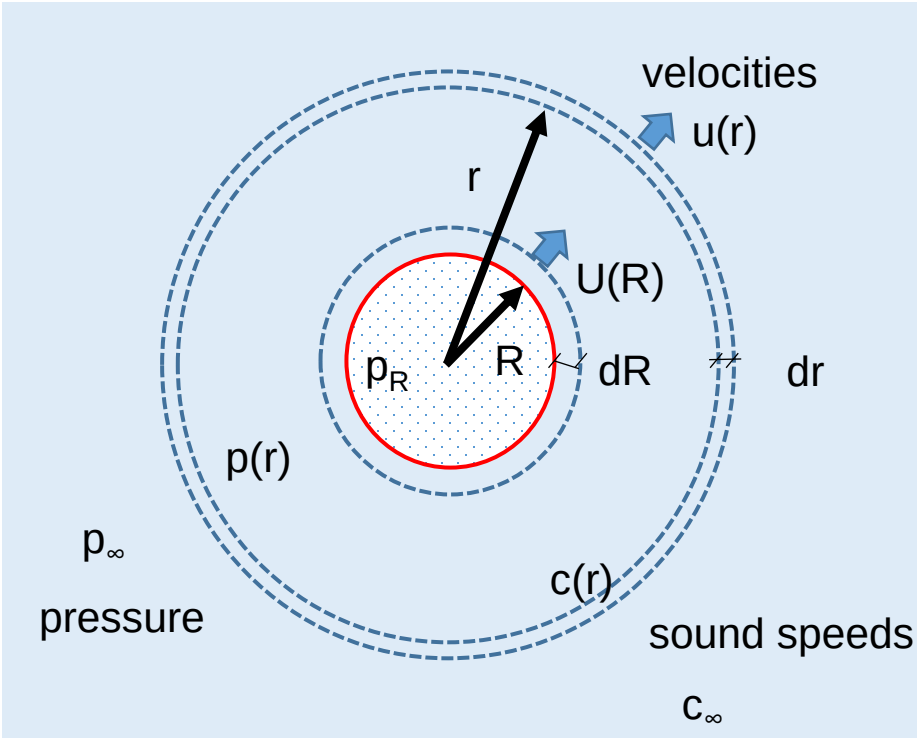
Monitoring Bubble Expansion with Shadowgraphy – monitoring sound waves and cavitation



Comparison of Bubble Expansion with cavitation theory

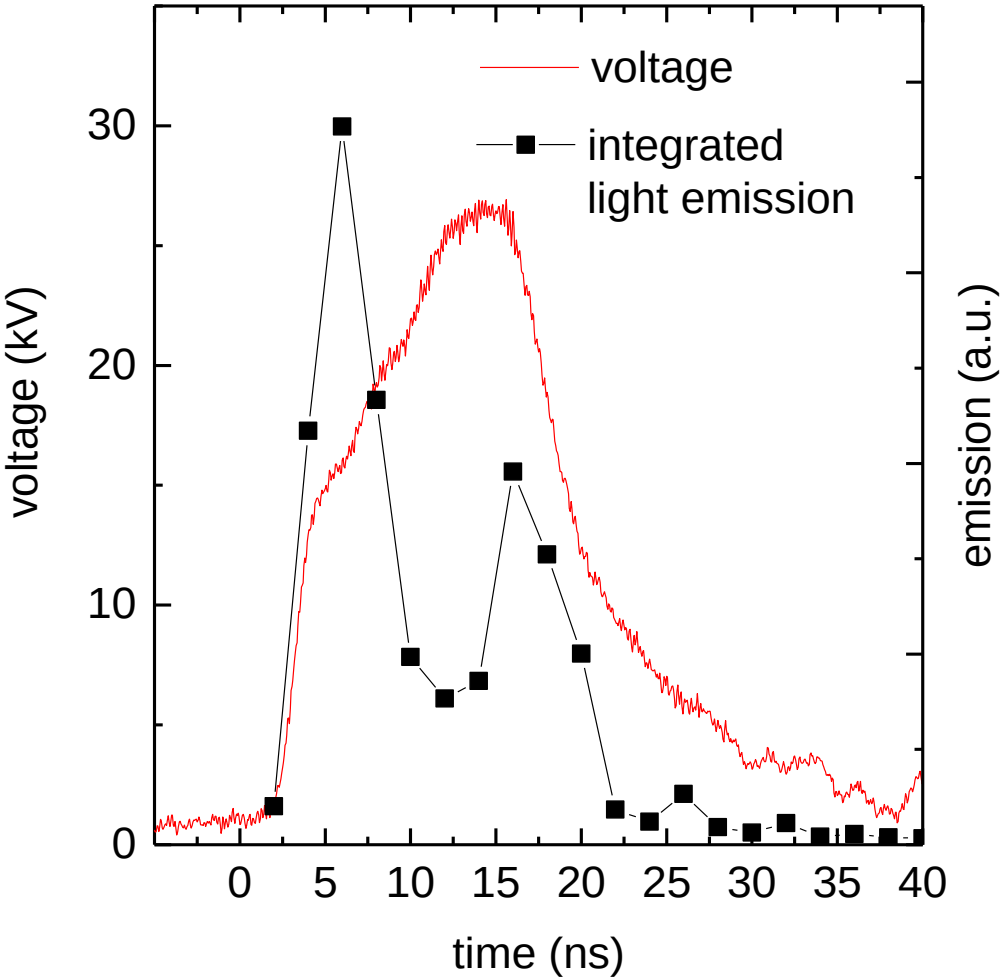
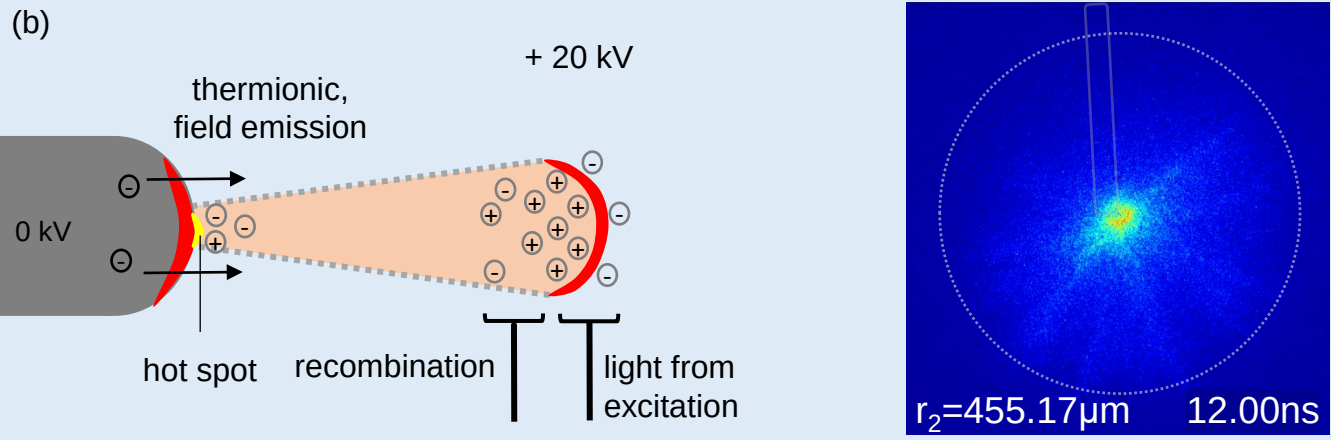
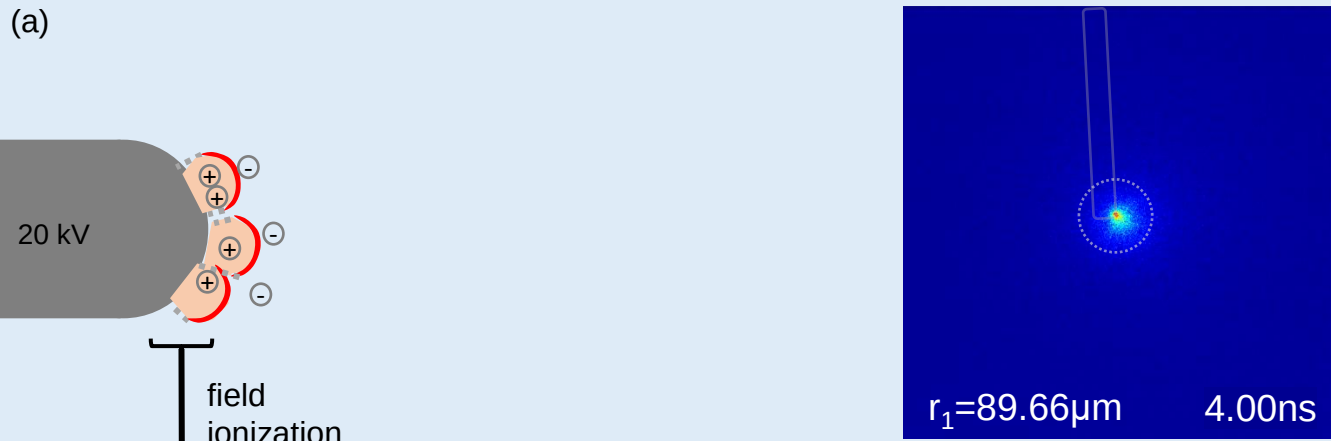
Rayleigh Plesset equation:

$$R\ddot{R}\left(1-\frac{\dot{R}}{c}\right)+\frac{3}{2}\dot{R}^2\left(1-\frac{\dot{R}}{3c}\right)=h\left(1+\frac{\dot{R}}{c}\right)+\left(1-\frac{\dot{R}}{c}\right)\frac{R}{c}\frac{\partial h}{\partial t}$$



How does the plasma Ignites ?

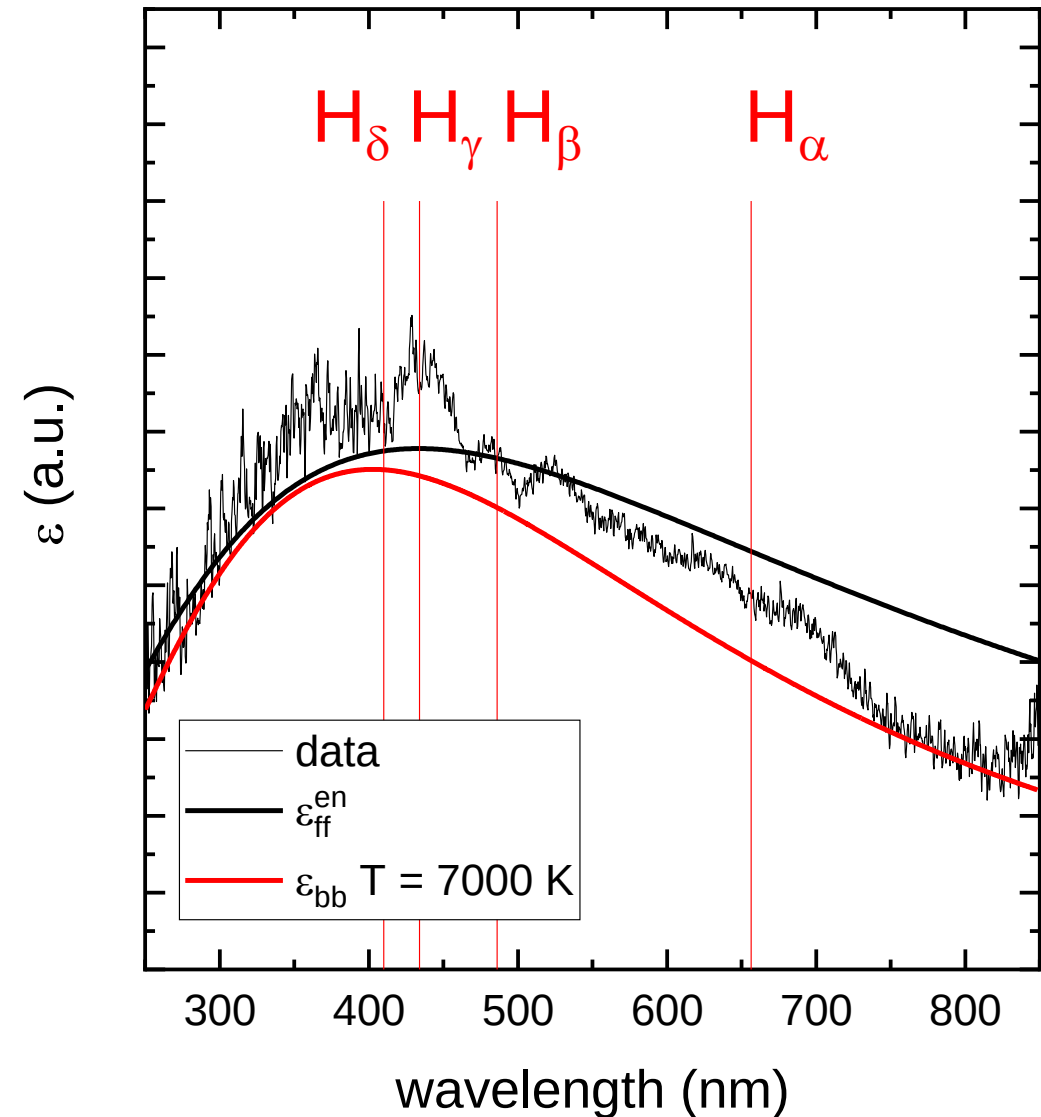
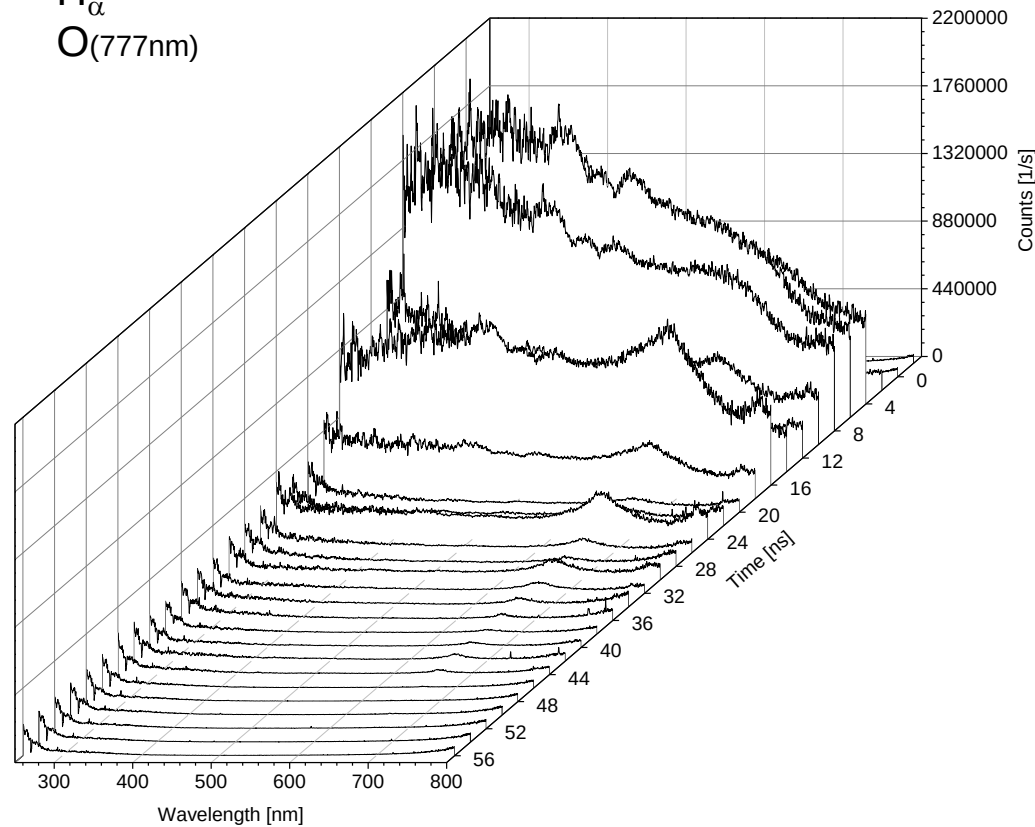
Experiment 22kV, 1Hz, distilled water, $t_{\text{gate}}=2\text{ns}$, $t_{\text{step}}=2\text{ns}$



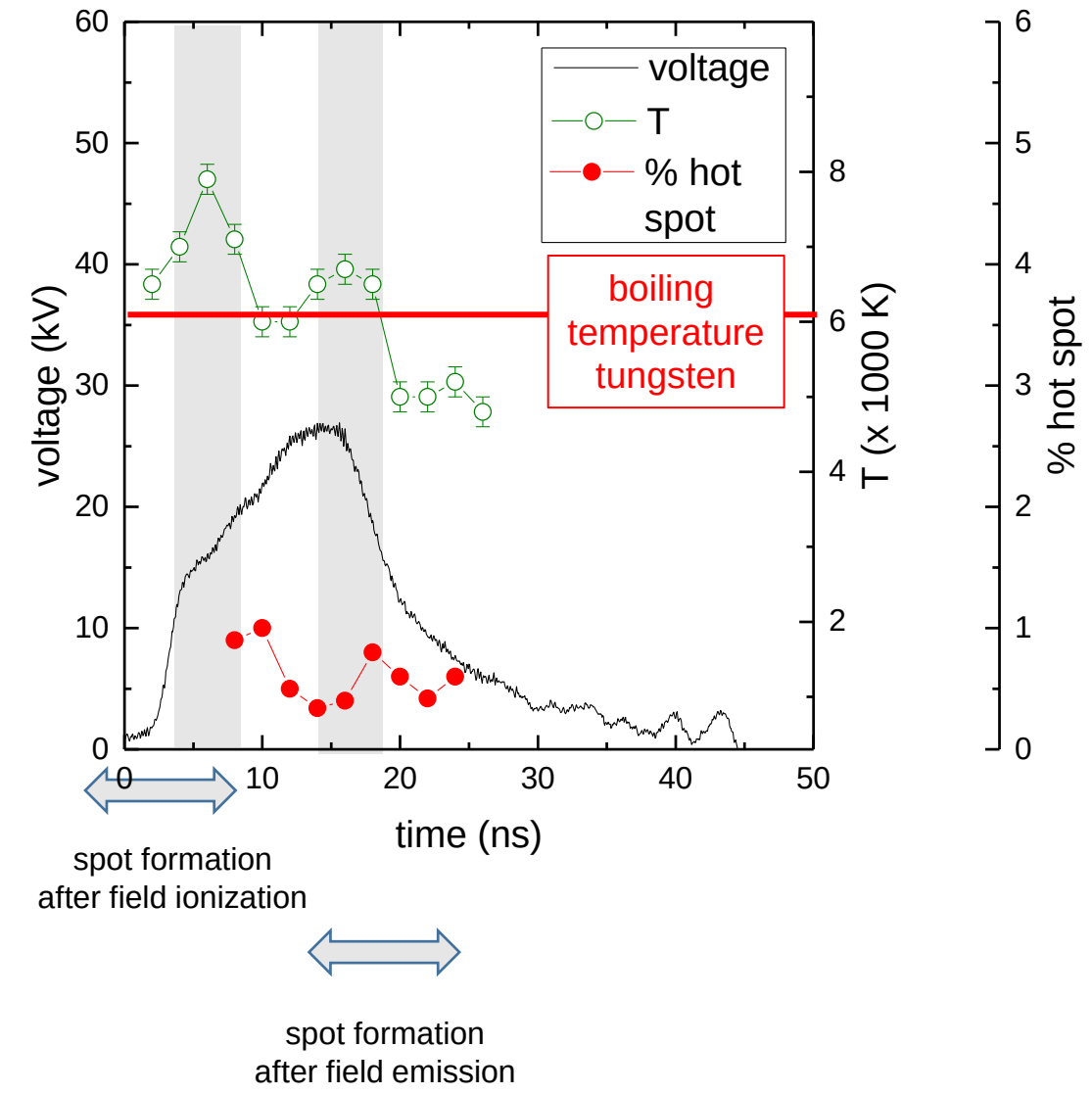
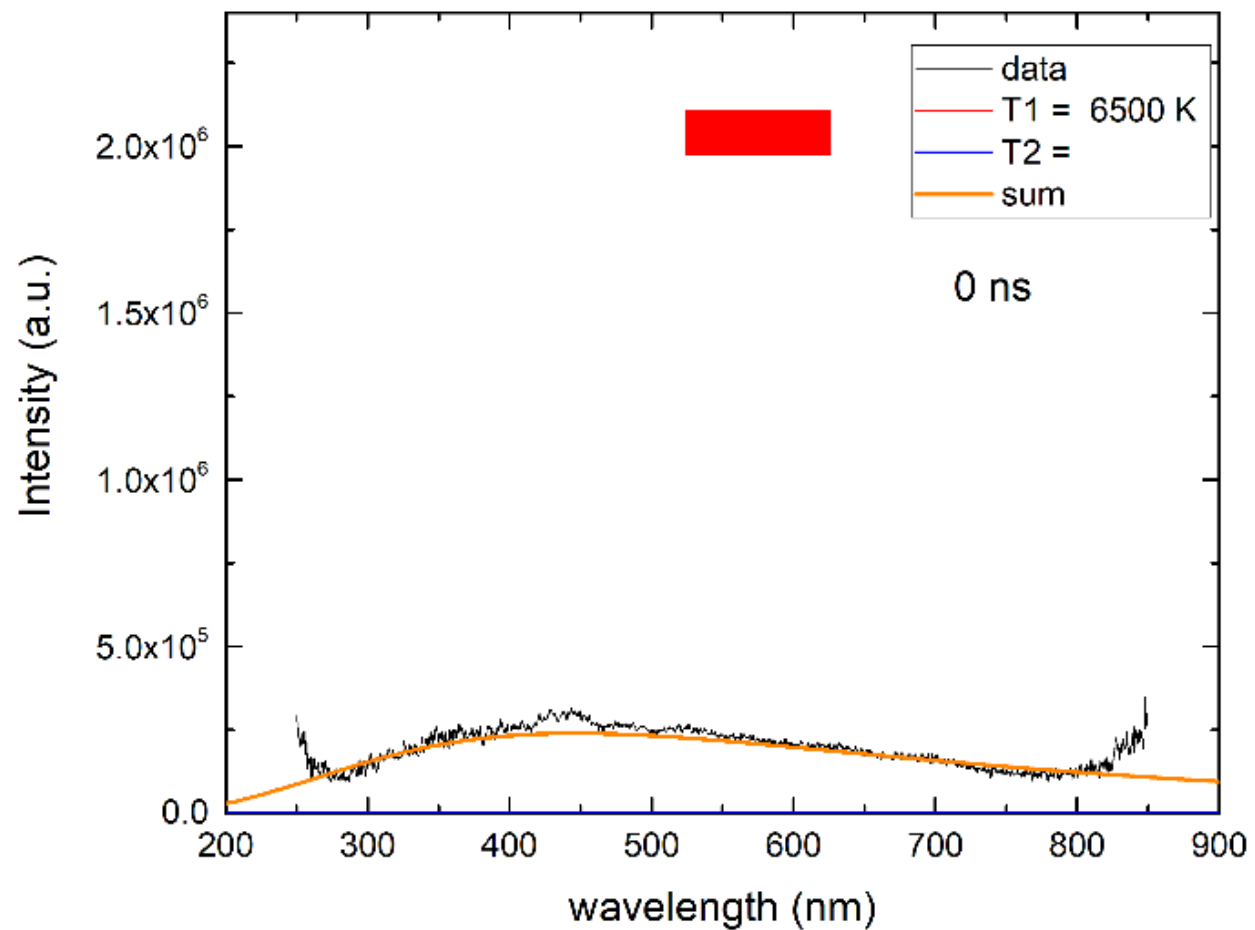
Temperatures from emission spectra of the plasma into the UV

Spectrum (first 50 ns, time resolution 2 ns)

- Recombination
- H_2 , H_2O recomb. continuum
- OH , OH^+ , H_2O , H_2O^+ bands
- Black body radiation (W)
- H_α
- $\text{O}(777\text{nm})$

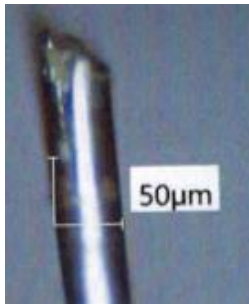
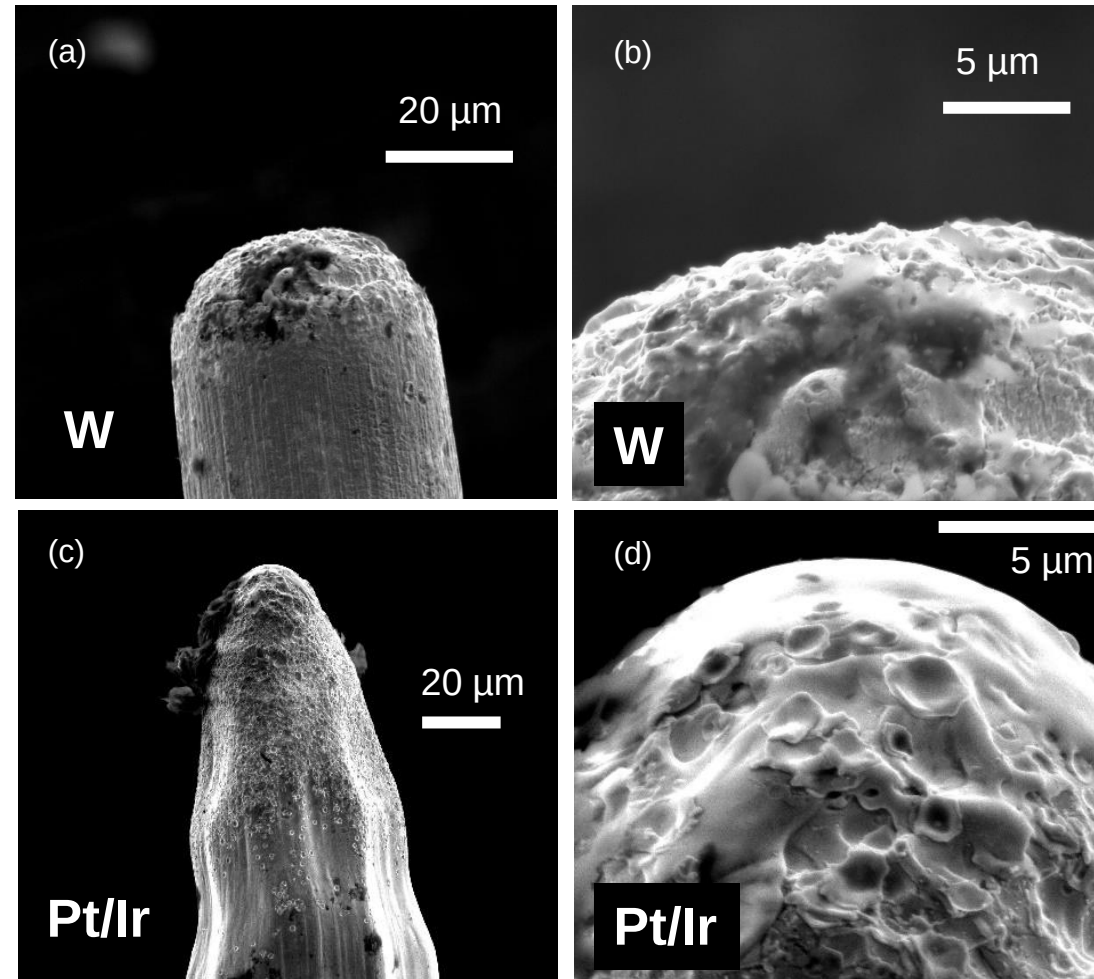


Nature of the $1/\lambda^x$ background in emission – cathode spots on the tungsten electrode



Tungsten tip vs. Platinum/Iridium tip

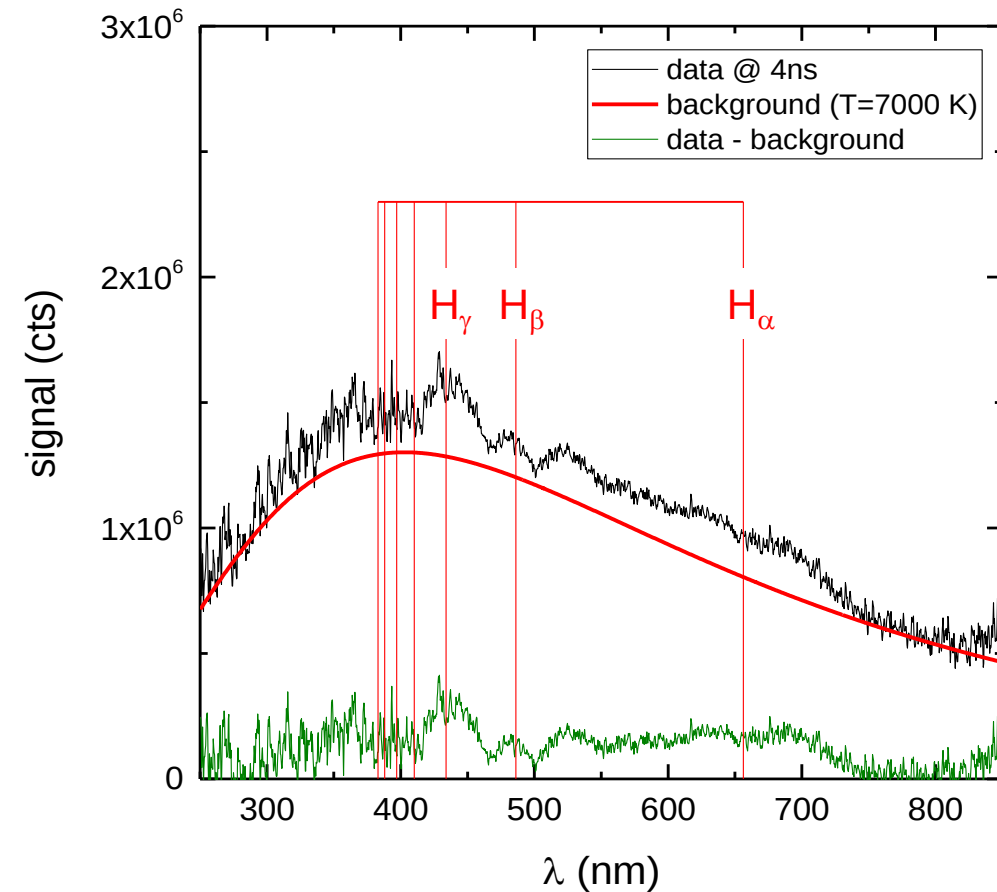
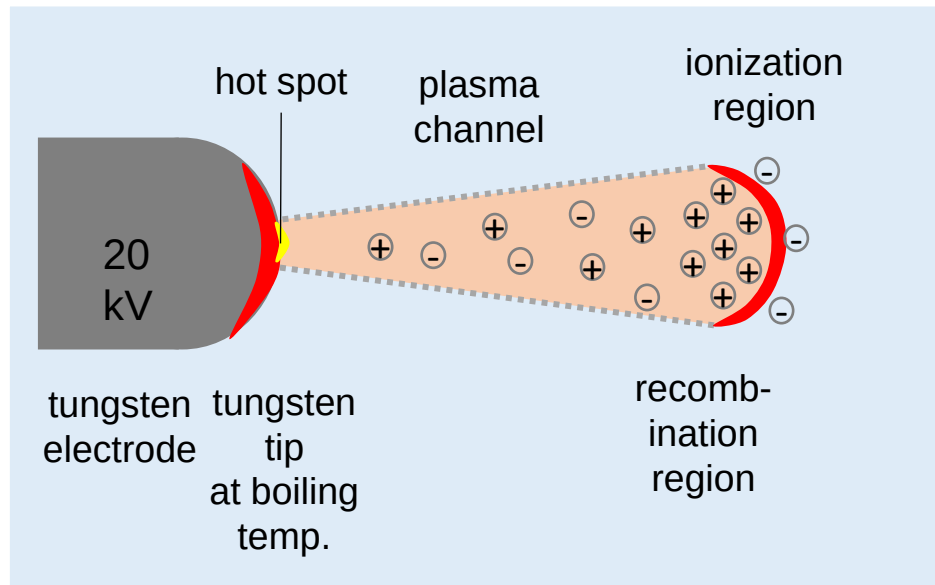
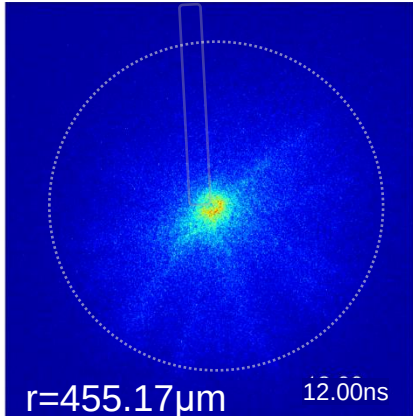
- W as high melting temperature
3700 K
- W therm. conduct.
115 W / m K
- W oxidizes, Crystallites are formed
- Pt melting temperature
2100 K
- Pt thermal conduct.
82 W/ m K
- Ir melting temperature
2700 K



Permanent operation possible

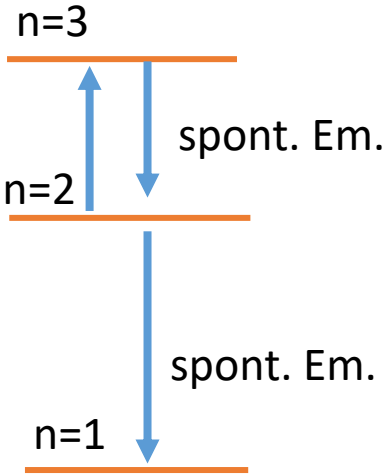
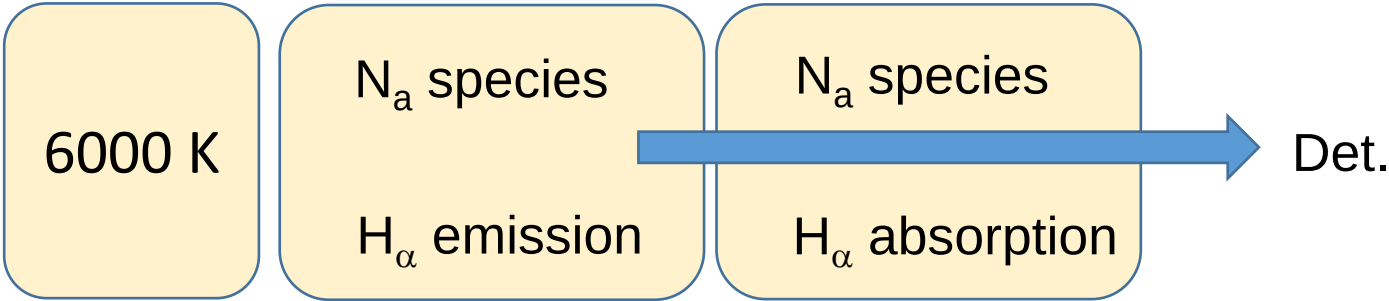
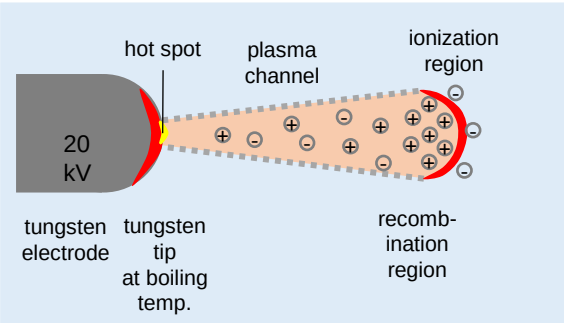
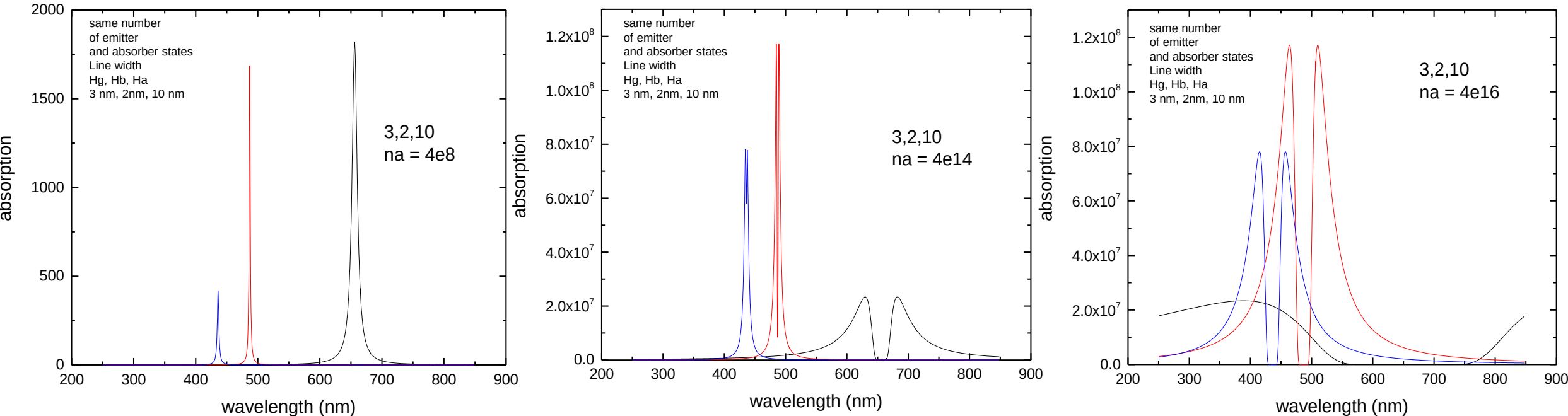
Ignition stops after 1 h of operation

Line emission – Hydrogen Balmer Series

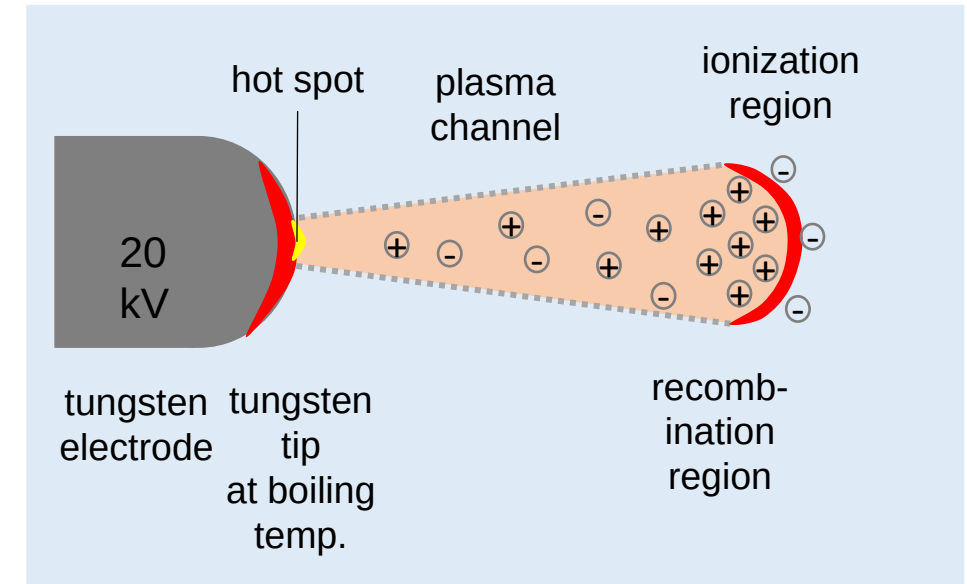
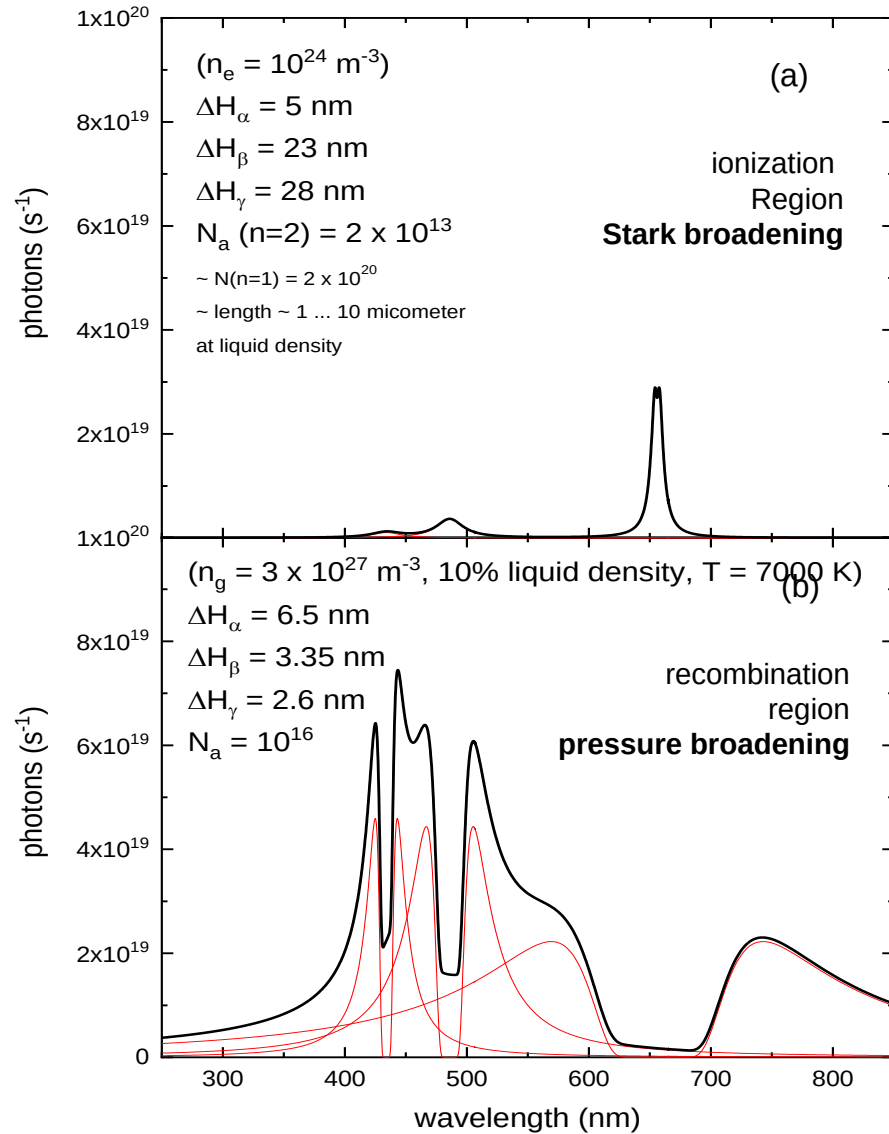


- H Balmer lines clearly visible
- Why is H_γ more pronounced than H_α ?

Line emission – Selfabsorption of Hydrogen Balmer Series



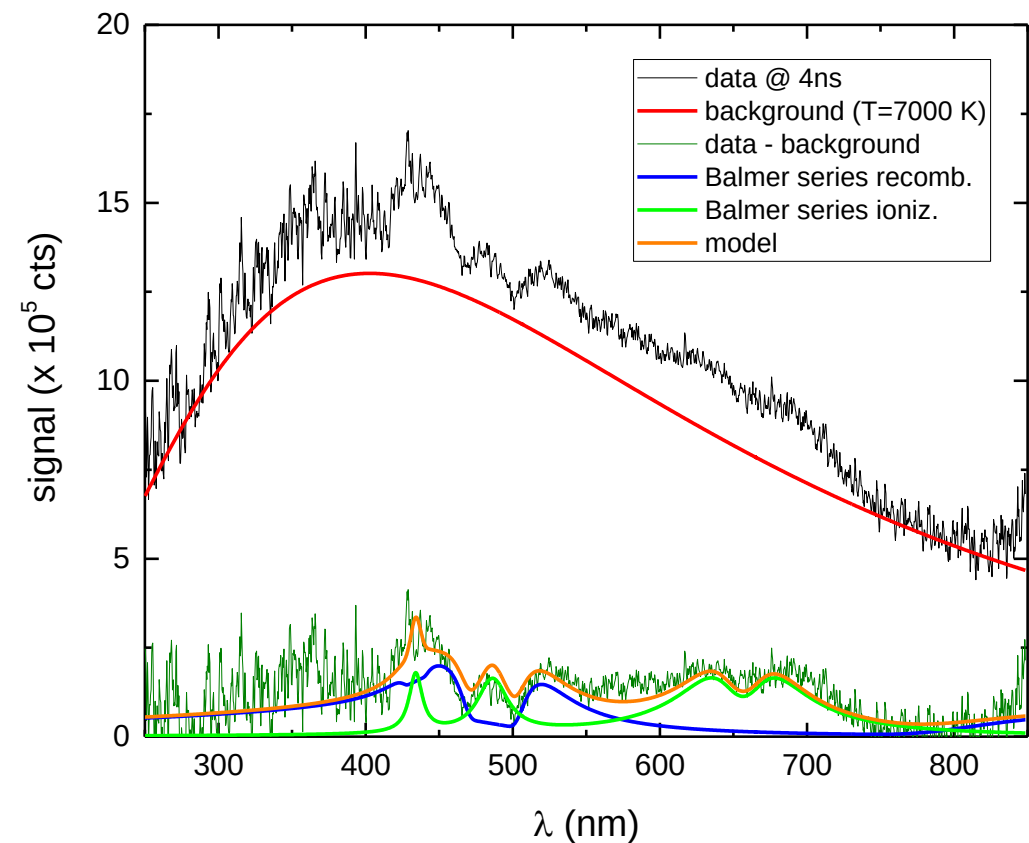
Line emission – Selfabsorption of Hydrogen Balmer Series



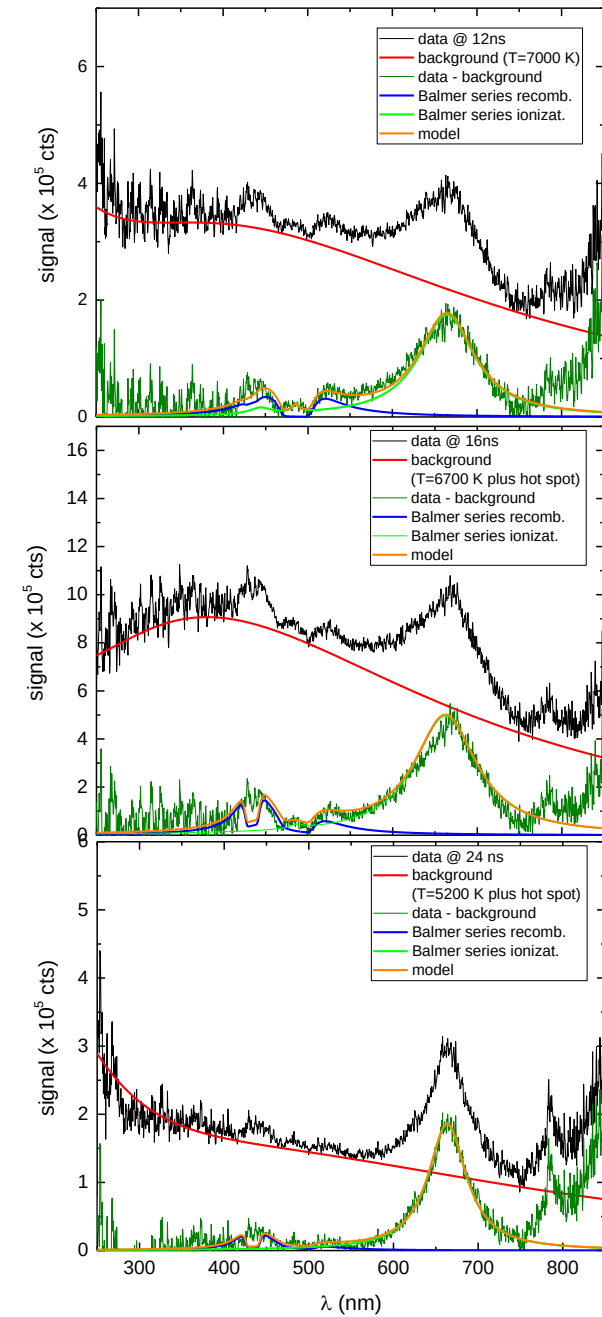
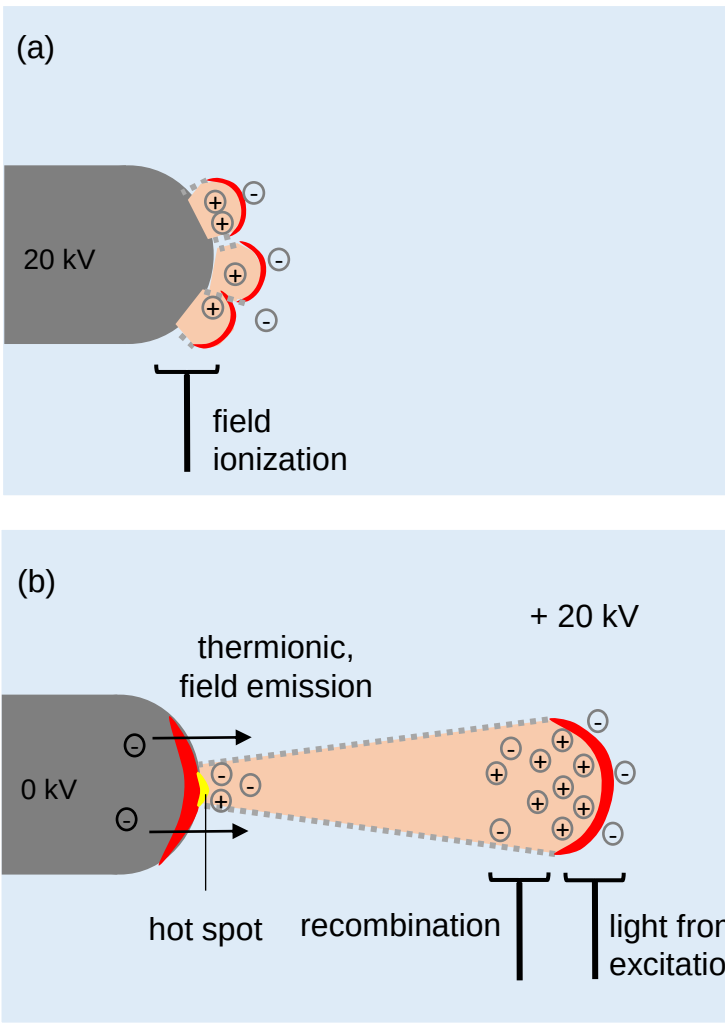
Three contributions

- Continuum blackbody $\sim 6000 - 7000 \text{ K}$
- H Balmer strong self absorption - recombination region (H_γ dominates) – Number of absorbers $\sim 50 \mu\text{m}$ region
- H Balmer small self absorption - ionization region (H_α dominates) - Number of absorbers $\sim 1 \mu\text{m}$ region

Line emission – Selfabsorption of Hydrogen Balmer Series



Degree of self-absorption of H α requires liquid density H atoms along an optical path of 1 μ m
→ Ionization occurs in high density regions
→ field effects



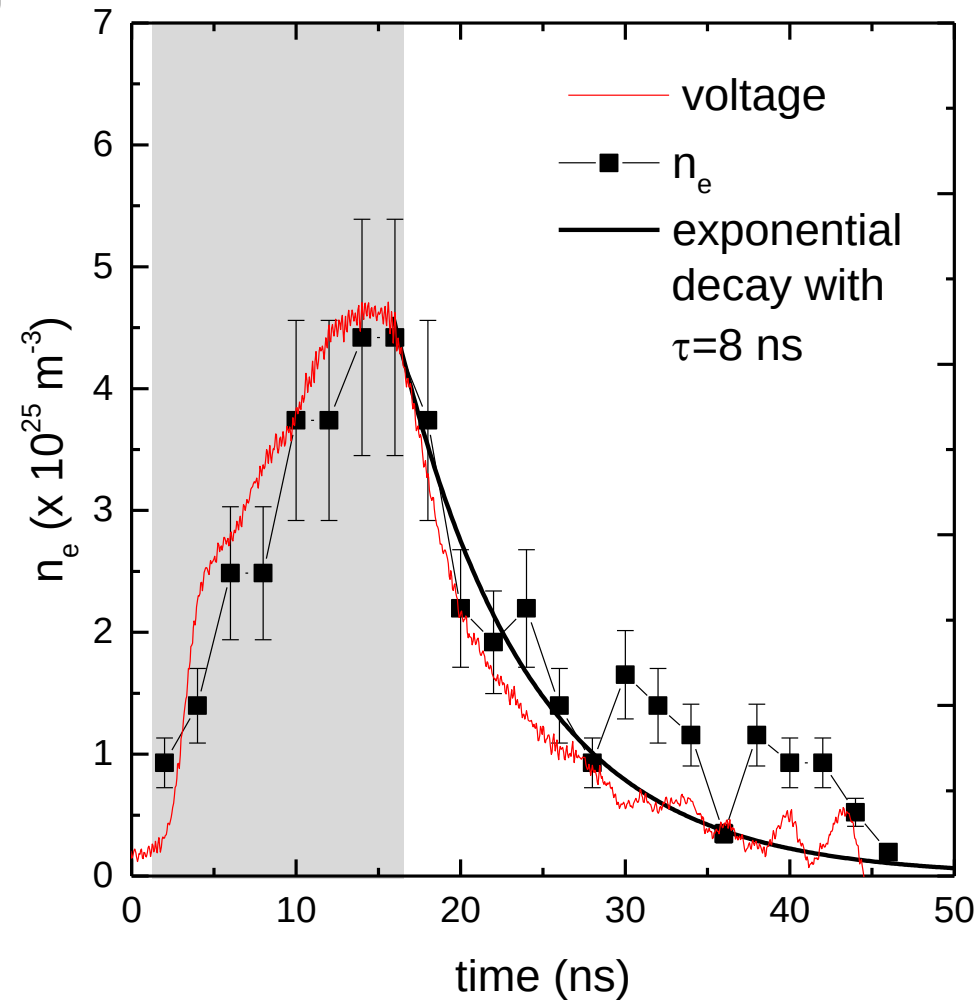
Line emission – Electron densities from Stark broadening of Hydrogen Balmer Series

electron density from Stark broadening

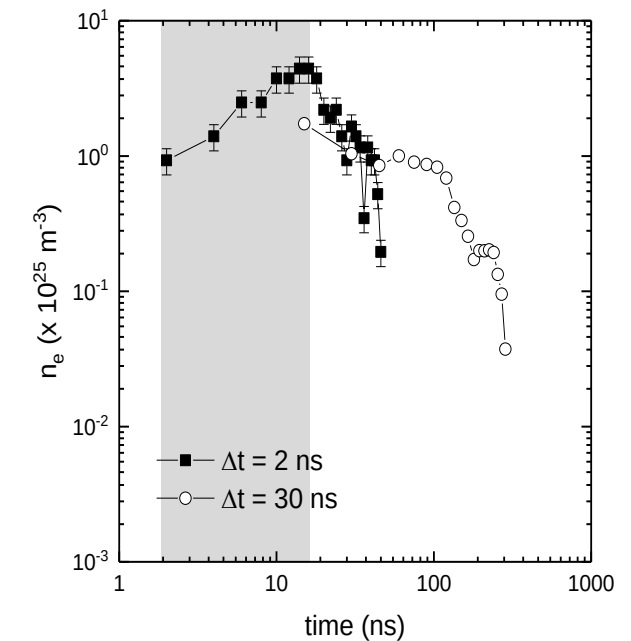
- n_e follows directly voltage (no delay as in ns air plasmas) ionization and recombination on ps time scales at liquid densities)
- decay follows the voltage

$$n_e \sim 5 \times 10^{25} \text{ m}^{-3}$$

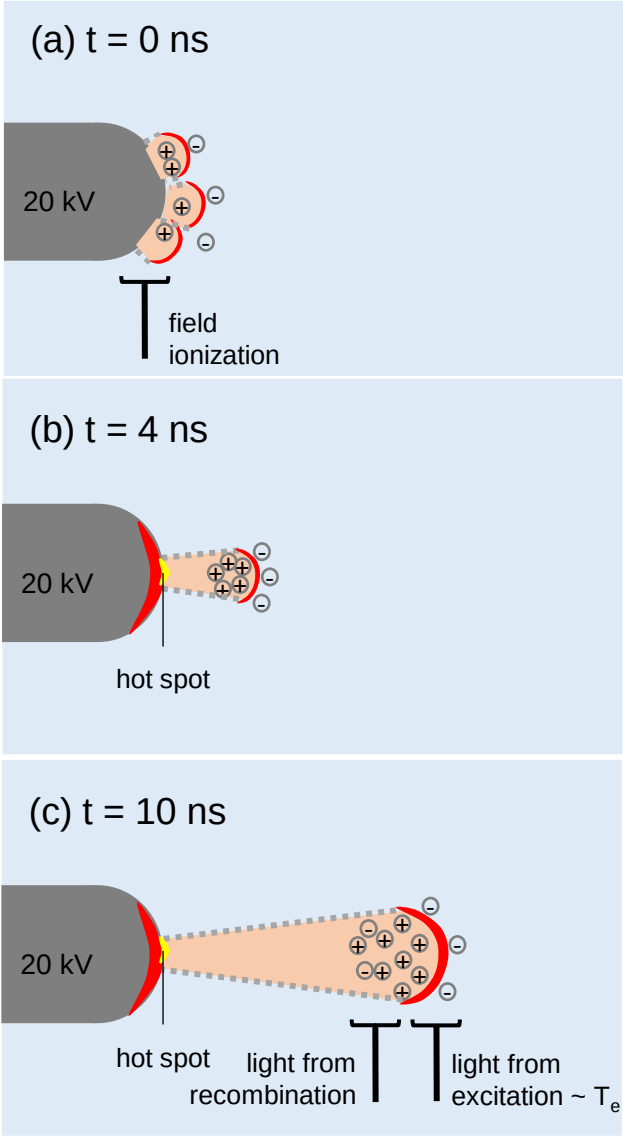
$$\text{ionization degree} \sim 10^{-3}$$



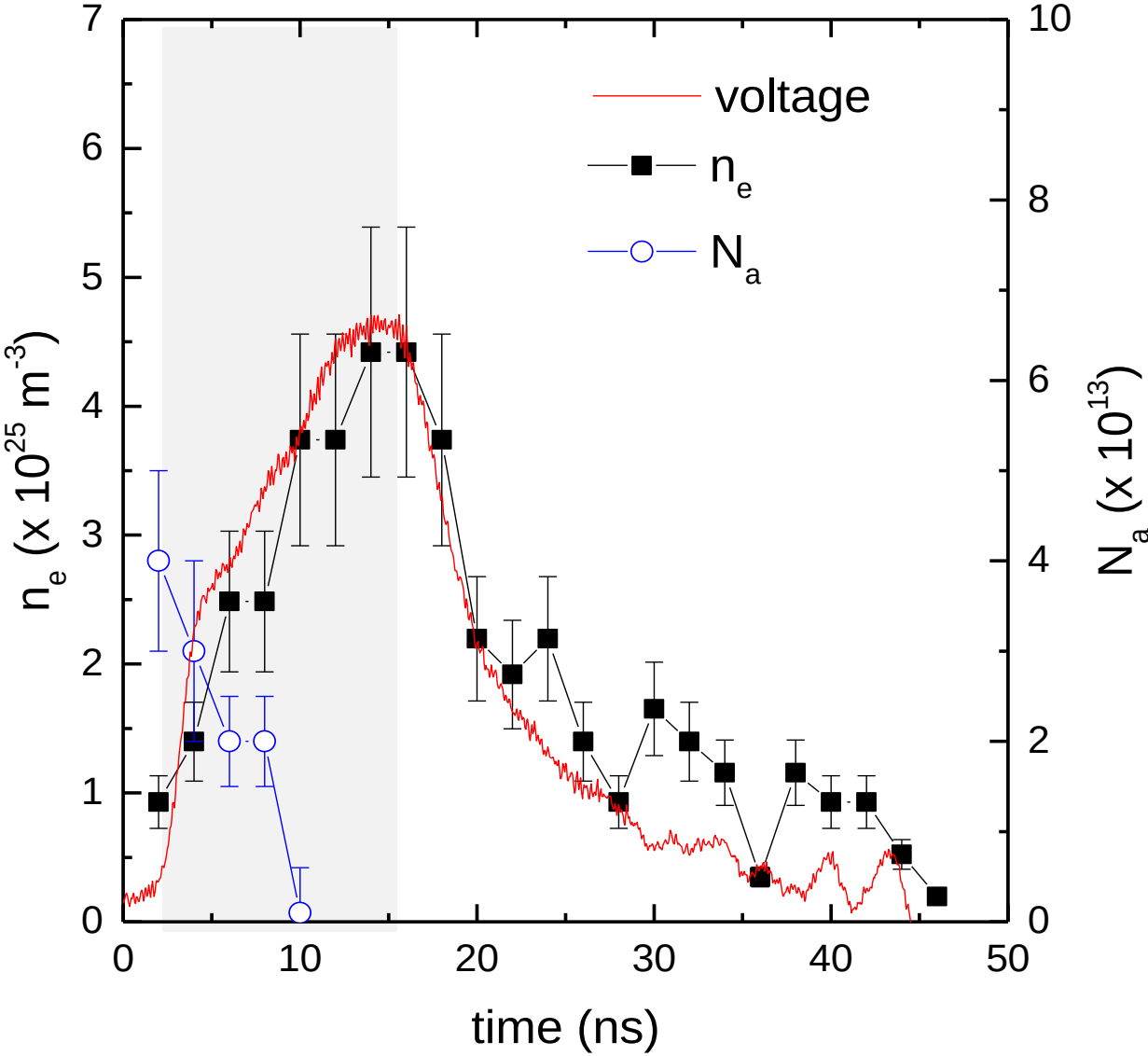
Comparison to n_e decay in the re-ignited plasmas During bubble expansion



Line emission – Ionization front propagates Hydrogen Balmer Series



self absorption of
H α from the
ionization region
disappears,
ionization front
steepens



Conclusion

ns plasmas in liquids for species conversion

- 10 ns plasma ignition in the liquid creating super critical water
- Subsequent expansion can be well described by cavitation theory
- Temperatures in the range of a few 10000 K in the beginning
- Emission dynamic dominated by black body radiation tip and cathode spot
- Pressures in the range of a few 10000 bar in the beginning
- Ignition by field emission is favored.

[Nanosecond plasmas in water: ignition, cavitation and plasma parameters](#)

Katharina Grosse, Julian Held, Maïke Kai, Achim von Keudell

Plasma Sources Sci. Technol. 28, 085003 (2019)

[Chemistry in Nanosecond plasmas in water](#)

L. Chauvet, C. Nenbangkaeo, K. Grosse, A. von Keudell

Plasma Processes and Polymers 201900192 (2019)

[Nanosecond pulsed discharges in distilled water - Part I: Continuum radiation and plasma ignition](#)

K. Grosse, V. Schulz-von der Gathen, A. von Keudell

Plasma Sources Sci. Technol. 29, 095008 (2020)

[Nanosecond pulsed discharges in distilled water - Part II: Line emission and plasma propagation](#)

A. von Keudell, K. Grosse, V. Schulz-von der Gathen

Plasma Sources Science and Technology 29, 085021 (2020)



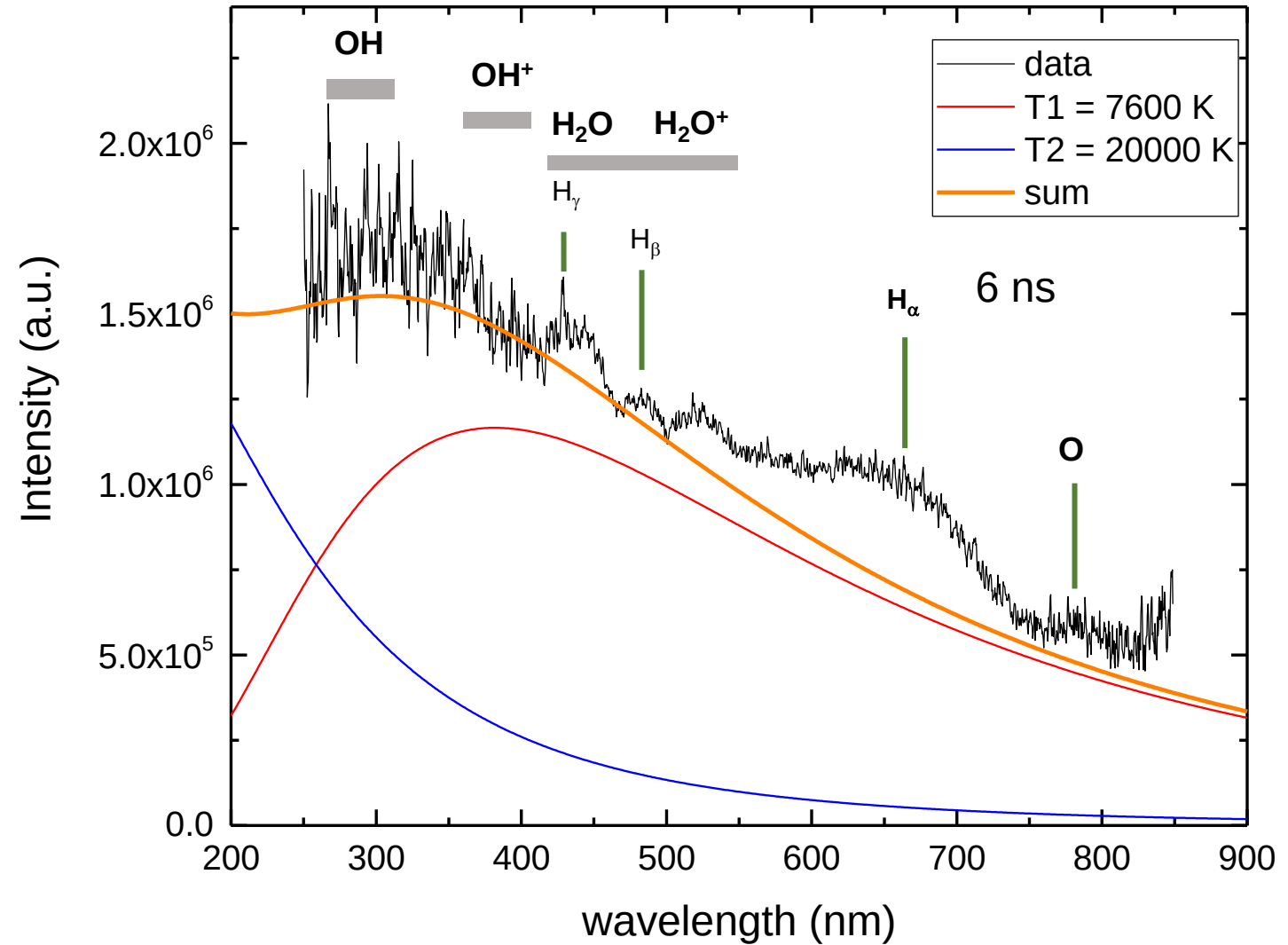
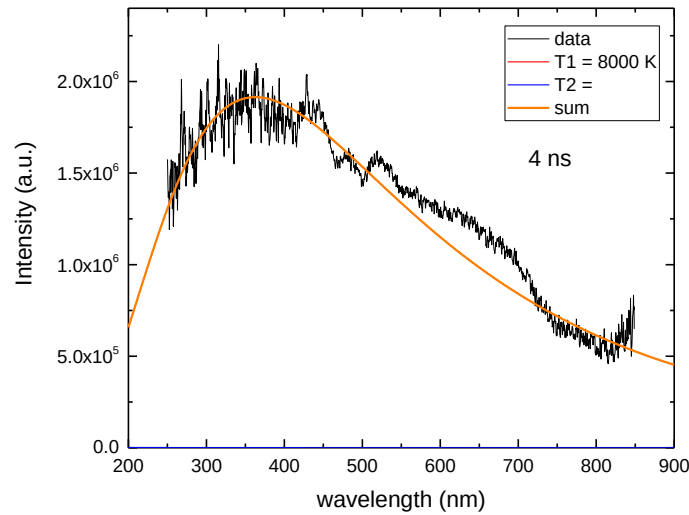
<https://sfb1316.rub.de/>

Backup Slides

Temperatures from emission spectra of the plasma UV part

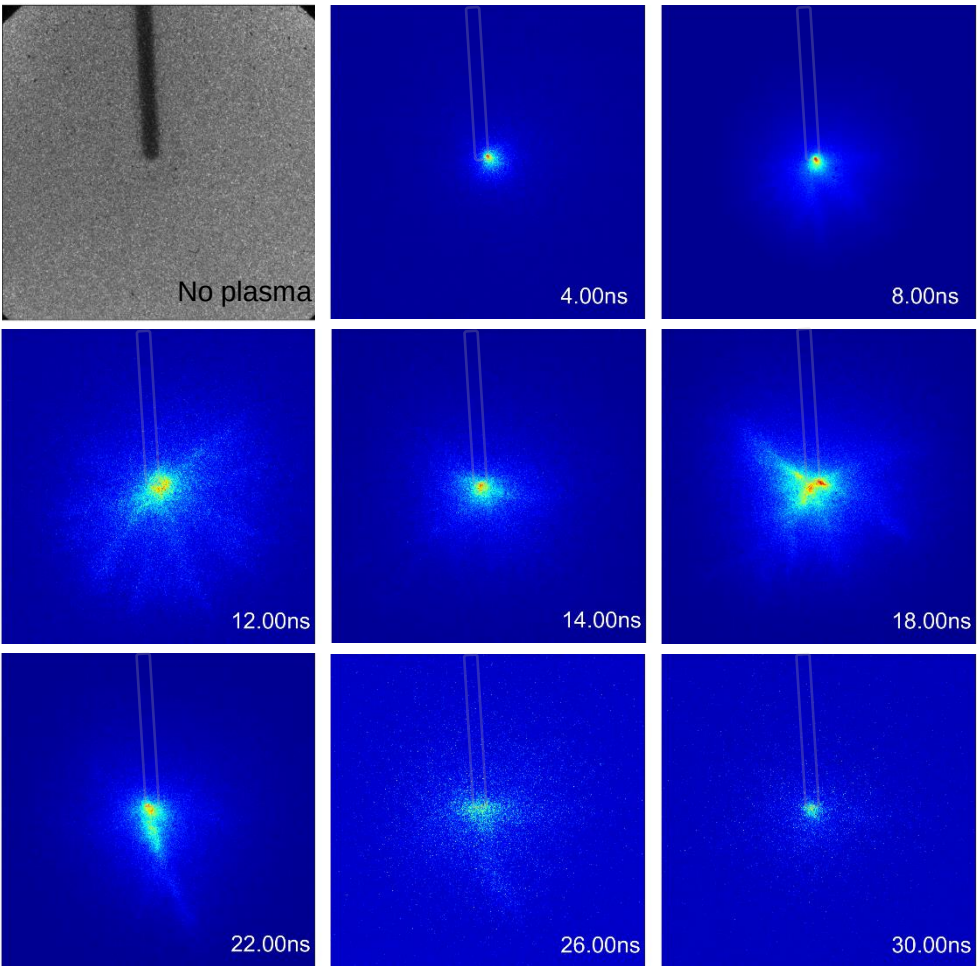
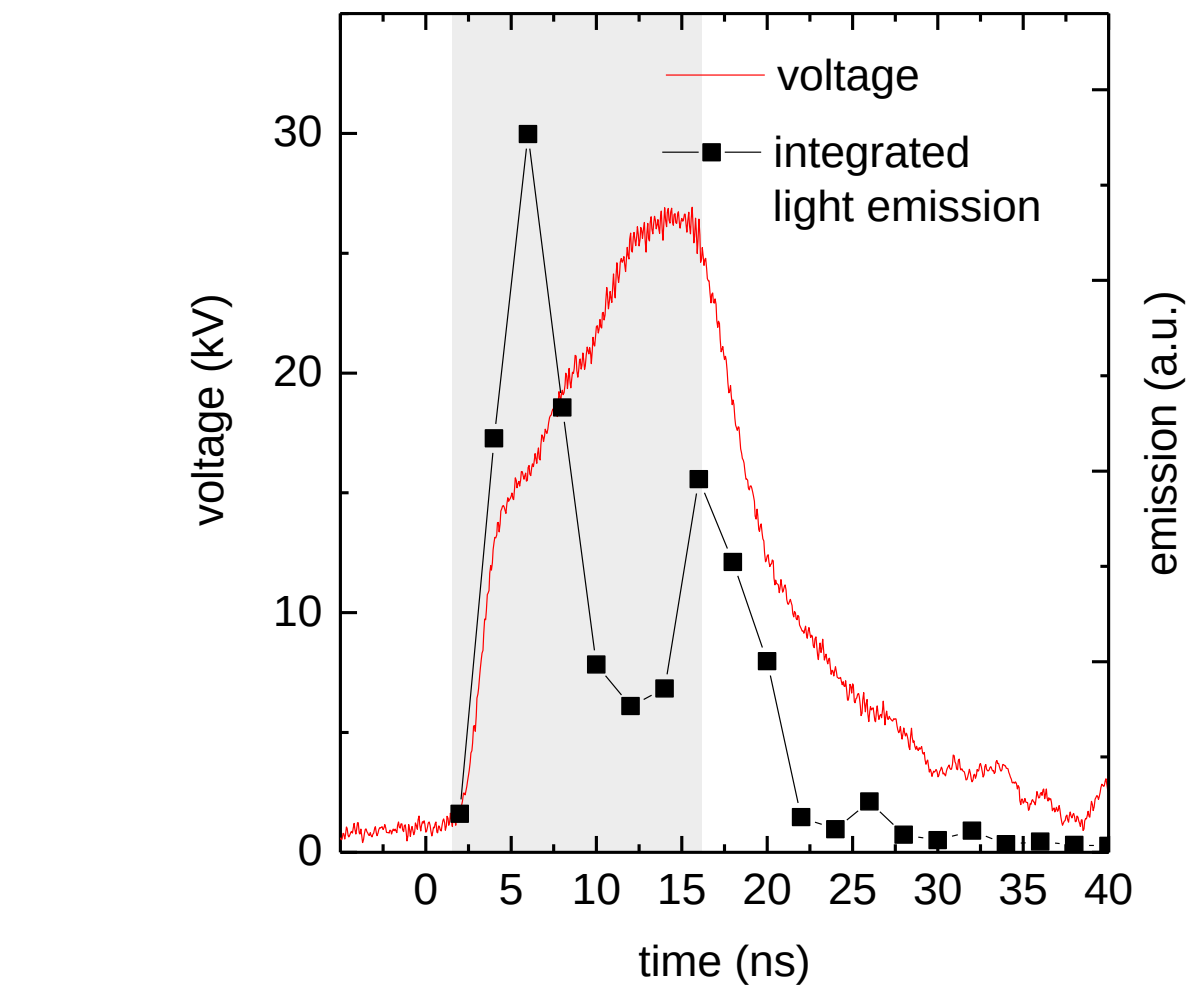
Spectrum (first 50 ns, time resolution 2 ns)

- Recombination
- H_2 , H_2O recomb. continuum
- OH, OH^+ , H_2O , H_2O^+ bands
- Black body radiation (W)
- H_α
- $\text{O}(777\text{nm})$



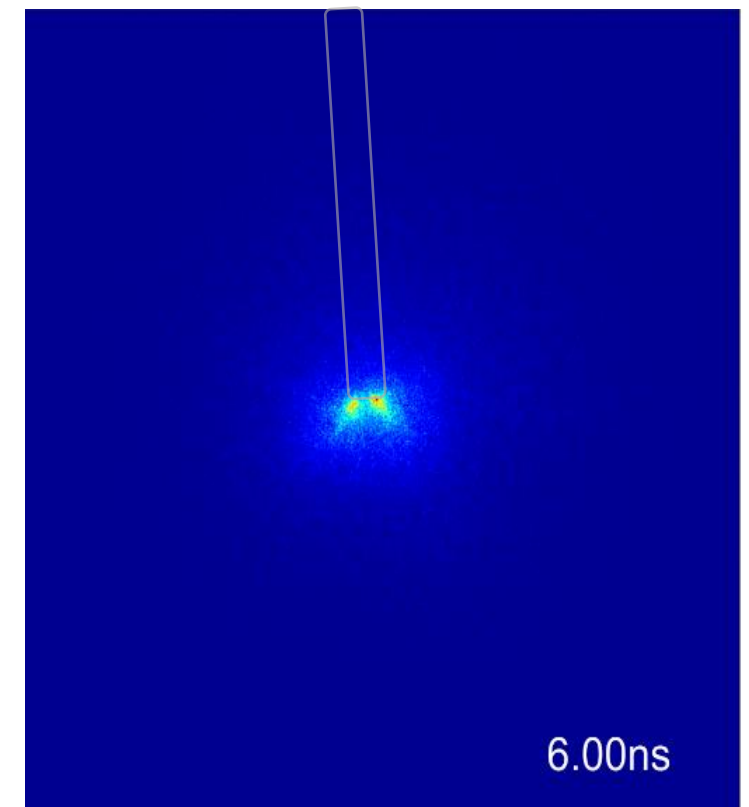
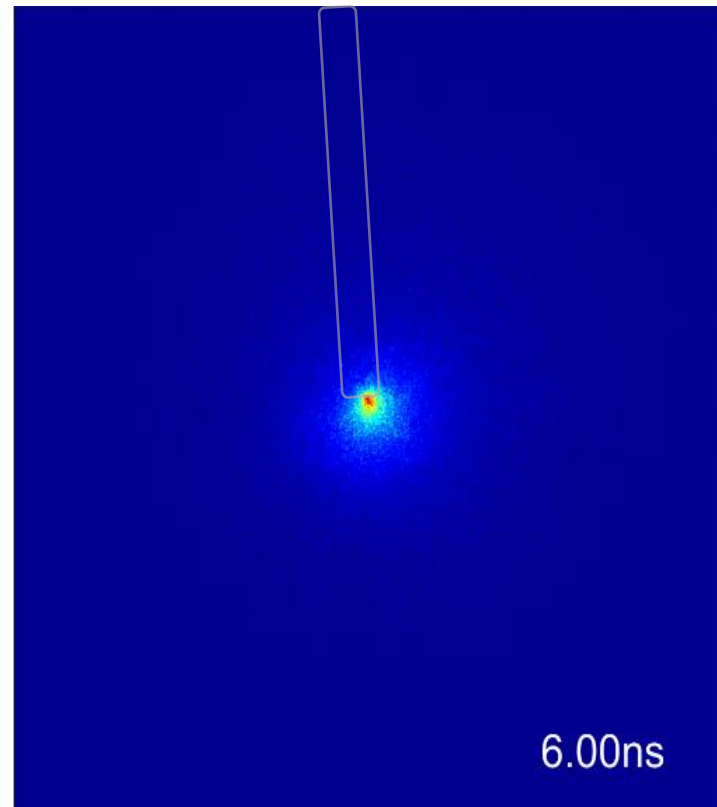
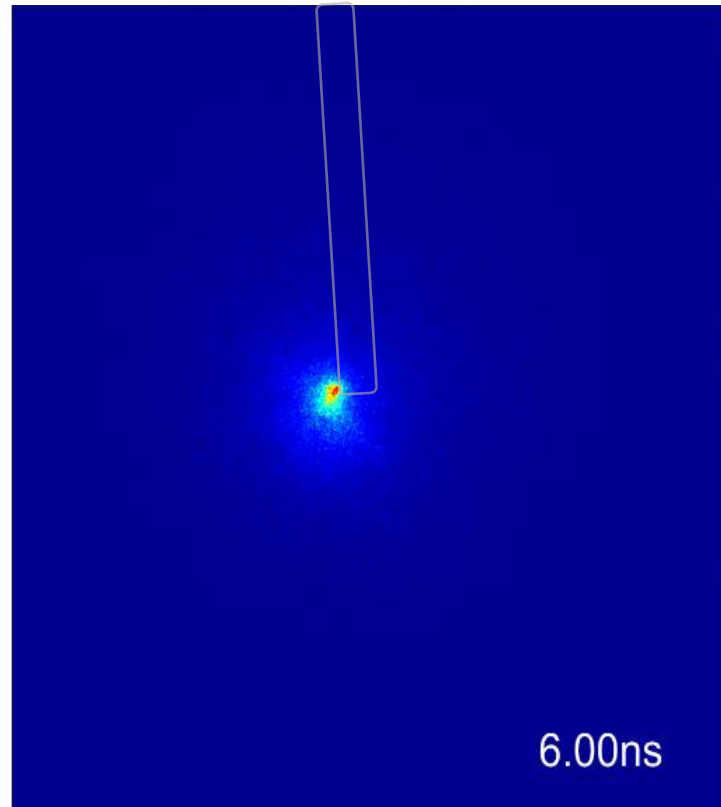
How does the plasma Ignites ?

Experiment 22kV, 1Hz, distilled water, $t_{\text{gate}}=2\text{ns}$, $t_{\text{step}}=2\text{ns}$

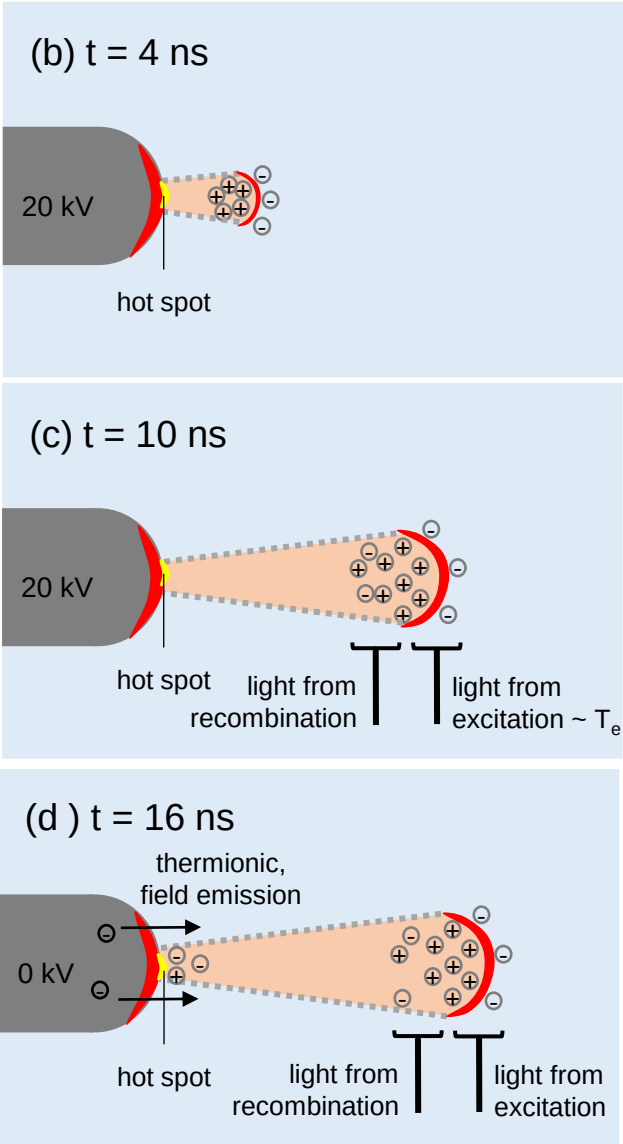


How does the plasma Ignites ?

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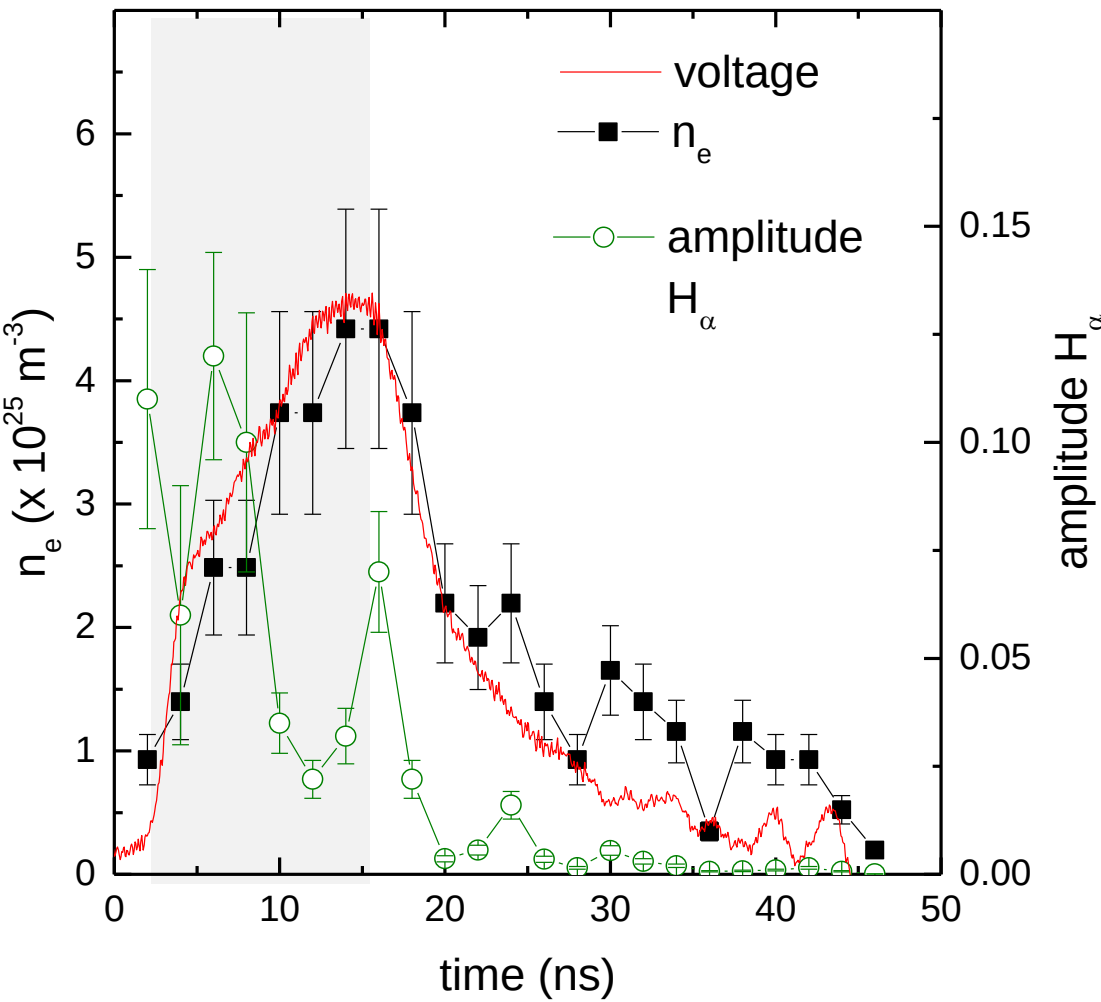
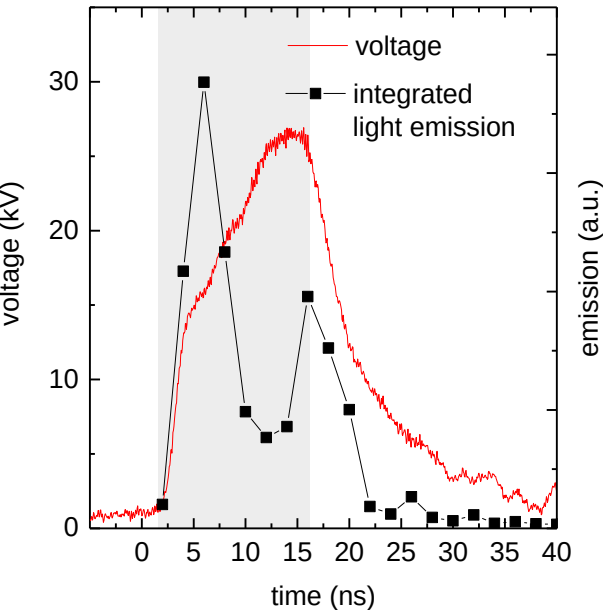


Line emission – H alpha from ionization region of Hydrogen Balmer Series



H alpha from ionization region dominates when electrons are being accelerated

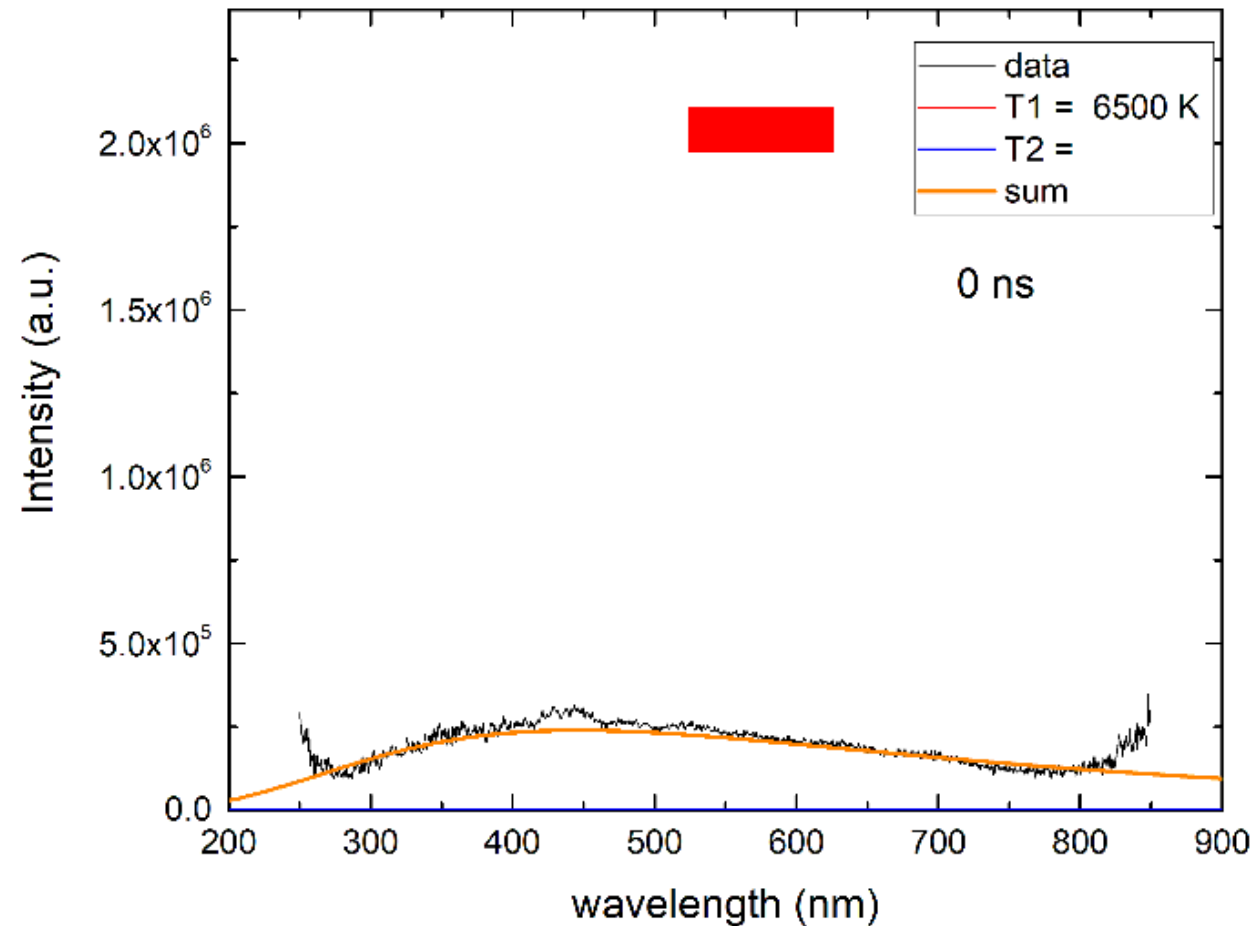
- Strong gradients in the beginning
- Field emission at the end of the pulse



Temperatures from emission spectra of the plasma into the UV

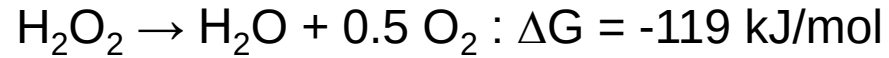
Spectrum (first 50 ns, time resolution 2 ns)

- Recombination
- H_2 , H_2O recomb. continuum
- OH , OH^+ , H_2O , H_2O^+ bands
- Black body radiation (W)
- H_α
- $\text{O}(777\text{nm})$



Efficiency to create H_2O_2 with these plasmas

Measurement of the concentration with a colorimetric kit



Measurement:

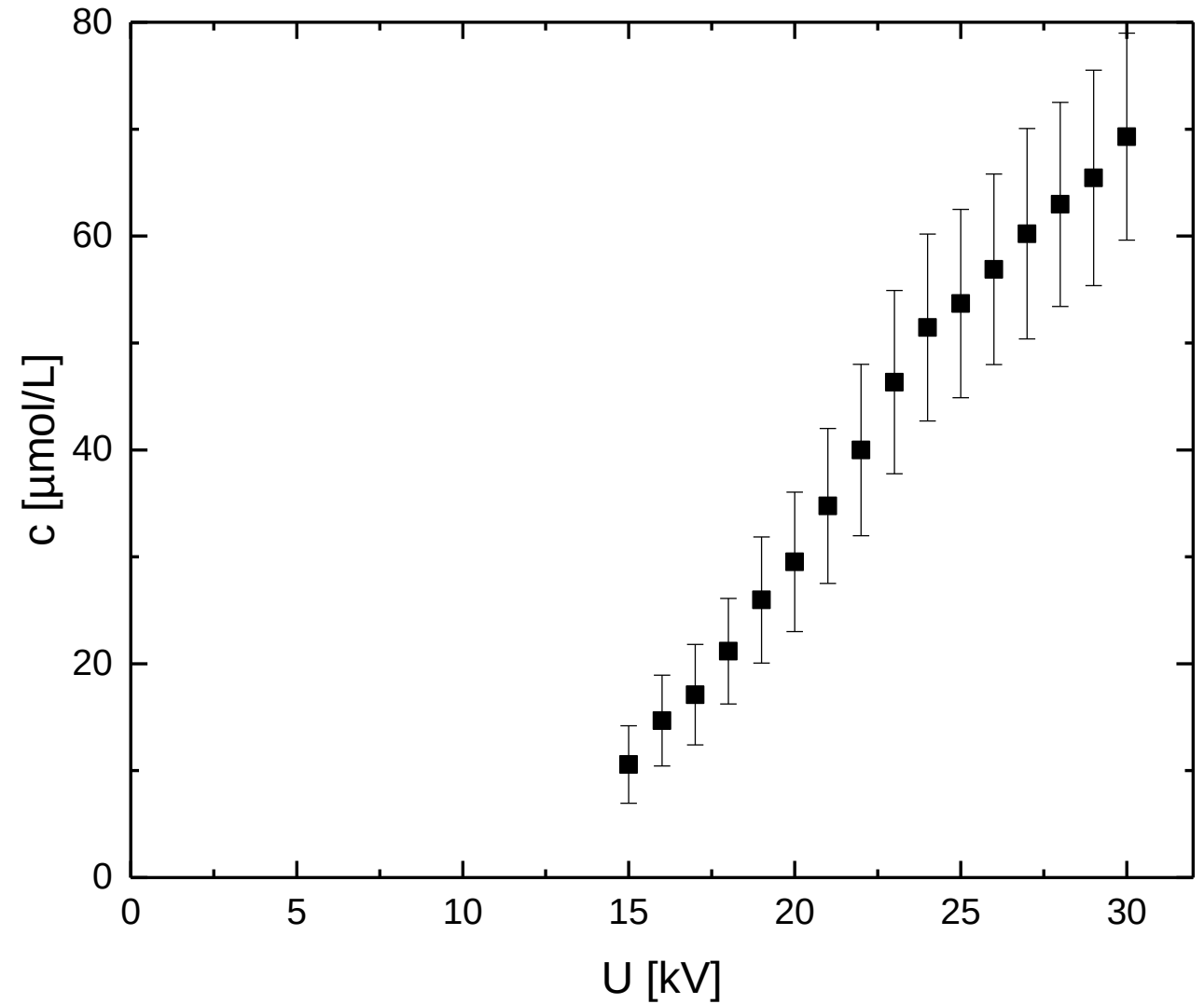
@ 20 kV, 30 $\mu\text{mol/l}$ in 25 ml liquid is equivalent to 4×10^{17} species in total

Estimate:

Species in 25 μm radius spheres at density of liquid water $3 \times 10^{22} \text{ cm}^{-3}$: 2×10^{15} species

Total number of species treated in 10 min @ 15 Hz, 10 ns pulses: 3.8×10^{19} molecules are exposed to plasma

efficiency 1.1%

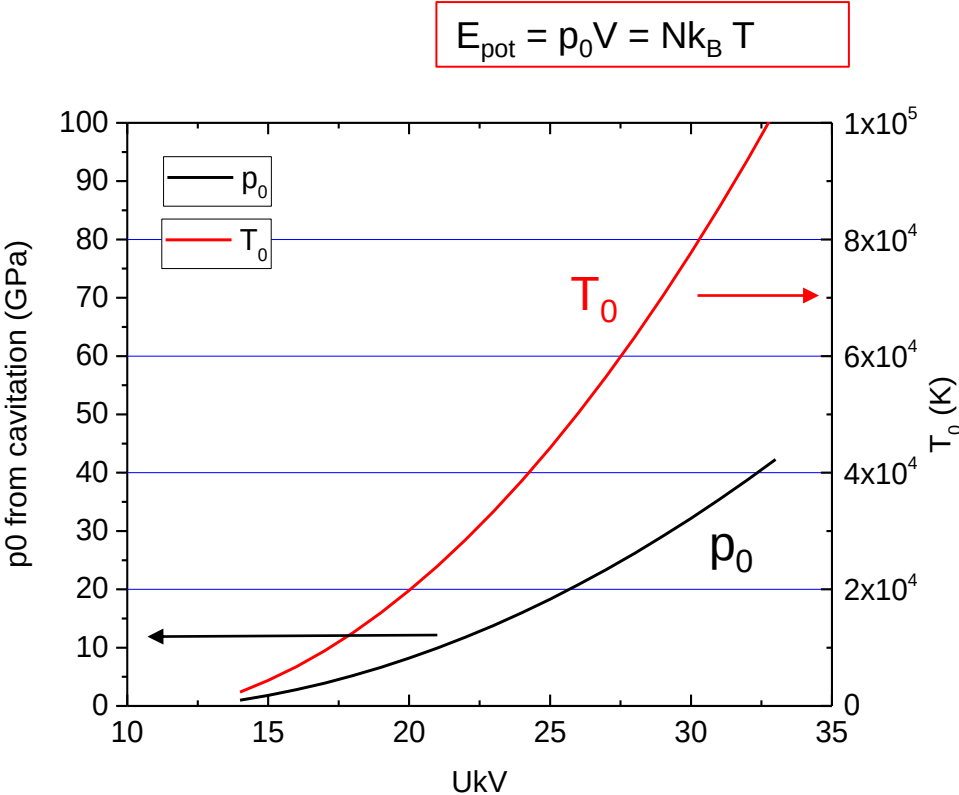


Efficiency to create H₂O₂ with these plasmas

Modeling the chemistry

*S. Mededovic, B. Locke
JPD 40, 7734 (2007)
PCPP 32, 875 (2012)

- Taking H₂O chemistry from spark plasma simulation*
- Taking the evolution of the temperature from cavitation theory



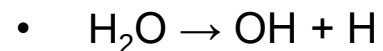
Reaction	T	rate coefficient
H₂O reactions		
H ₂ O + M → H + OH + M	2000-6000 K	$k_{21} = 5.8 \cdot 10^{-9} \exp[-440000(RT)^{-1}]$
O₂ reactions		
O ₂ + M → O + O + M	200-10000 K	$k_{27} = 1.99 \cdot 10^{-10} \exp[-9500(RT)^{-1}]$
OH reactions		
OH + M → H + O + M	300-2500 K	$k_{22} = 4.09 \cdot 10^{-9} \exp[-416000(RT)^{-1}]$
OH + OH → H ₂ O + O	250-300 K	$k_{29} = 1.02 \cdot 10^{-12} (T/298)^{1.4} \exp[1660(RT)^{-1}]$
O + OH → O ₂ + H	250-5000 K	$k_{81} = 4.55 \cdot 10^{-12} (T/298)^{0.4} \cdot \exp[3090(RT)^{-1}]$
OH + H → H ₂ O	300-2100 K	$k_{82} = 2.69 \cdot 10^{-10} \exp[-620(RT)^{-1}]$
H + OH → O + H ₂	300-2500 K	$k_{83} = 6.68 \cdot 10^{-14} (T/298)^{2.8} \cdot \exp[-16210(RT)^{-1}]$
H ₂ O ₂ + OH → HO ₂ + H ₂ O	300-2500 K	$k_{84} = 2.91 \cdot 10^{-12} \cdot \exp[-1330(RT)^{-1}]$
O ₂ + OH → HO ₂ + O	300-2500 K	$k_{85} = 3.7 \cdot 10^{-11} \cdot \exp[-220000(RT)^{-1}]$
OH + OH → H ₂ O ₂	300-1500 K	$k_{86} = 1.51 \cdot 10^{-11} (T/298)^{-0.37}$
OH + OH → 2 O + 2 H	300-2500 K	$k_{87} = 4.09 \cdot 10^{-9} \cdot \exp[-416000(RT)^{-1}]$
H₂O₂ reactions		
H ₂ O ₂ + O → HO ₂ + OH	300-2500 K	$k_{88} = 1.42 \cdot 10^{-12} (T/298)^2 \exp[-16631(RT)^{-1}]$
H ₂ O ₂ + H → OH + H ₂ O	300-2500 K	$k_{89} = 4.01 \cdot 10^{-11} \exp[-16630(RT)^{-1}]$
H ₂ O ₂ + H → HO ₂ + H ₂	300-2500 K	$k_{810} = 8 \cdot 10^{-11} \exp[-33260(RT)^{-1}]$
H ₂ O ₂ + O ₂ → 2 HO ₂	300-2500 K	$k_{811} = 9 \cdot 10^{-11} \exp[-166000(RT)^{-1}]$
HO₂ reactions		
HO ₂ + OH → H ₂ O + O ₂	300-2000 K	$k_{812} = 4.81 \cdot 10^{-11} \exp[2080(RT)^{-1}]$
HO ₂ + O → OH + O ₂	300-2500 K	$k_{813} = 2.91 \cdot 10^{-11} \exp[-1660(RT)^{-1}]$
HO ₂ + H → 2 OH	300-2500 K	$k_{814} = 2.81 \cdot 10^{-10} \exp[-3660(RT)^{-1}]$
HO ₂ + H → H ₂ + O ₂	300-2500 K	$k_{815} = 1.1 \cdot 10^{-10} \exp[-8900(RT)^{-1}]$
HO ₂ + HO ₂ → H ₂ O ₂ + O ₂	300-2500 K	$k_{816} = 3.01 \cdot 10^{-12}$
HO ₂ + H ₂ → H ₂ O ₂ + H	300-2500 K	$k_{817} = 5 \cdot 10^{-11} \exp[-109000(RT)^{-1}]$
HO ₂ + M → O ₂ + H + M	300-2200 K	$k_{818} = 2.41 \cdot 10^{-8} (T/298)^{-1.18} \exp[-2031000(RT)^{-1}]$
H reactions		
O + H + M → OH + M	300-2500 K	$k_{819} = 4.36 \cdot 10^{-32} (T/298)^{-1}$
H + H + M → M + H ₂	300-2500 K	$k_{820} = 6.04 \cdot 10^{-33} (T/298)^{-1}$
O ₂ + H → OH + O	500-2000 K	$k_{821} = 2.94 \cdot 10^{-10} \exp[-69680(RT)^{-1}]$
O ₂ + H + M → HO ₂ + M	200-2200 K	$k_{822} = 1.94 \cdot 10^{-32} (T/298)^{-1}$
H₂ reactions		
H ₂ + M → H + H + M	2500-8000 K	$k_{25} = 1.5 \cdot 10^{-9} \exp[-402000(RT)^{-1}]$
OH + H ₂ → H ₂ O + H	200-2400 K	$k_{823} = 2.97 \cdot 10^{-12} (T/298)^{1.21} \exp[-19710(RT)^{-1}]$
O + H ₂ → OH + H	300-2500 K	$k_{824} = 3.44 \cdot 10^{-13} (T/298)^{2.67} \exp[-26270(RT)^{-1}]$
O reactions		
O + O + M → O ₂ + M	200-4000 K	$k_{825} = 5.21 \cdot 10^{-36} \exp[7480(RT)^{-1}]$
O + H ₂ O → OH + OH	300-2000 K	$k_{826} = 6.68 \cdot 10^{-13} (T/298)^{2.60} \exp[-63520(RT)^{-1}]$

Efficiency to create H_2O_2 with these plasmas

Modeling the chemistry

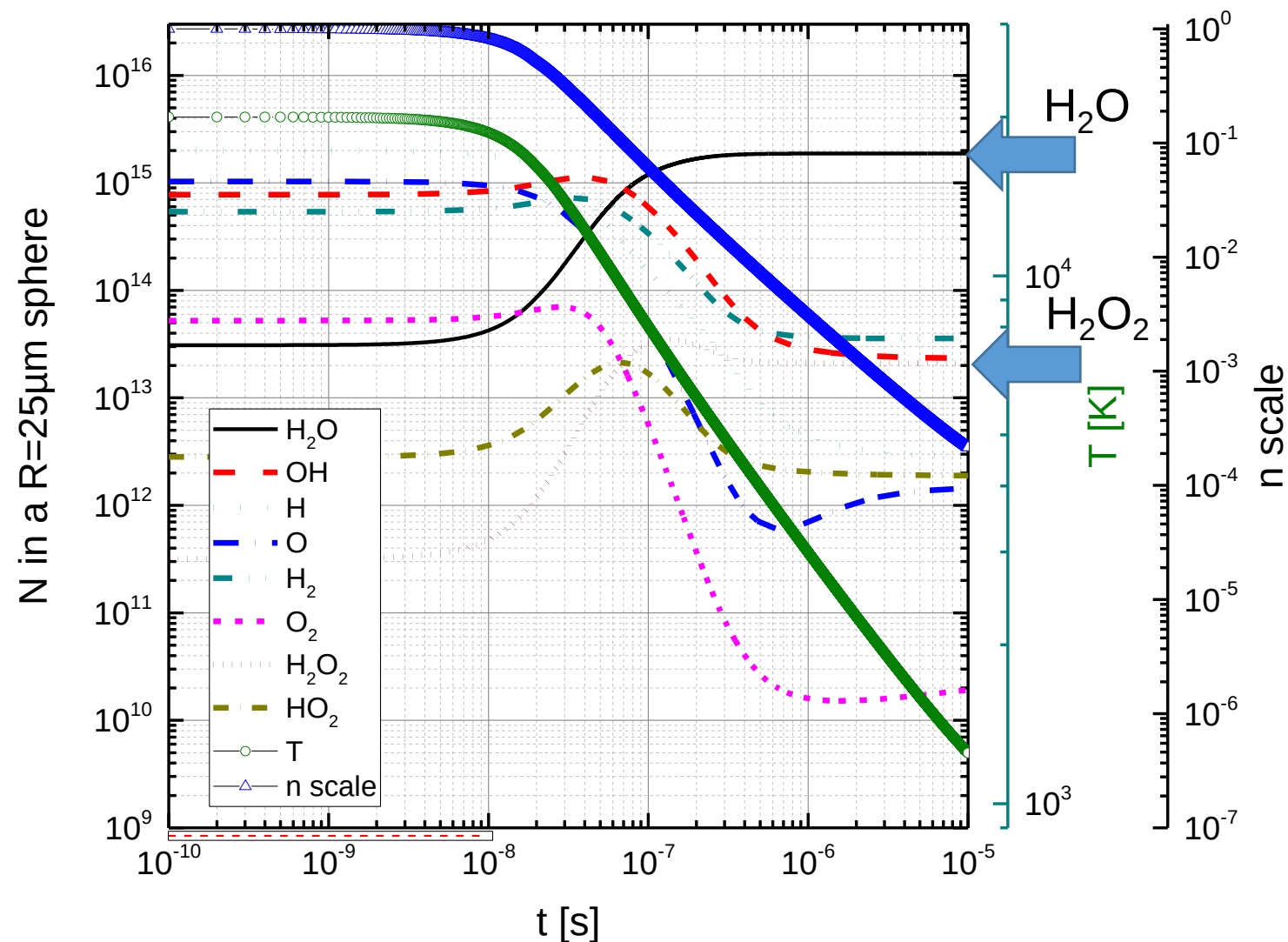
- Starting point
gas density $3 \times 10^{22} \text{ cm}^{-3}$
- Starting Temperature $T = 20000 \text{ K}$
- $\text{H}_2\text{O}_2/\text{H}_2\text{O}$ ratio at $10 \mu\text{s} \sim 10^{-2}$**

Hot phase:



recombination phase

- $\text{OH} + \text{OH} \rightarrow \text{H}_2\text{O}_2$
- $\text{H} + \text{H} \rightarrow \text{H}_2$
- $\text{OH} + \text{H} \rightarrow \text{H}_2 + \text{O}$



*S. Mededovic, B. Locke
JPD 40, 7734 (2007)
PCPP 32, 875 (2012)

In the expanding phase, chemistry freezes out, $\text{H}_2\text{O} \rightarrow \text{H}_2\text{O}_2 + \text{H}_2 + \text{O} + \text{H}$

Efficiency to create H_2O_2 with these plasmas

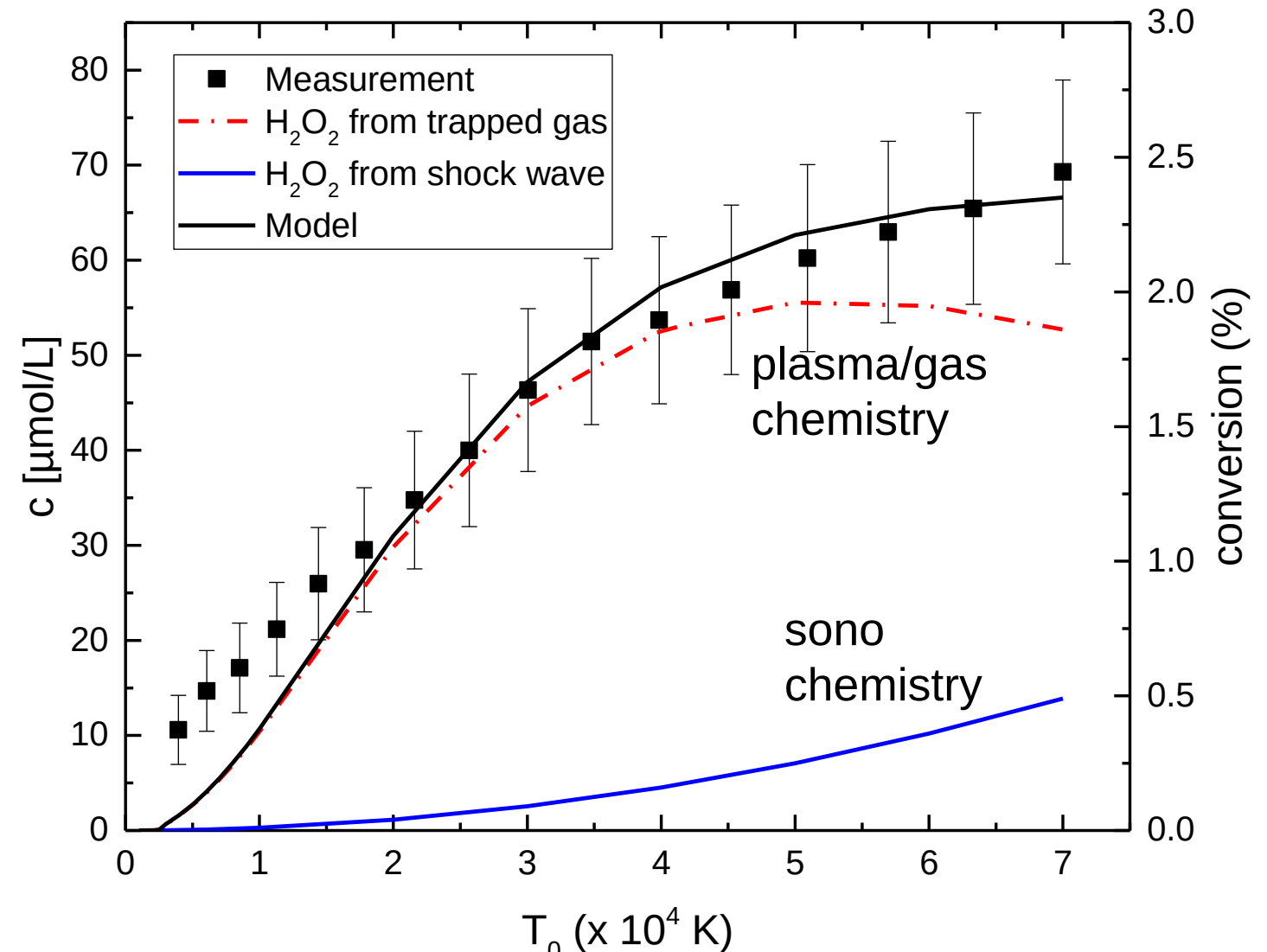
Modeling the chemistry

- Take T_0 from cavitation
- calculate time development of the chemistry until $10\ \mu\text{s}$
- determine H_2O_2 concentration after $10\ \mu\text{s}$ in the model

efficiency 1.1%
@ 20 kV (20000 K)

- At high voltages/ T_0 , contribution due to sonochemistry becomes significant

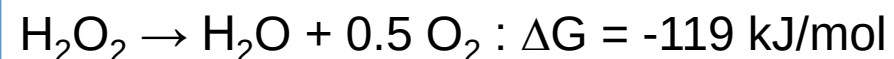
46 g H_2O_2 /kWh
(most other plasma methods only a few g/kWh)



Efficiency to create H₂O₂ with these plasmas

Modeling the chemistry

- Take T₀ from cavitation
- use chemical equilibrium



0th order reaction (no local H₂O depletion)

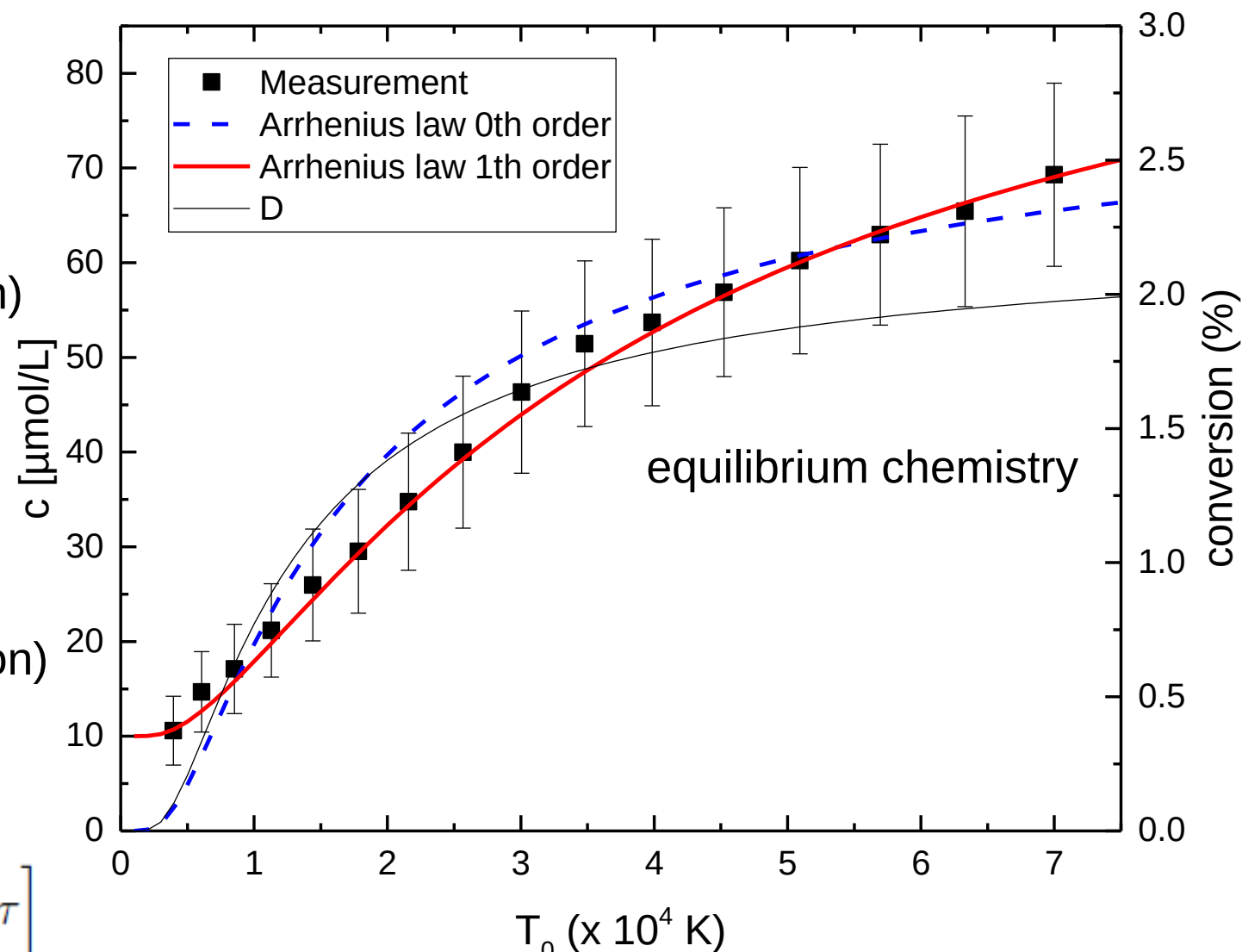
$$\frac{dn_{\text{H}_2\text{O}_2}}{dt} = kn_{\text{H}_2\text{O}}$$

$$n_{\text{H}_2\text{O}_2} = \exp\left(-\frac{E_a}{RT}\right) n_{\text{H}_2\text{O}}\tau + n_{\text{H}_2\text{O}_2}|_0$$

1st order reaction (with local H₂O depletion)

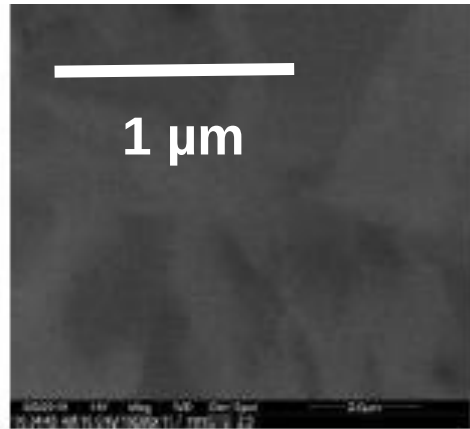
$$\frac{dn_{\text{H}_2\text{O}_2}}{dt} = -\frac{dn_{\text{H}_2\text{O}}}{dt} = kn_{\text{H}_2\text{O}}$$

$$n_{\text{H}_2\text{O}_2} = n_{\text{H}_2\text{O}_2}|_0 \exp\left[\exp\left(-\frac{E_a}{RT}\right) n_{\text{H}_2\text{O}}\tau\right]$$

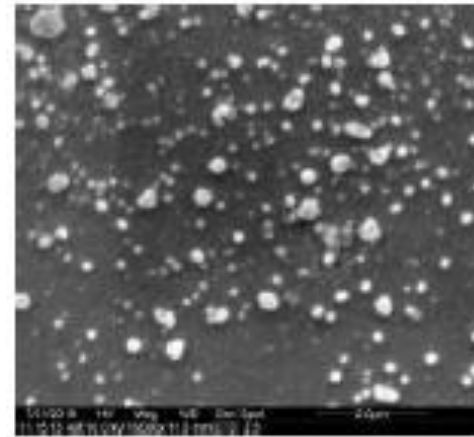


Nanosecond plasma based recovery of CuO nanocubes at copper electrodes

distilled water



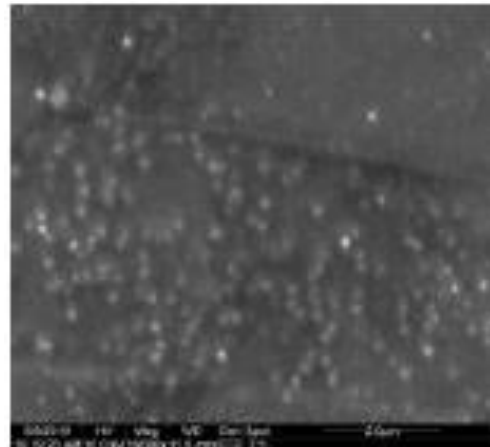
dist. Water + 0.0035M KCl



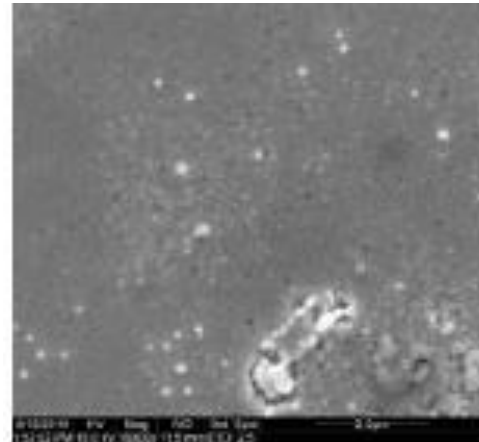
Creation of Cu-nanocubes possible, if

- no direct current to the sample, reduction of the oxide, plasma electrode distance to the sample important
- Competition between oxidation due to H_2O_2 , OH and reduction by H, e^-

distilled water



dist. Water + 0.0035M KCl



P. Grosse, B. Roldan et al.

Reference plasma based low pressure creation of CuO nanocubes

$\langle p \rangle_{\text{initial}}$ scales with the dissipated energy

$$p_0 V_0 / \Delta t = P_{\text{electrical}} = U^2 / R$$

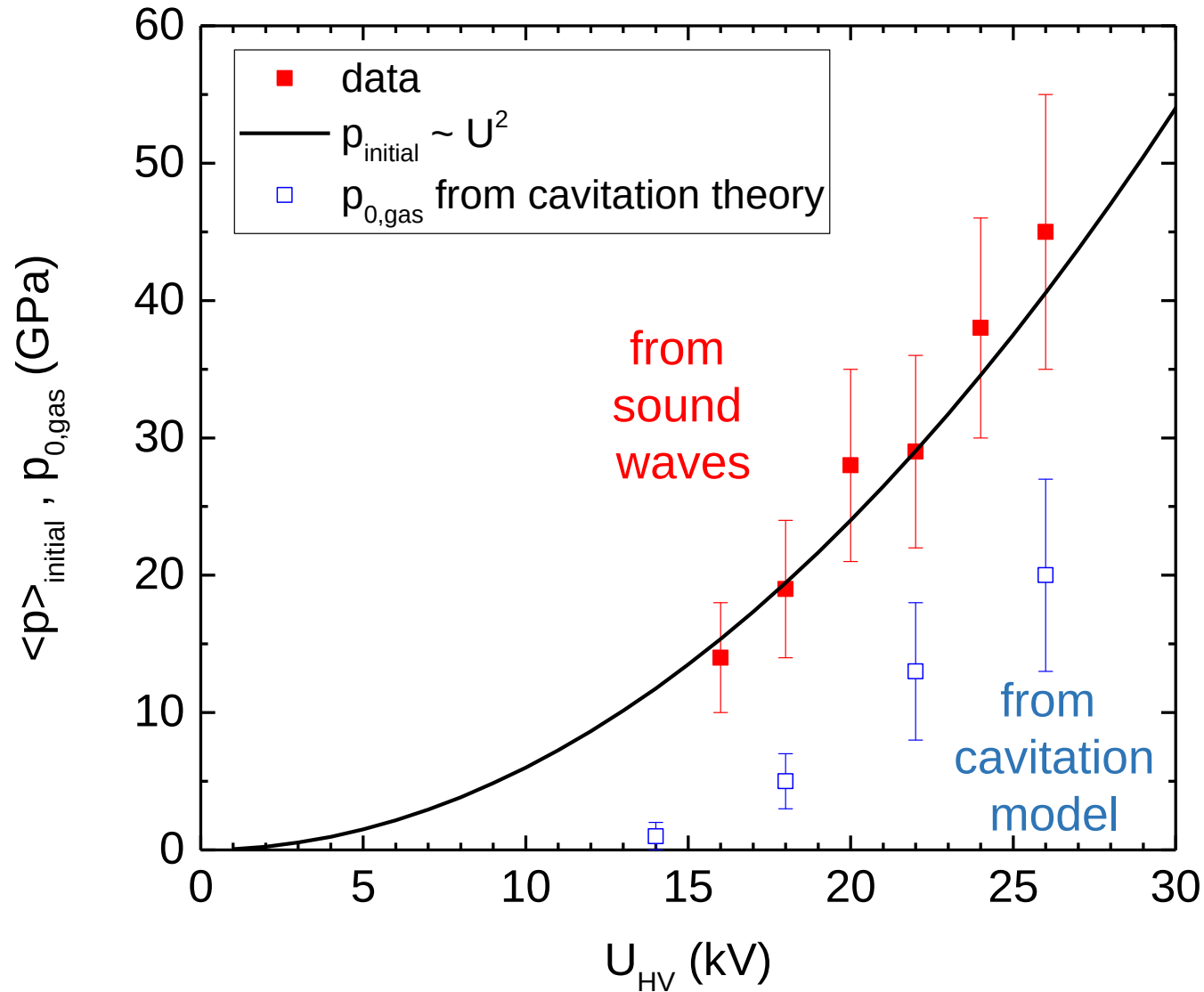
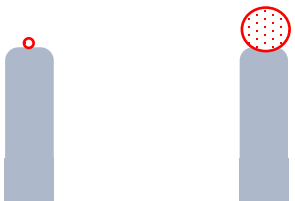
for $R = 2.5 \text{ k}\Omega$

p_0, V_0

$r = 25 \text{ }\mu\text{m}$
 $t = 10 \text{ ns}$

$T \sim$
**2000...
70000 K**

**Ignition
plasma**



26 ns

0.5 mm

gate 2ns

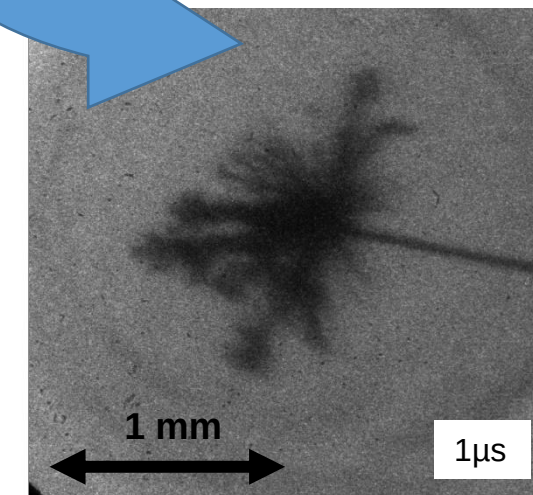
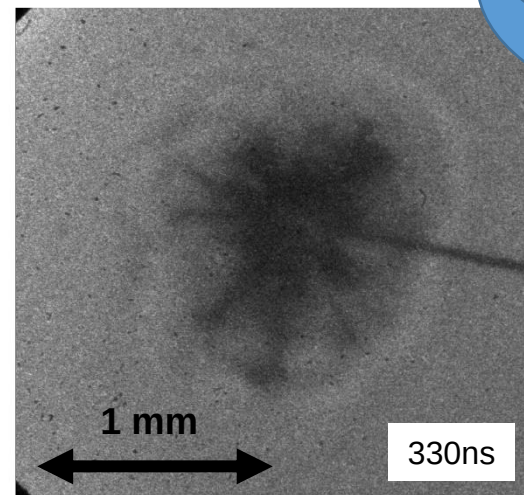
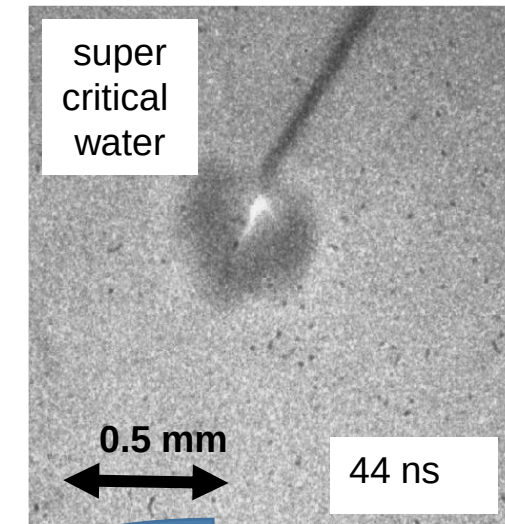
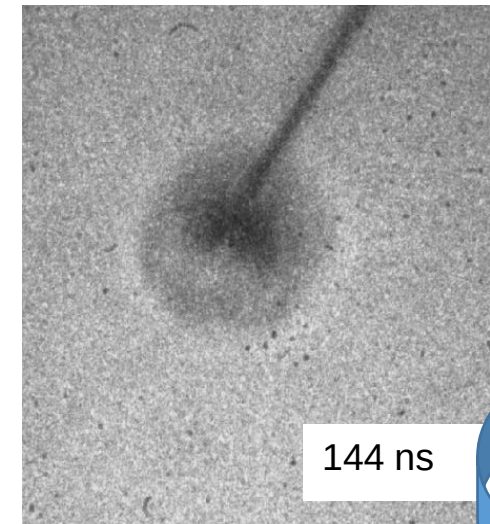
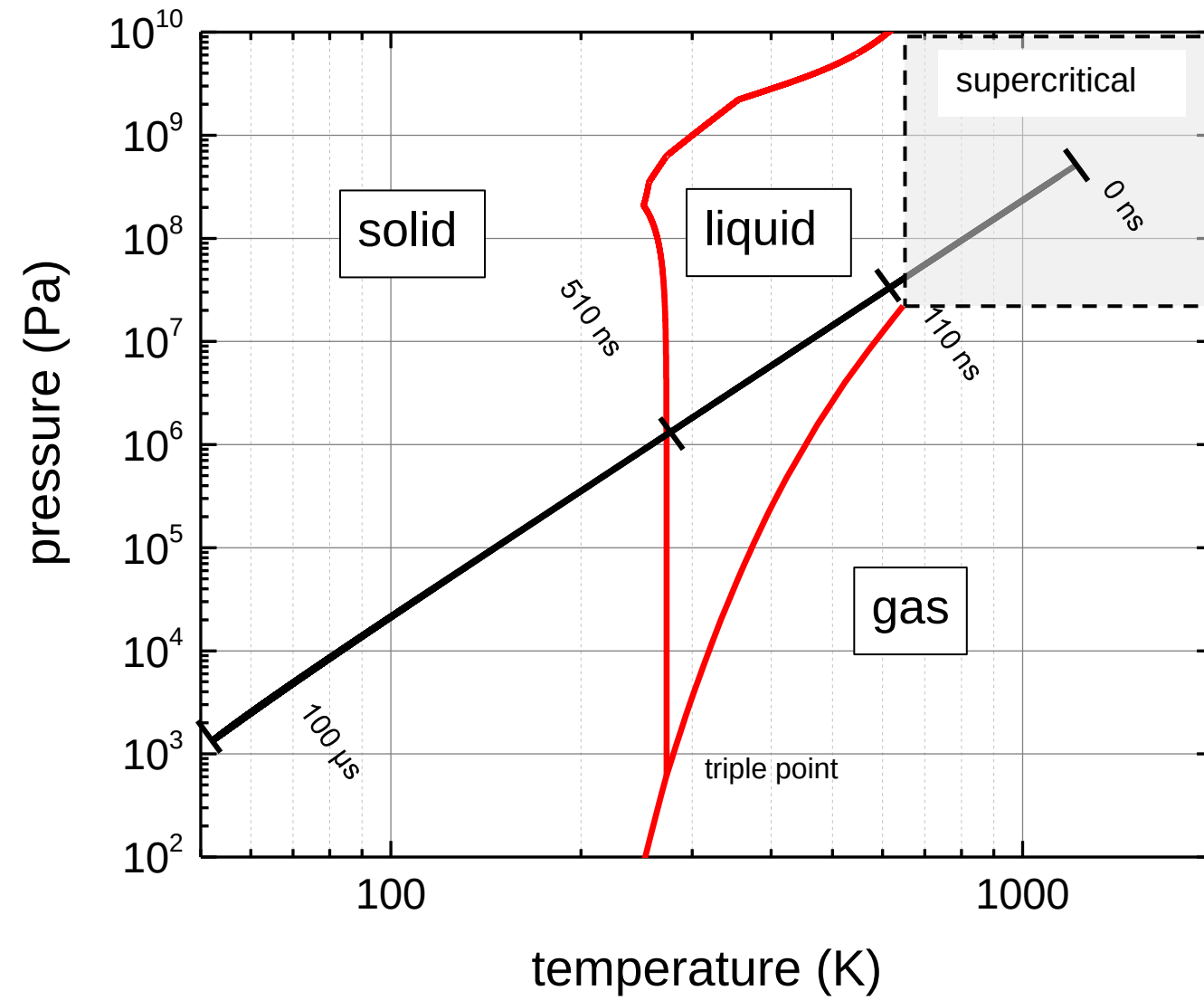
28 ns

gate 2ns

44 ns

gate 70ns

Transition of the water vapor in the bubble through the phase diagram of water



Solution for R(t) assuming a compressible liquid and condensation of vapor species

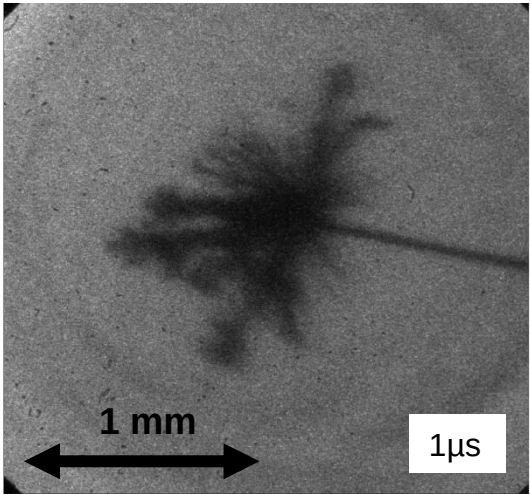
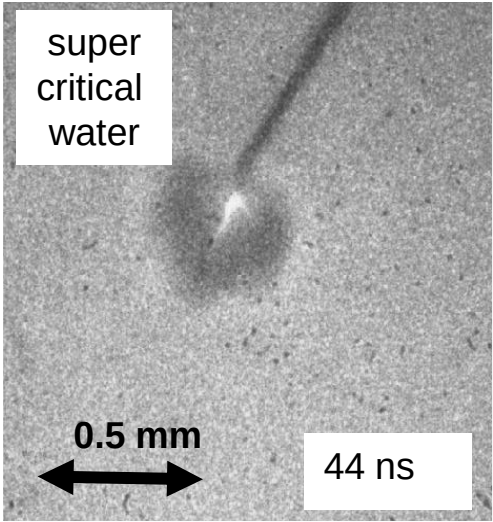
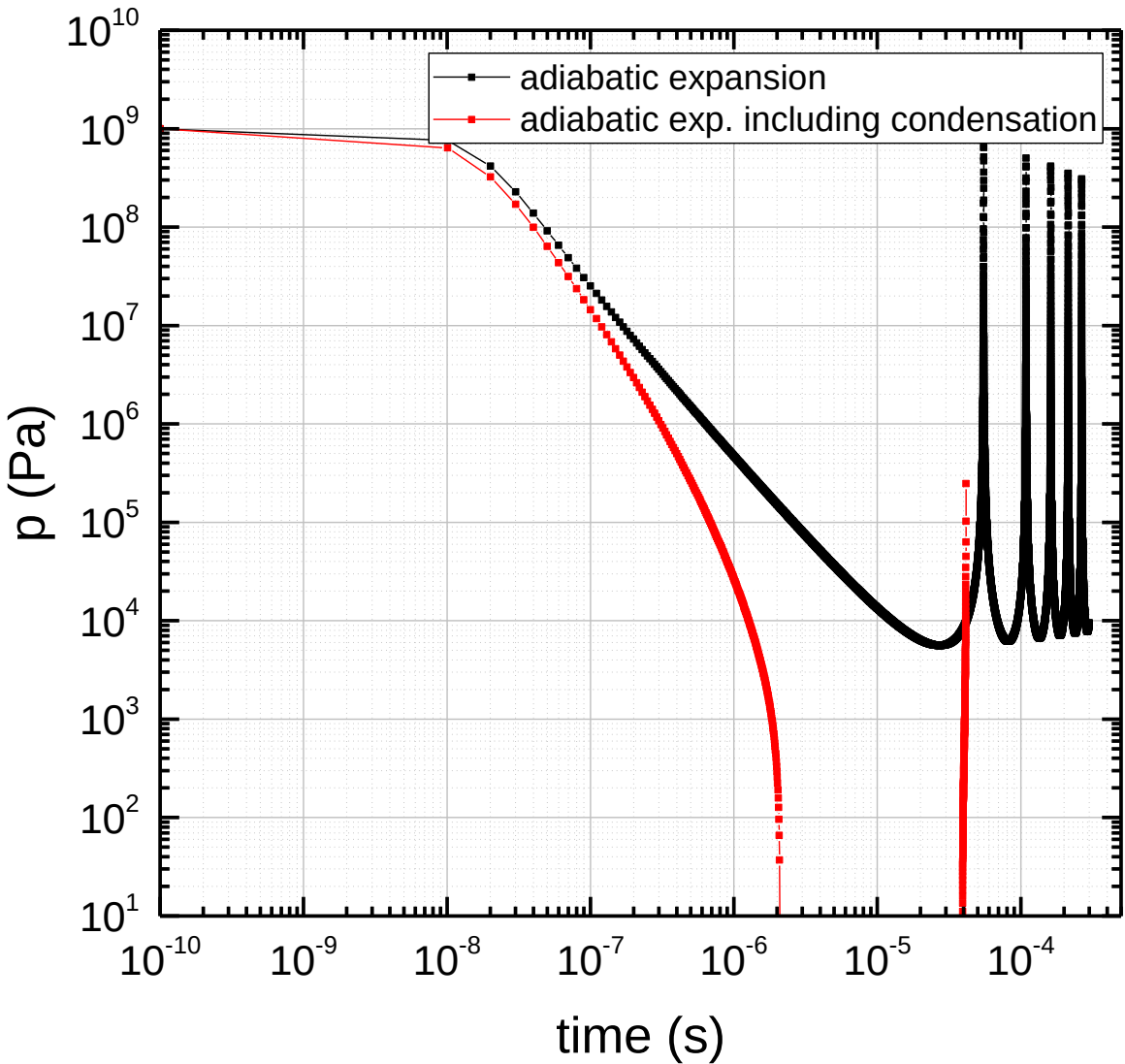
Balance between surface flux and volume loss depending on R,
 β =sticking coeff. = 1

$$\frac{1}{4}nv_{therm}4\pi R^2\beta = \frac{4\pi}{3}R^3n\frac{1}{\tau}$$

$$\tau = \frac{4R}{3v_{therm}\beta}$$

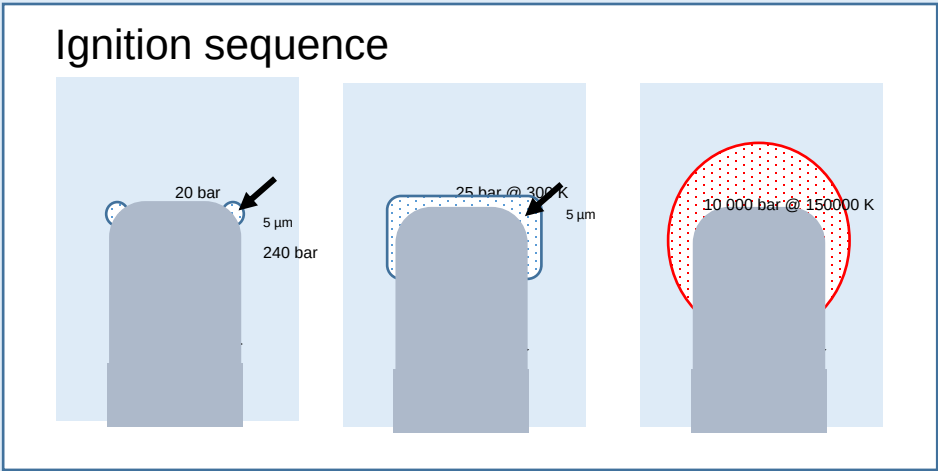
$$p_0 \rightarrow p_0 \exp\left(-\frac{t}{\tau}\right)$$

$$p(t) \rightarrow p_0 \exp\left(-\frac{t}{\tau}\right) \left(\frac{R_0}{R}\right)^{3\gamma}$$



Plasma in a bubble expansion

everything to scale



$r = 5 \mu\text{m}$
 $t = 1\text{ns}$

$r = 25 \mu\text{m}$
 $t = 10\text{ns}$

$r = 50 \mu\text{m}$
 $t = 100 \text{ ns}$

$r = 80 \mu\text{m}$
 $t = 200 \text{ ns}$

$r = 100 \mu\text{m}$
 $t = 400 \text{ ns}$

Ignition
plasma

supercrit.
vapor

re-heated

re-heated

re-heated

conden-
sation

$n_0=3 \cdot 10^{28} \text{ m}^{-3}$
 $n_e=3 \cdot 10^{28} \text{ m}^{-3}$
 $p=10^{11} \text{ Pa}$

$n_0=3 \cdot 10^{28} \text{ m}^{-3}$
 $p=5 \cdot 10^8 \text{ Pa}$
 $T=1200 \text{ K}$

$n_0=2.6 \cdot 10^{27} \text{ m}^{-3}$
 $n_e=10^{25} \text{ m}^{-3}$
 $p=2 \cdot 10^7 \text{ Pa}$
 $T=550 \text{ K}$

$n_0=1.6 \cdot 10^{27} \text{ m}^{-3}$
 $n_e=10^{23} \text{ m}^{-3}$
 $p=10^7 \text{ Pa}$
 $T=450 \text{ K}$

$n_0=2.8 \cdot 10^{26} \text{ m}^{-3}$
 $p=10^6 \text{ Pa}$
 $T=260 \text{ K}$

sound
wave

$r_{\text{max}}=600 \mu\text{m}$
 $t=60 \mu\text{s}$

$r_{\text{min}}=5 \mu\text{m}$
 $t=100 \mu\text{s}$

gas

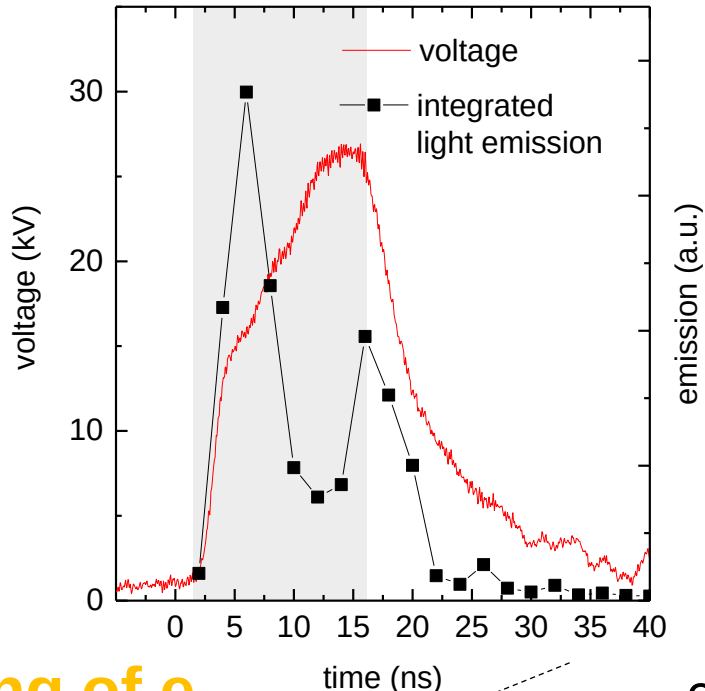
collapse

$n_0=1.4 \cdot 10^{24} \text{ m}^{-3}$
 $p=10^3 \text{ Pa}$
 $T=50 \text{ K}$

Field emission effects

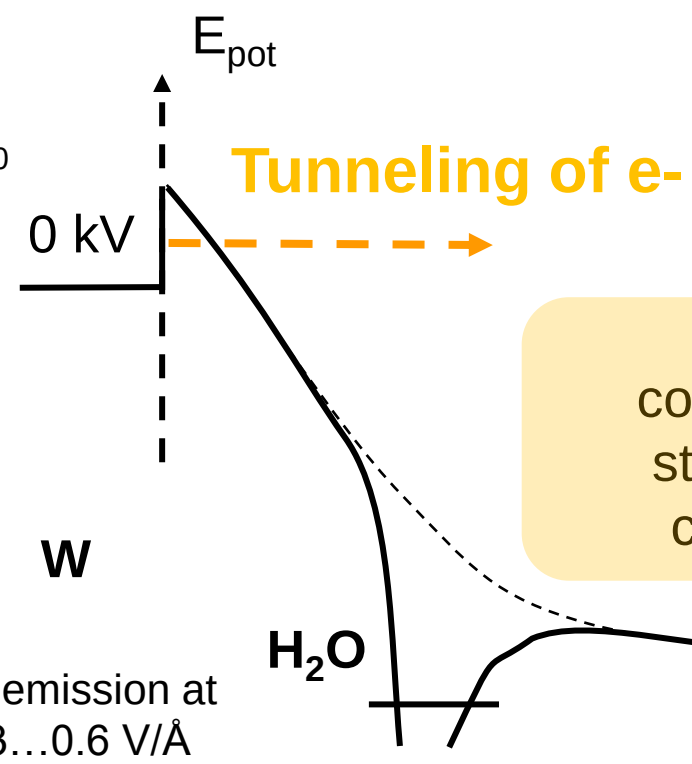
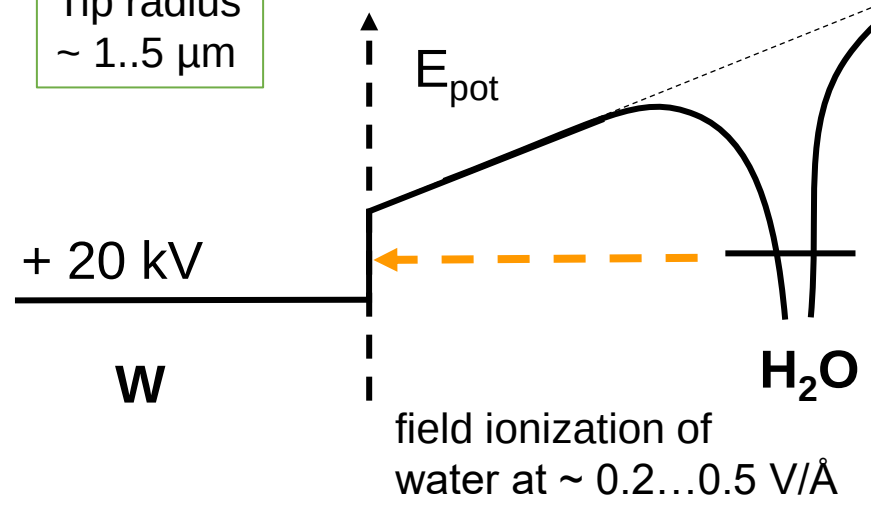


Start of the pulse
water
is polarized
Field ionization

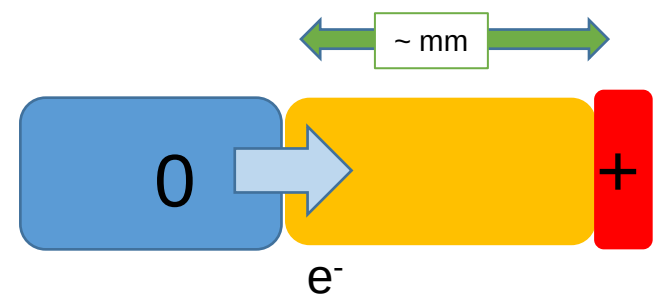


Tunneling of e-

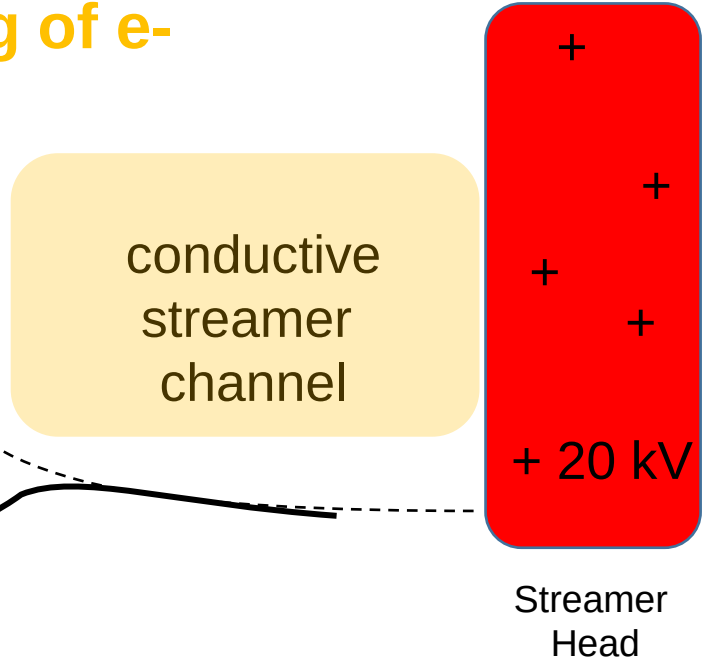
Tip radius
~ 1.5 μm



field emission at
~ 0.3...0.6 V/Å



Voltage stops,
Field emission
electron flow reverses
attracted to positive
streamer head

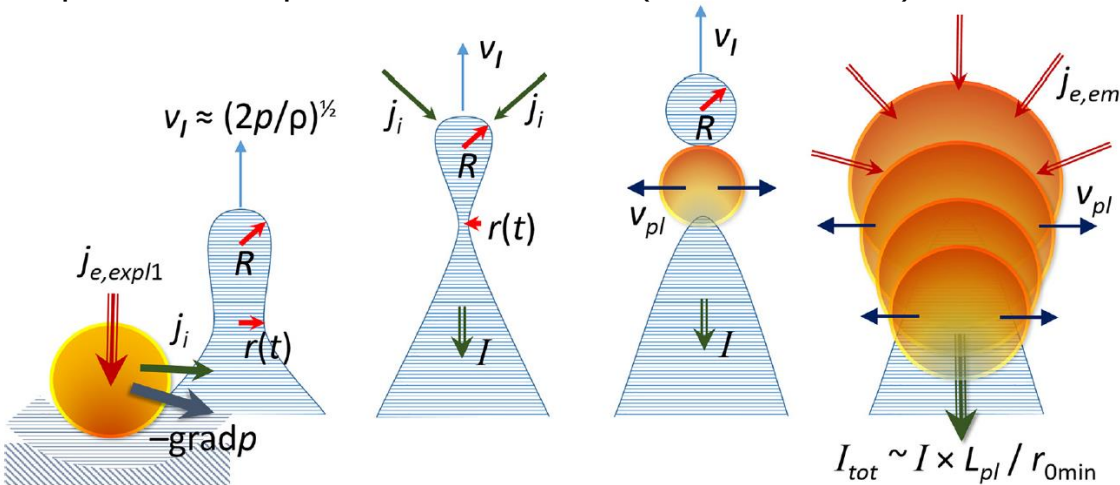


Nature of the $1/\lambda^x$ background in emission

Possible sources for $1/\lambda^x$ background

- H_2O , H_2 recombination background (300...500 nm, no part down to 250 nm)
- $1/\lambda^2$ recombination radiation free-free, bound-free
- $1/\lambda^5$ long wavelength part of the emission of a hot cathode spot

Example cathode spot in vacuum arcs T (15000...2000 K)

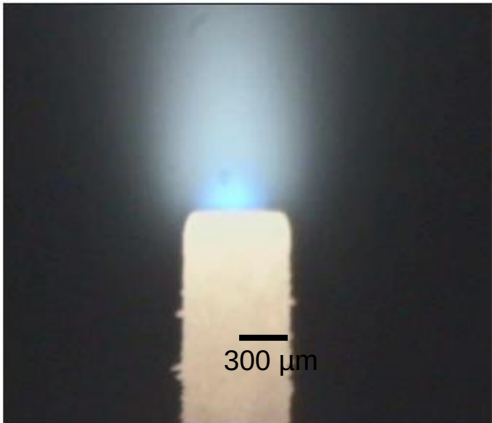


initial
droplet $R=1\mu\text{m}$

Coulomb-explosion of the neck
leads to metal plasma
(10 μm diameter, $n_e \sim 10^{26} \text{ m}^{-3}$,)

Tsventoukh,
Phys. Plasmas 25, 53504 (2018)

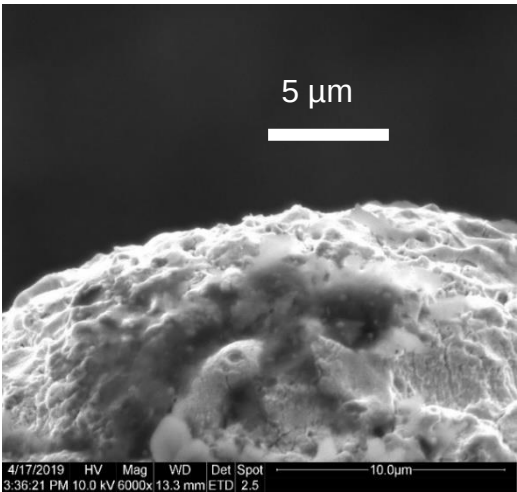
Example cathode spots
in arc lamps

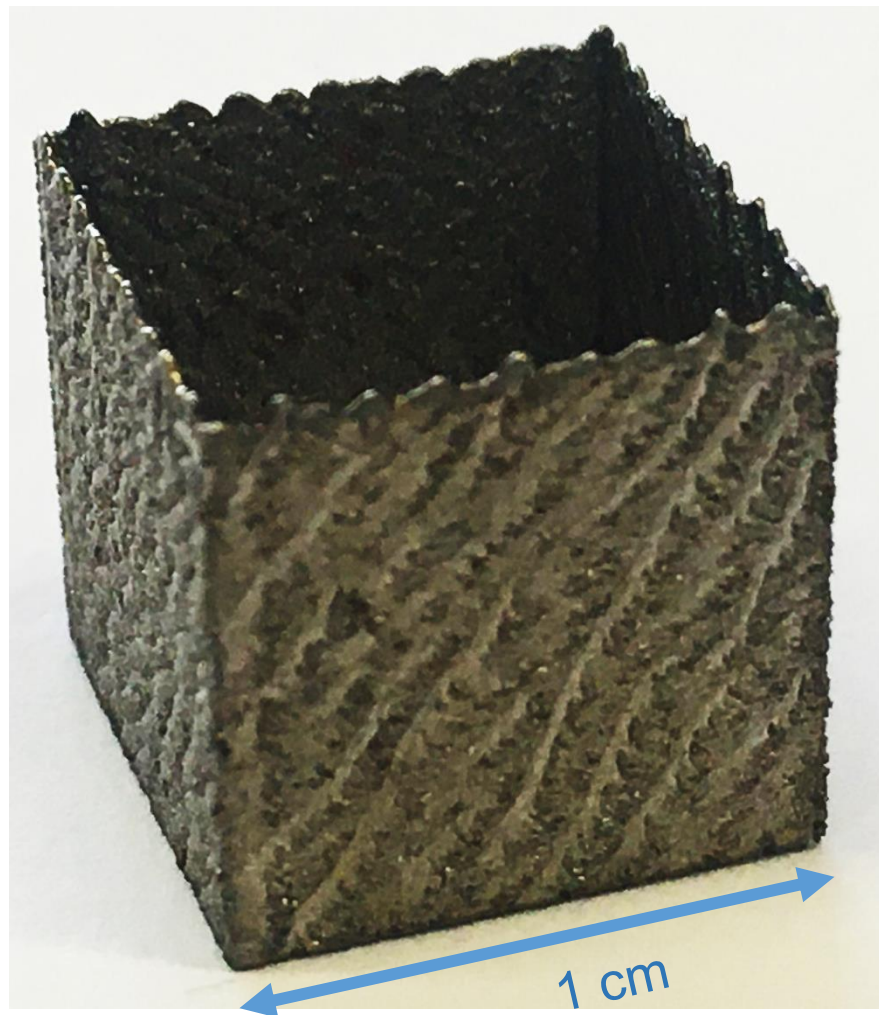


(d) $i_{\text{arc}} = 15.0 \text{ A}$

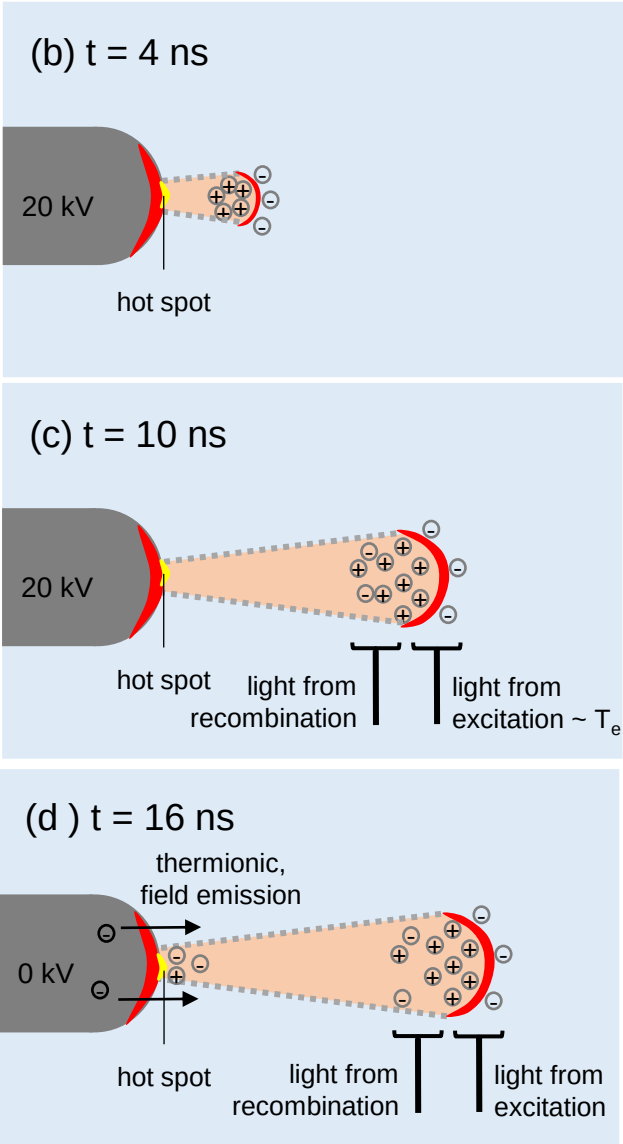
A. Bergner et al. PSST 23, 054005 (2014)

Cathode spots at W tips

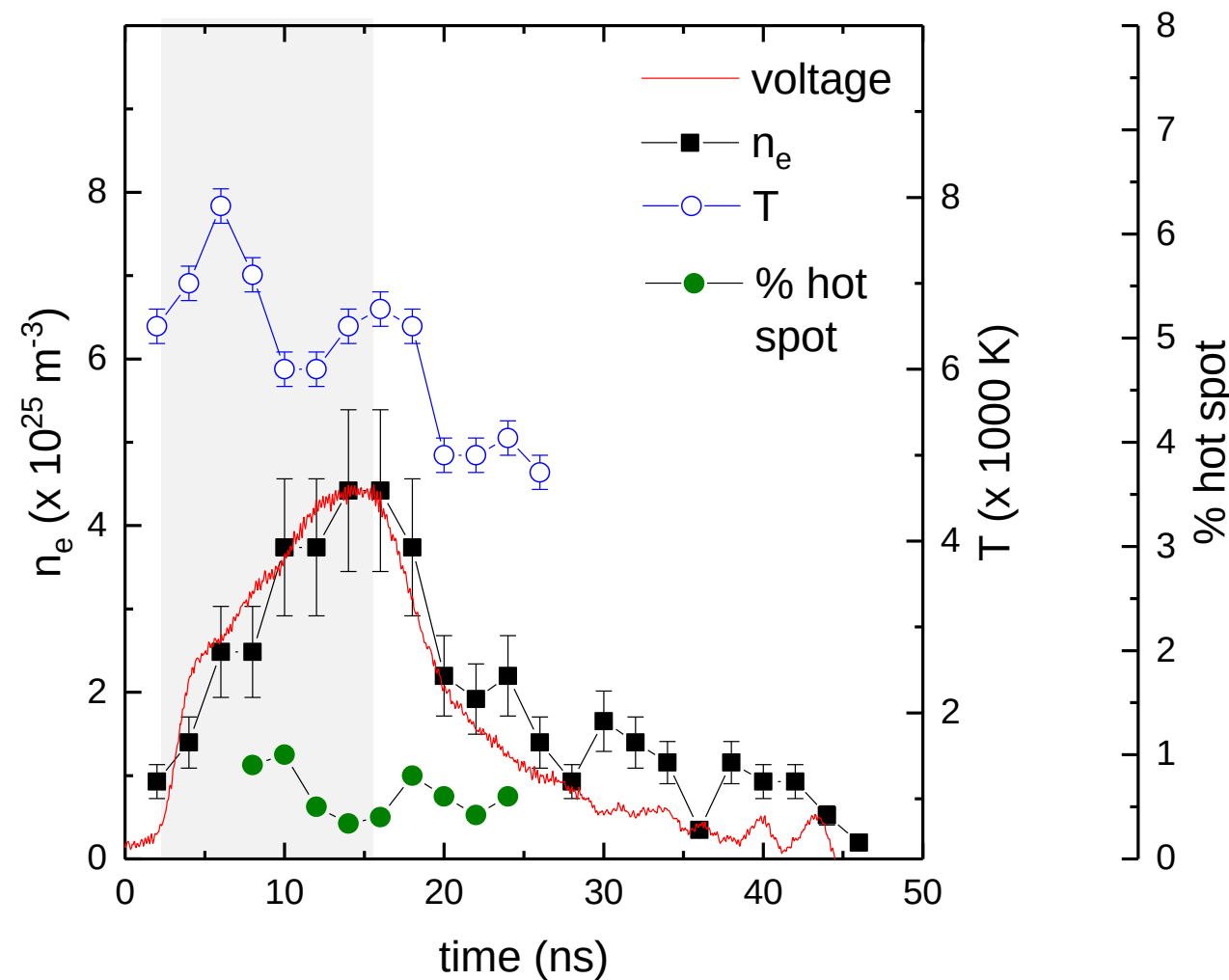




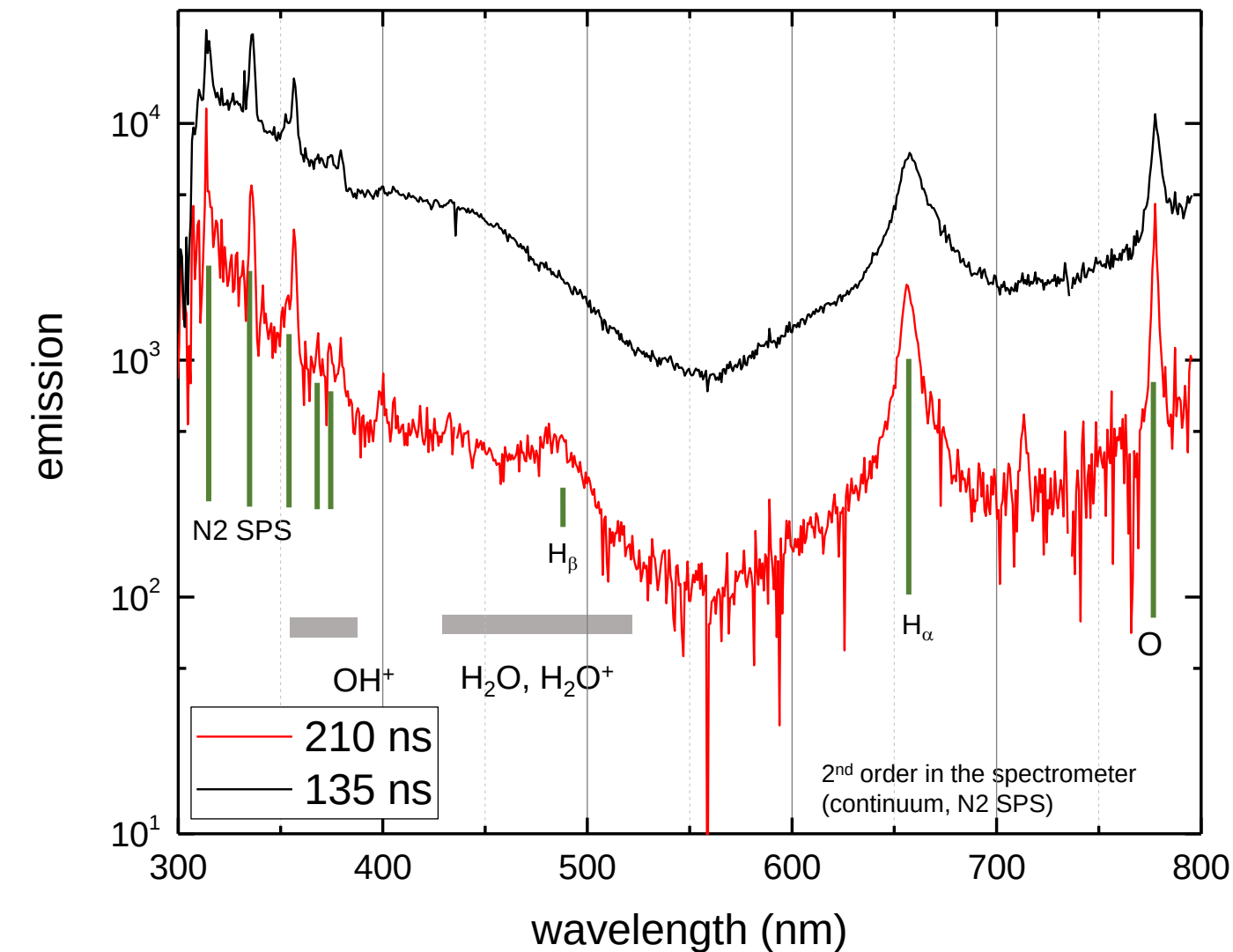
Line emission – H alpha from ionization region of Hydrogen Balmer Series



Temperature variation

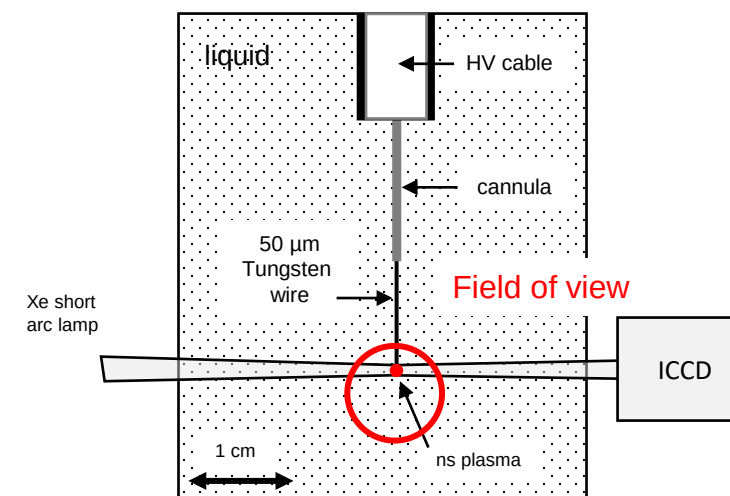
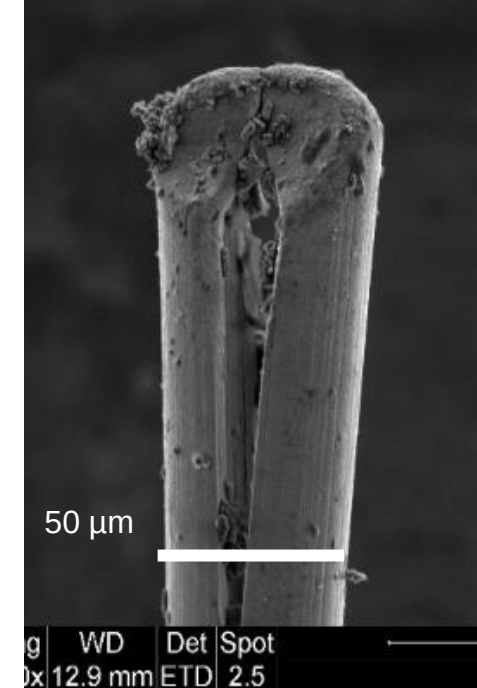


Temperatures from N2 SPS as thermometer for the later stages



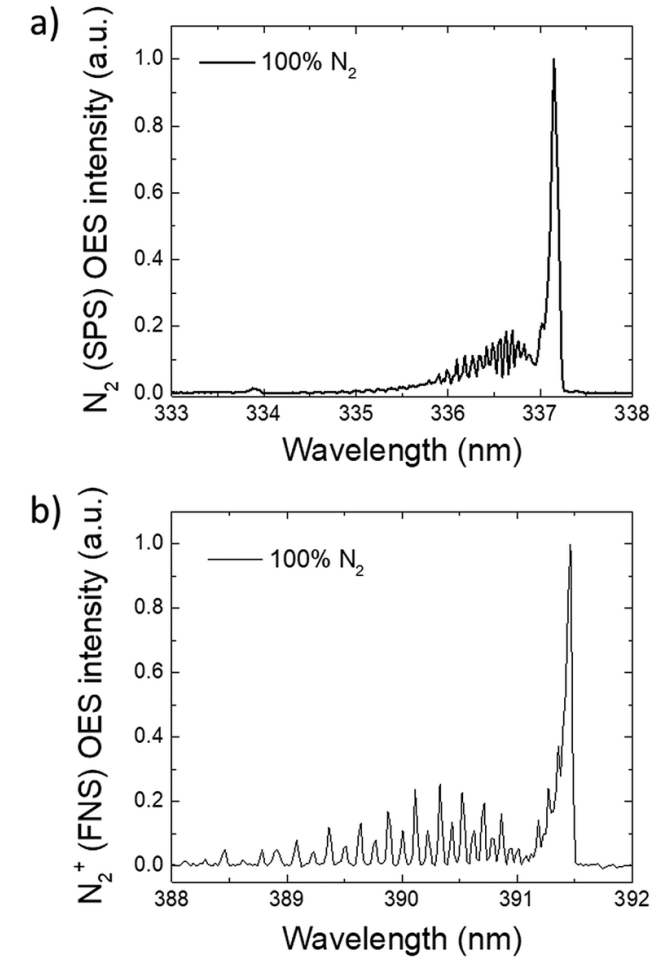
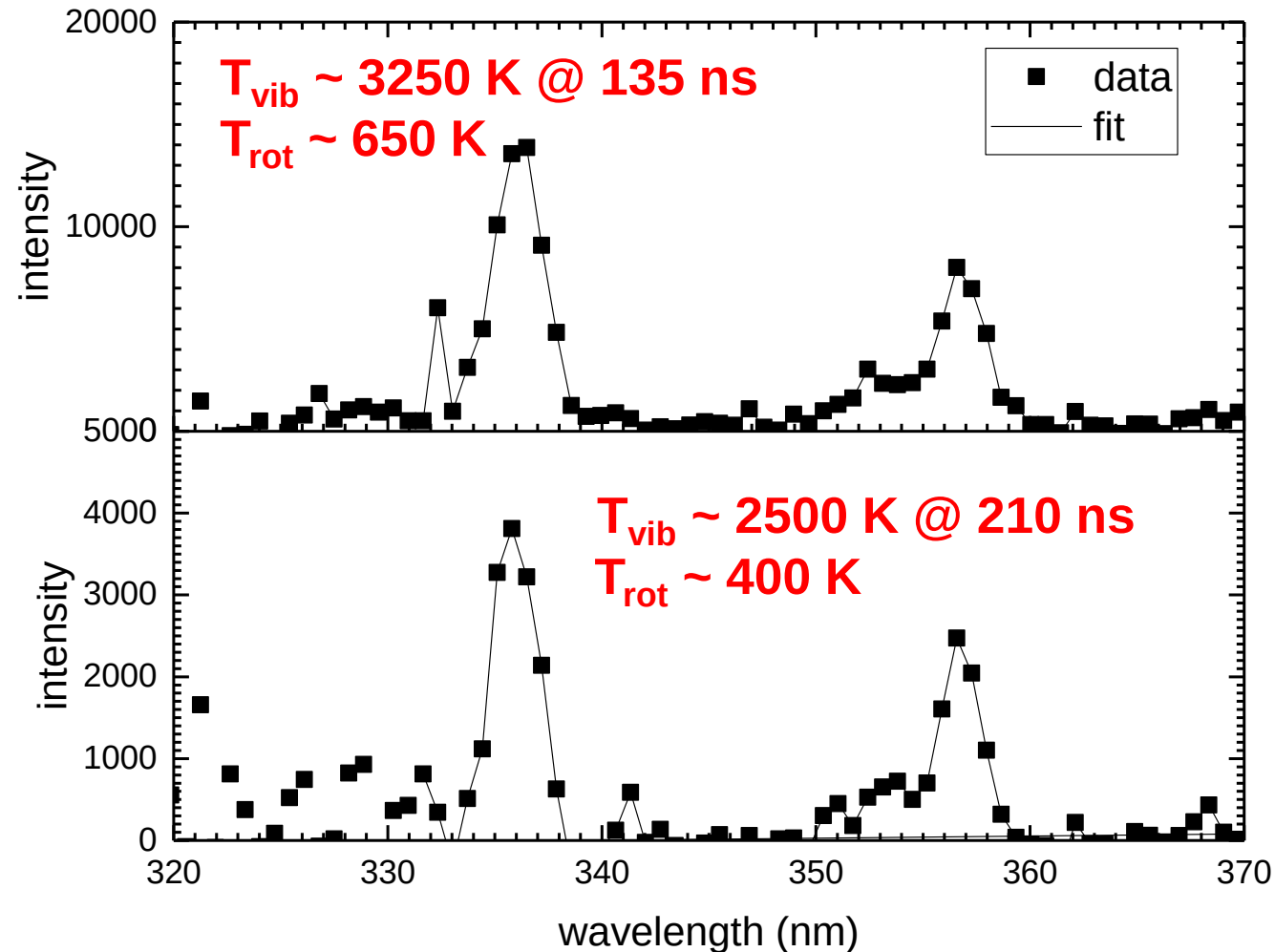
Line identification

- H_α, H_β
- O 777
- N2 SPS form N2 intrusion
- Bands of OH, H2O hard to detect



Temperatures from N₂ SPS as thermometer for the later stages

For 20 kV Experiment



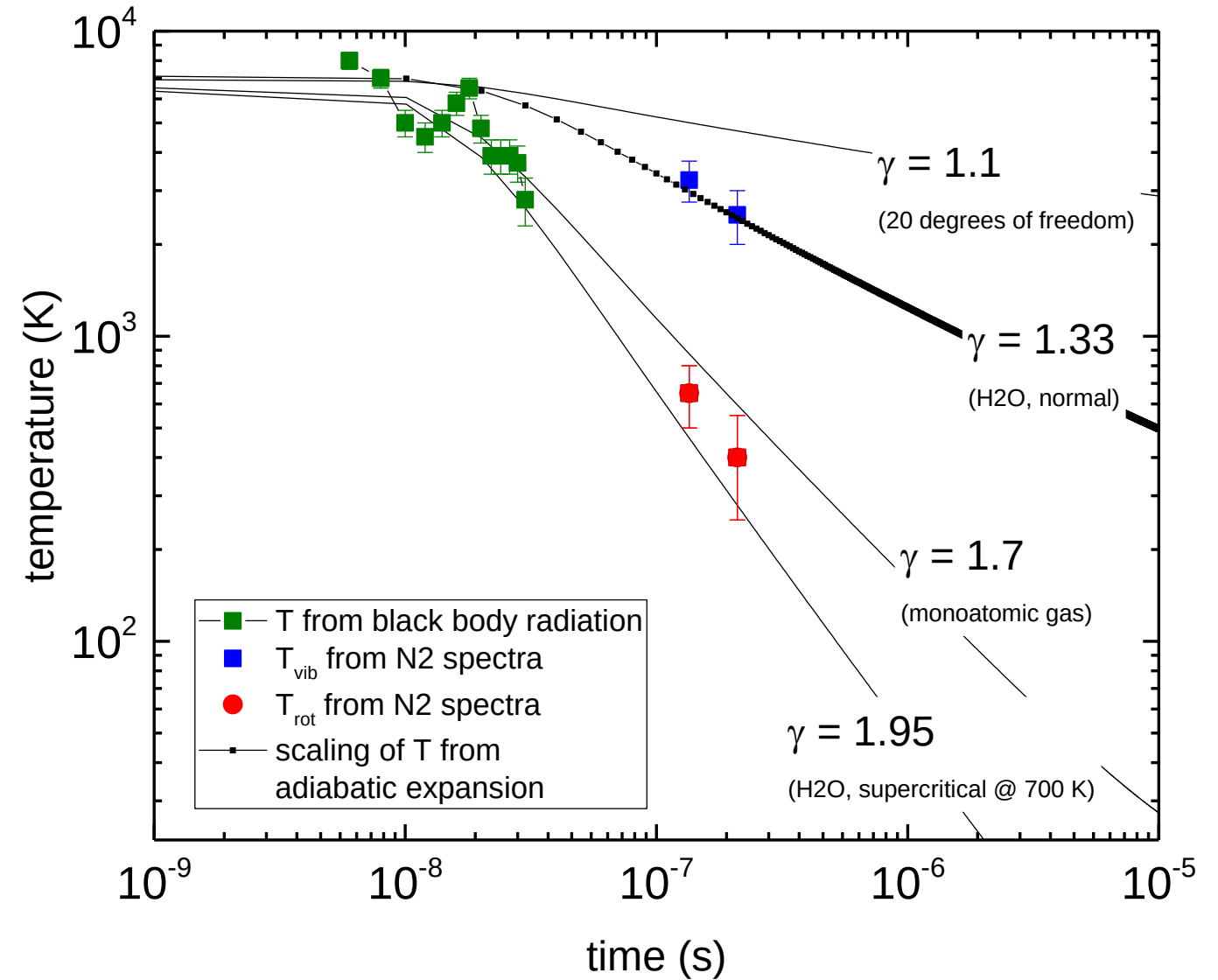
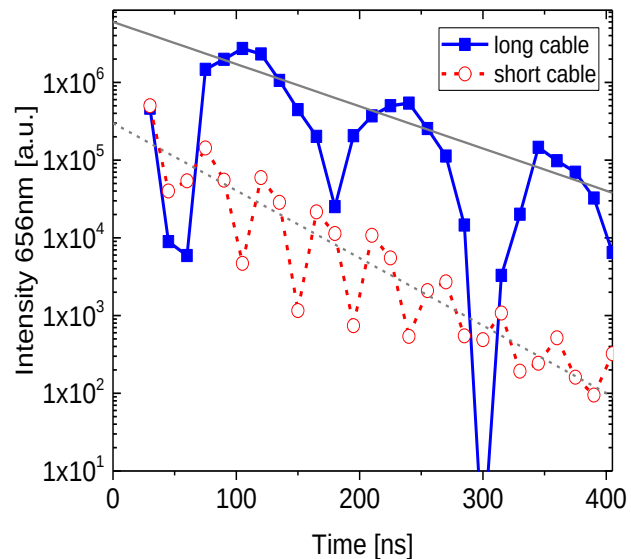
From Girard et al. PCCP 20, 2198 (2018)

Temperatures from spectroscopies

T from cavitation theory

Cooling during expansion depends on
VV, VT, VR relaxation times.

Usually T_{rot} decouples from T_{vib}
In chemical non-equilibrium
expanding flows



Non-equilibrium in expanding ns plasmas

Rocket
Chemical
Hypersonic

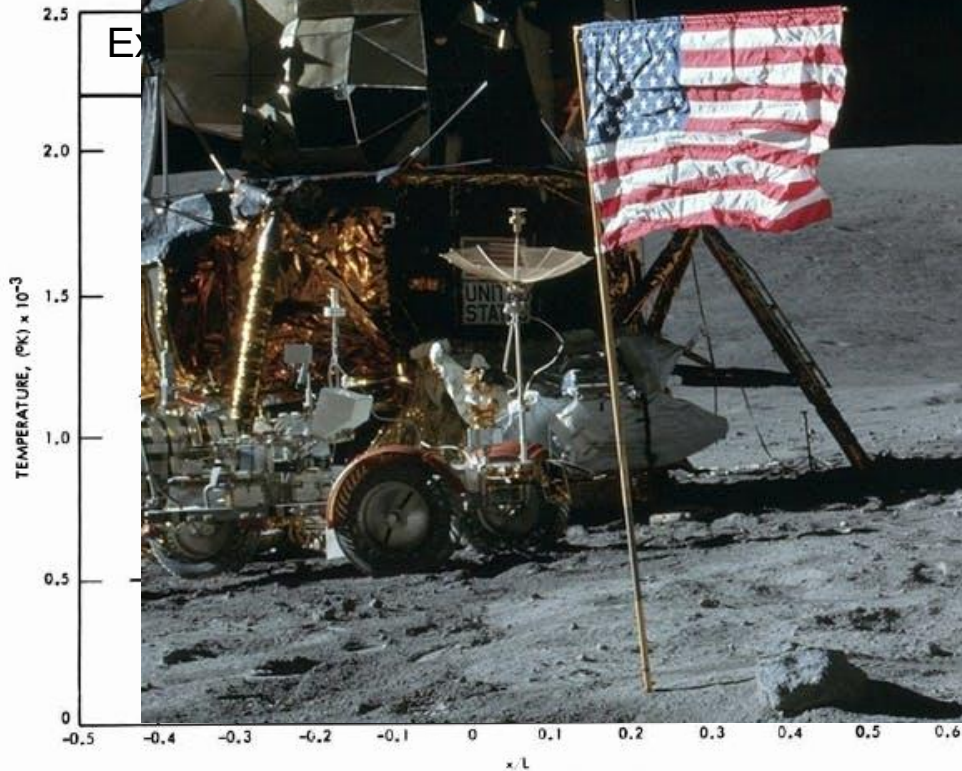
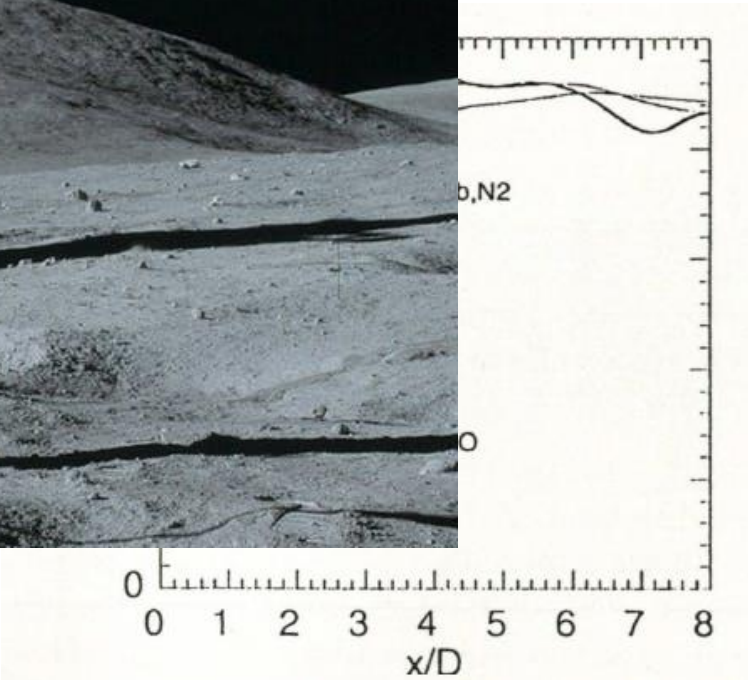
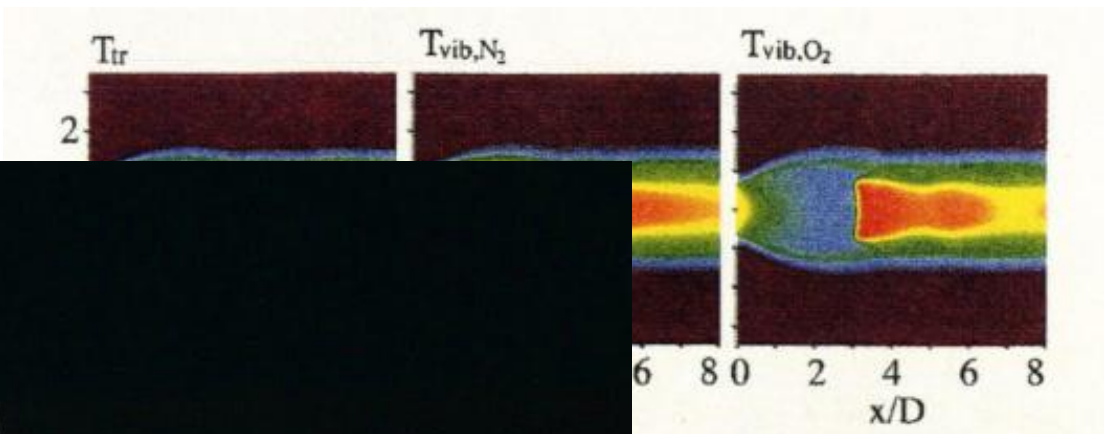


FIG. 7 STEADY-STATE T_{vib} AND T_{trans} DISTRIBUTIONS FOR THE NONEQUILIBRIUM EXPANSION OF N_2 ; COMPARISON OF THE PRESENT TIME-DEPENDENT ANALYSIS WITH THE STEADY-FLOW ANALYSIS OF REFERENCE 7.

J. D. Anderson, Report Naval Ordnance Labatory (1969)



M. Nichida, M. Matsumoto, Verlag d. Zeitung f. Naturforschung 0932-0784 (1997)

Solution for R(t) assuming a compressible liquid

$$r \frac{Dh}{Dt} + ru \frac{Du}{Dt} + (c + u) \left(h + \frac{u^2}{2} \right) + rc \frac{\partial h}{\partial r} + rcu \frac{\partial u}{\partial r} = 0$$

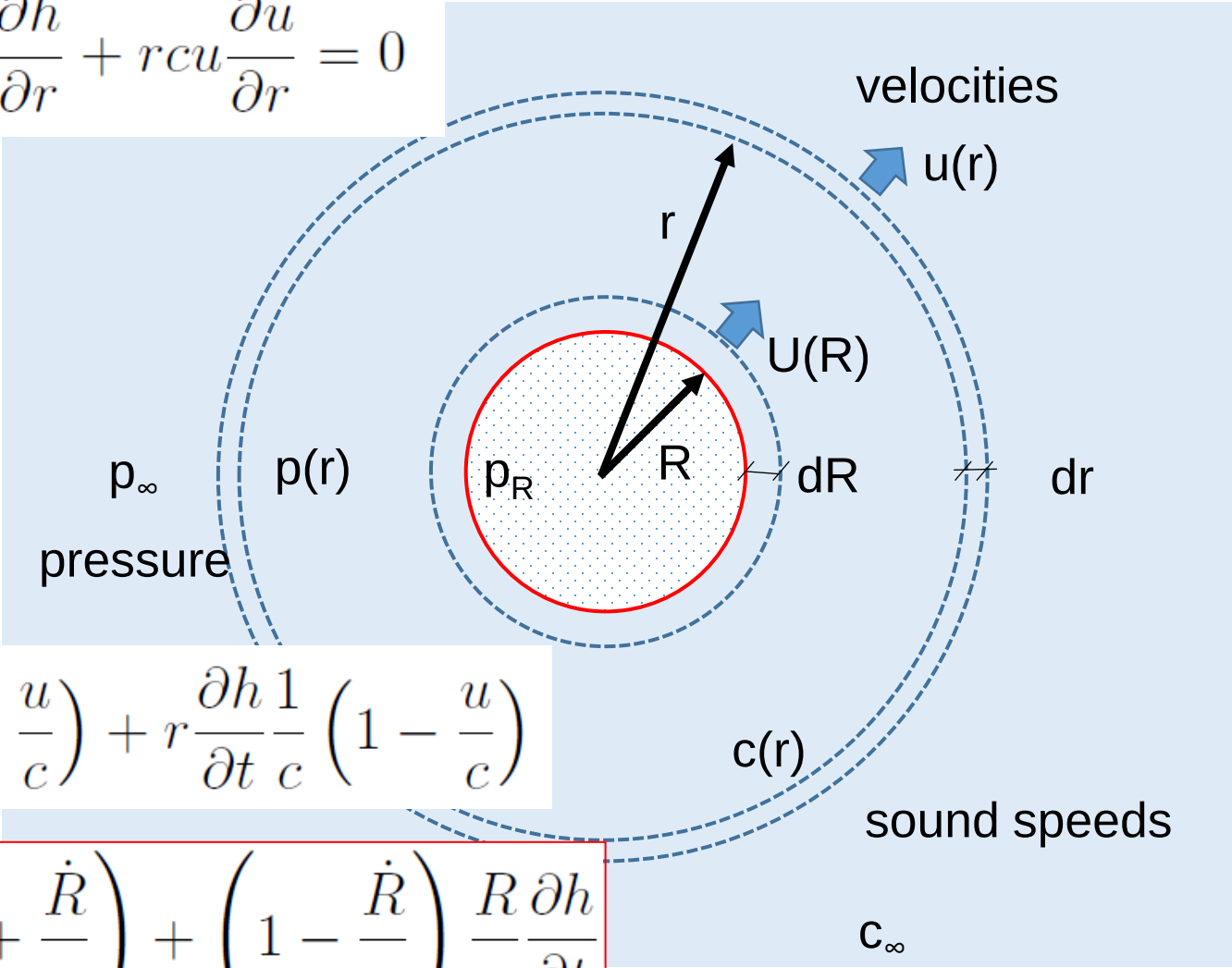
with momentum and mass conservation

$$\frac{Du}{Dt} = - \frac{\partial h}{\partial r}$$

$$\frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 u \right) = - \frac{1}{\rho} \frac{d\rho}{dt}$$

$$r \frac{Du}{Dt} \left(1 - \frac{u}{c} \right) + \frac{3}{2} u^2 \left(1 - \frac{u}{3c} \right) = h \left(1 + \frac{u}{c} \right) + r \frac{\partial h}{\partial t} \frac{1}{c} \left(1 - \frac{u}{c} \right)$$

$$R \ddot{R} \left(1 - \frac{\dot{R}}{c} \right) + \frac{3}{2} \dot{R}^2 \left(1 - \frac{\dot{R}}{3c} \right) = h \left(1 + \frac{\dot{R}}{c} \right) + \left(1 - \frac{\dot{R}}{c} \right) \frac{R}{c} \frac{\partial h}{\partial t}$$



Solution for $R(t)$ assuming a compressible liquid

momentum balance equation (no Navier Stokes)

$$\frac{\partial}{\partial t} \left(-\vec{\nabla} \phi \right) + (\vec{u} \cdot \vec{\nabla}) \vec{u} = -\frac{\nabla p}{\rho}$$

Integrate over r

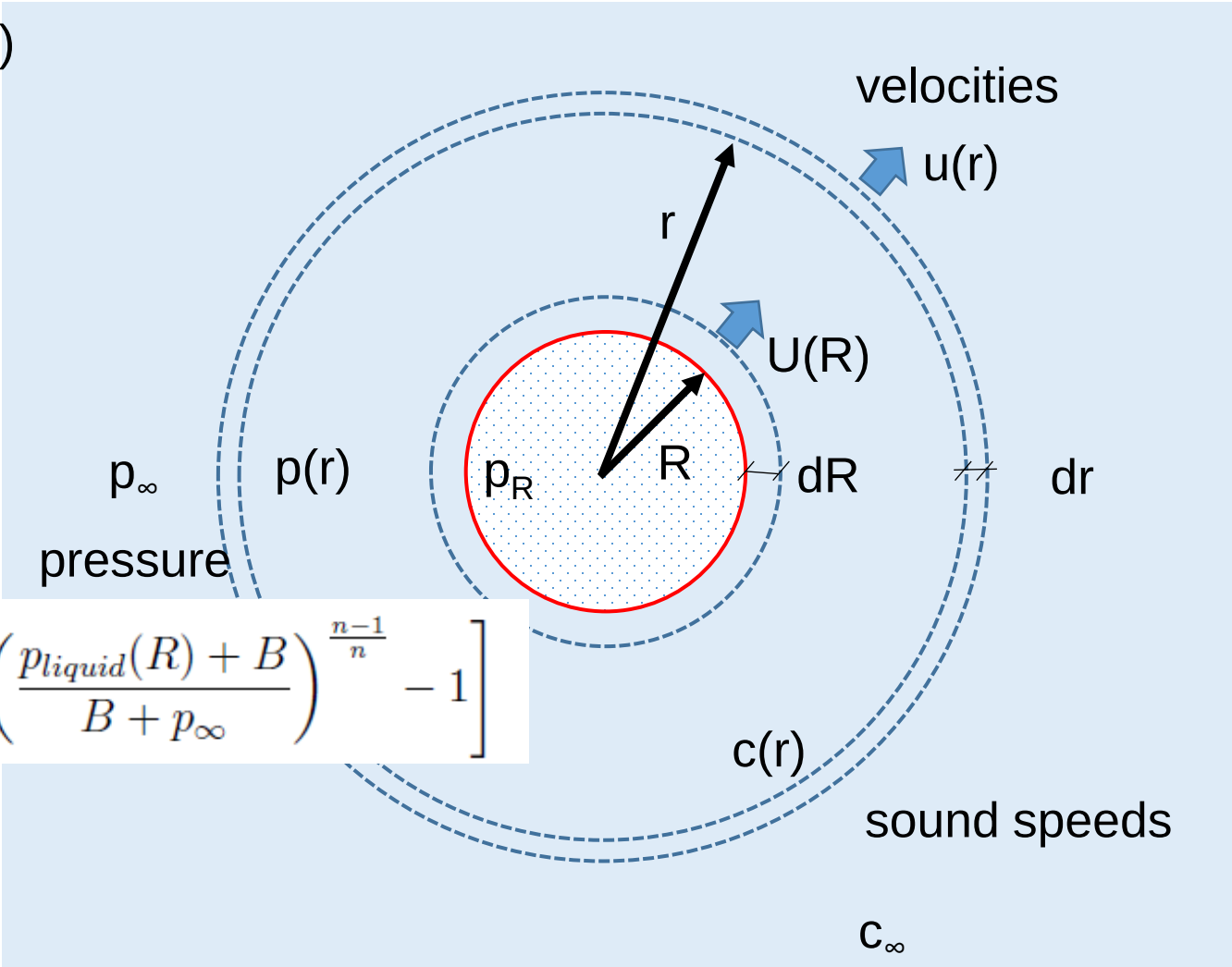
$$-\frac{\partial \phi}{\partial t} + \frac{1}{2} \vec{u}^2 = \int_{p_\infty}^{p(r)} -\frac{dp}{\rho}$$

definition enthalpy

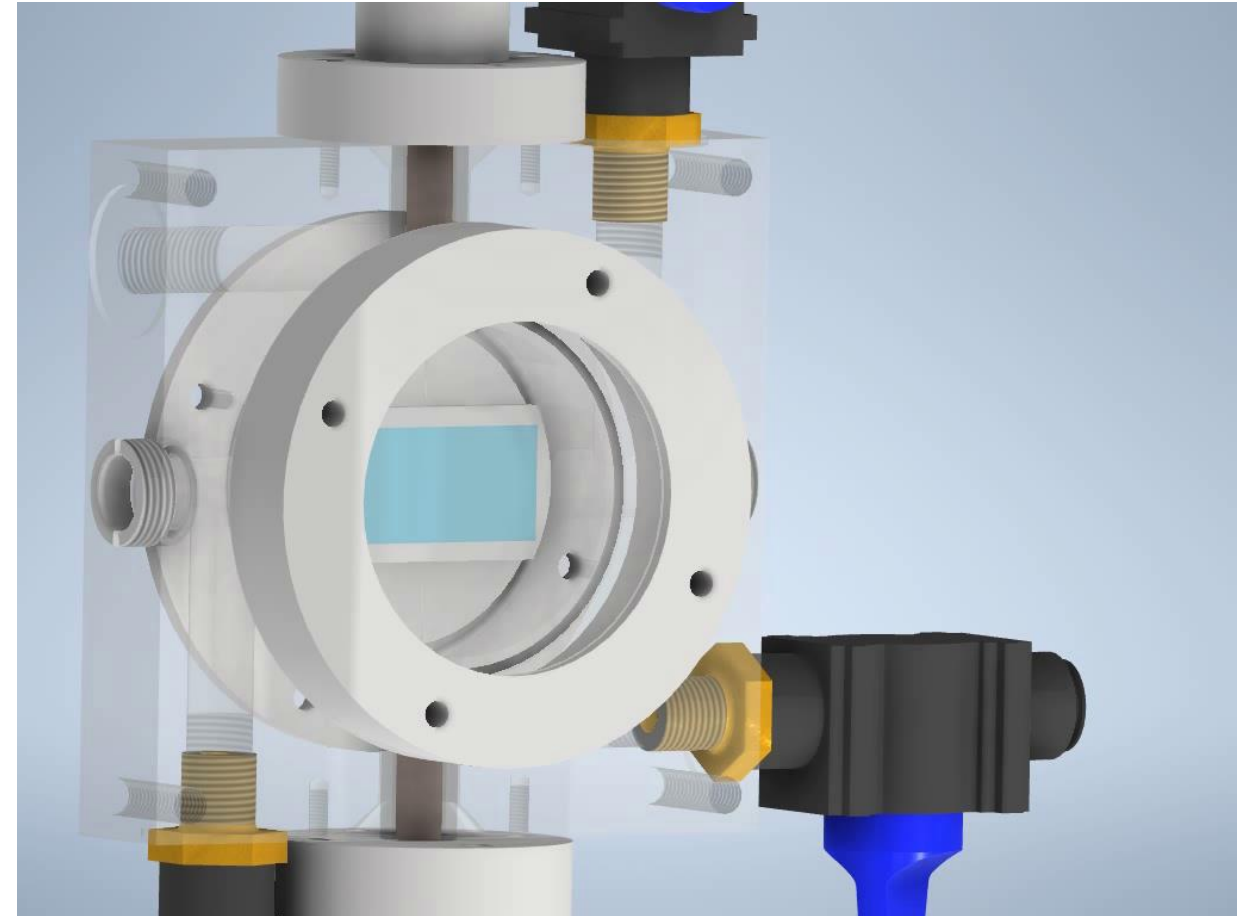
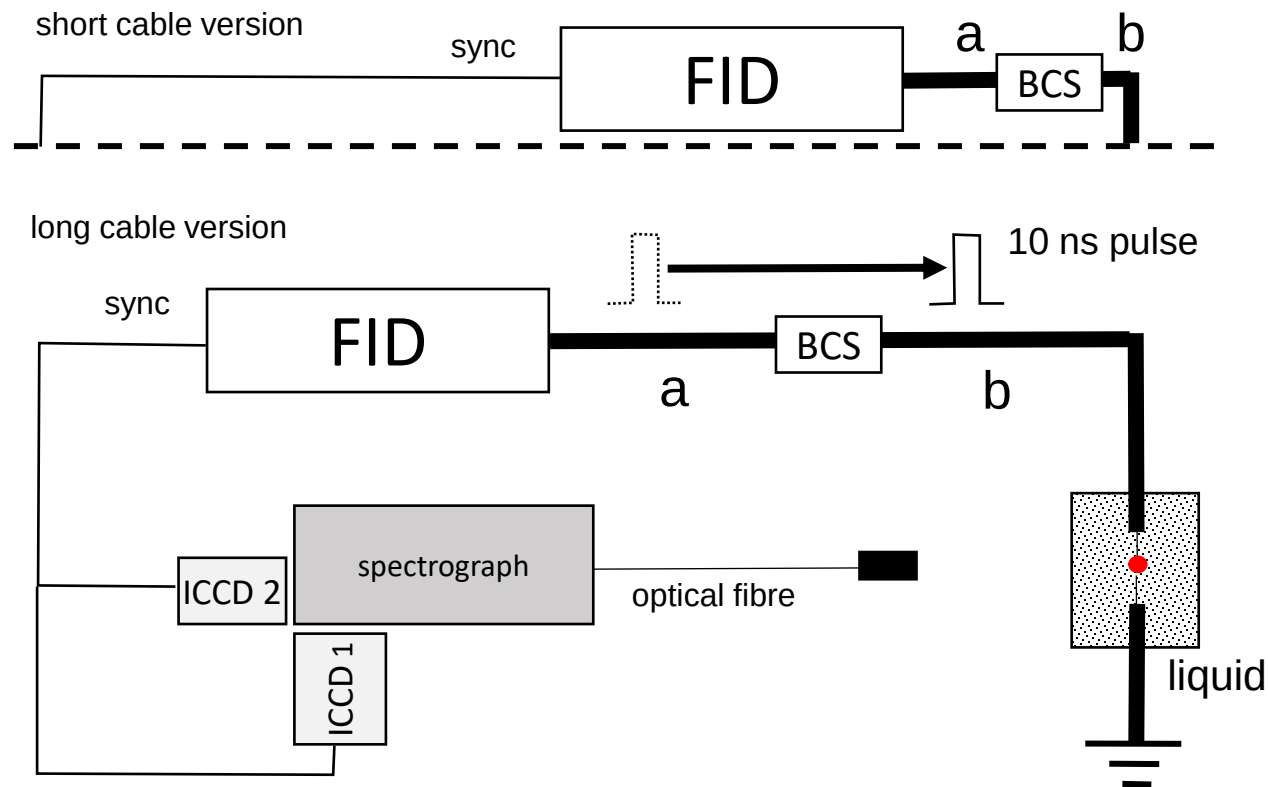
$$h = \int_{p_\infty}^{p(r)} -\frac{dp}{\rho} \quad h = \frac{n}{n-1} \frac{1}{\rho_0} (B + p_\infty) \left[\left(\frac{p_{liquid}(R) + B}{B + p_\infty} \right)^{\frac{n-1}{n}} - 1 \right]$$

results in Bernoulli equation

$$\frac{\partial \phi}{\partial t} = h + \frac{1}{2} \vec{u}^2$$



Example 2: Plasma Chemistry in liquids – example H_2O_2 generation



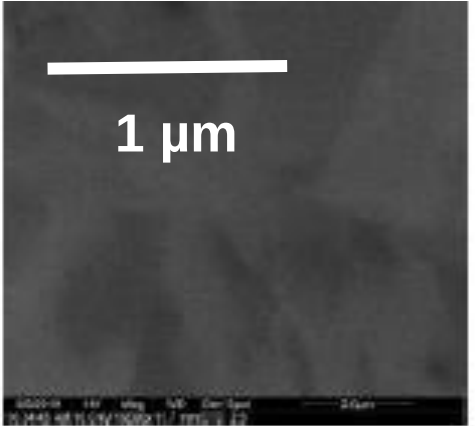
- 10 ns pulses, 14...30 kV, distilled water
- Shadowgraphy 2 ns ... 70 ns gate widths
- Optical emission spectroscopy with 2ns and 30 ns gate time

Nanosecond plasma based recovery of CuO nanocubes at copper electrodes

Creation of Cu-nanocubes possible, if

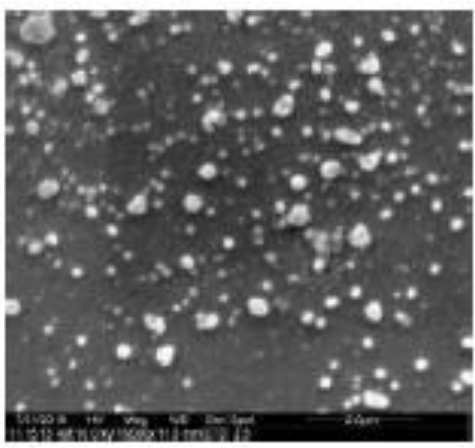
- no direct current to the sample, reduction of the oxide, plasma electrode distance to the sample important
- Cl necessary as nucleation sites
- Competition between oxidation due to H_2O_2 , OH and reduction by H, e^-

distilled water

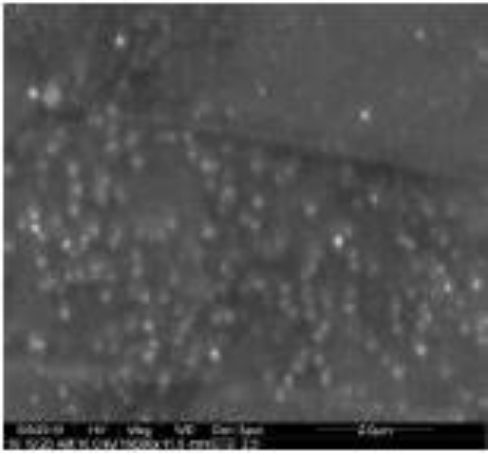


20 kV

dist. Water + 0.0035M KCl

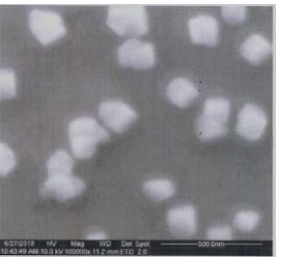
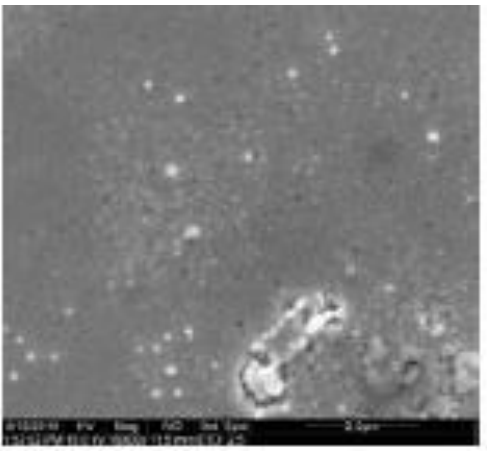


distilled water



26 kV

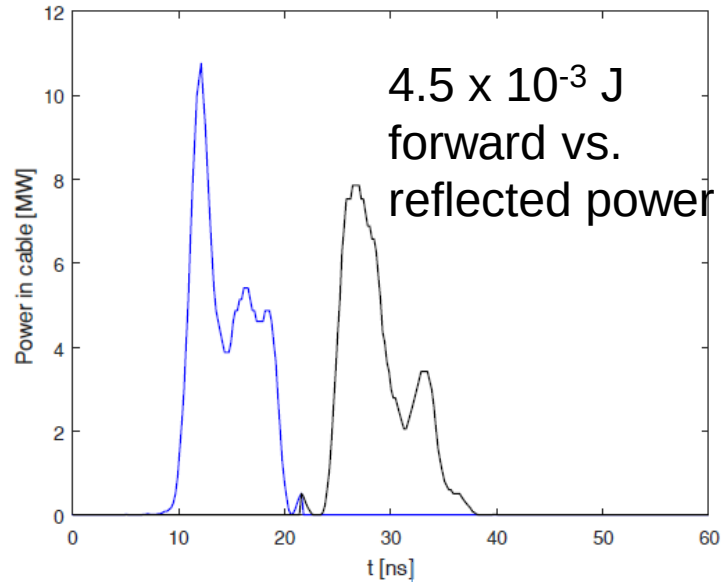
dist. Water + 0.0035M KCl



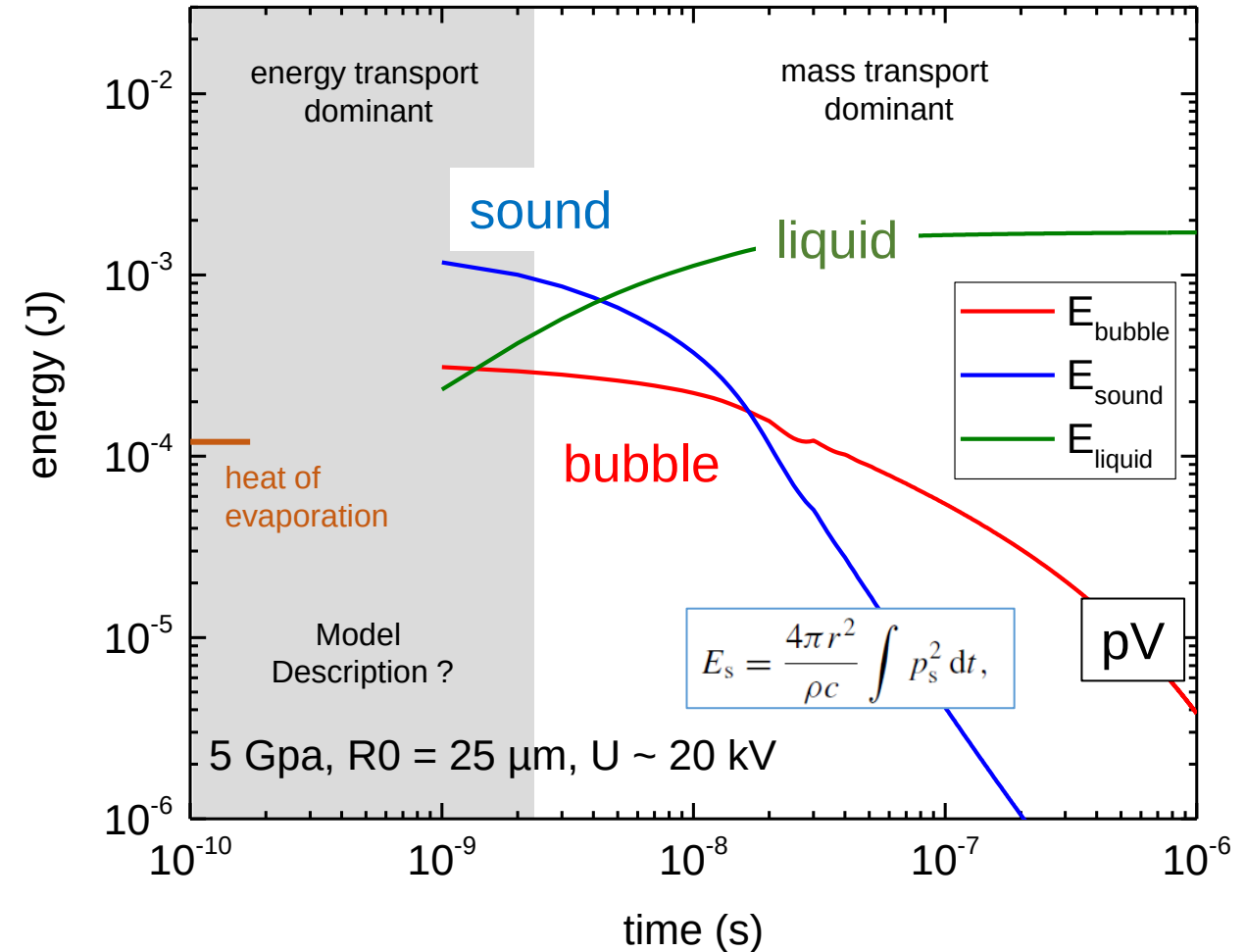
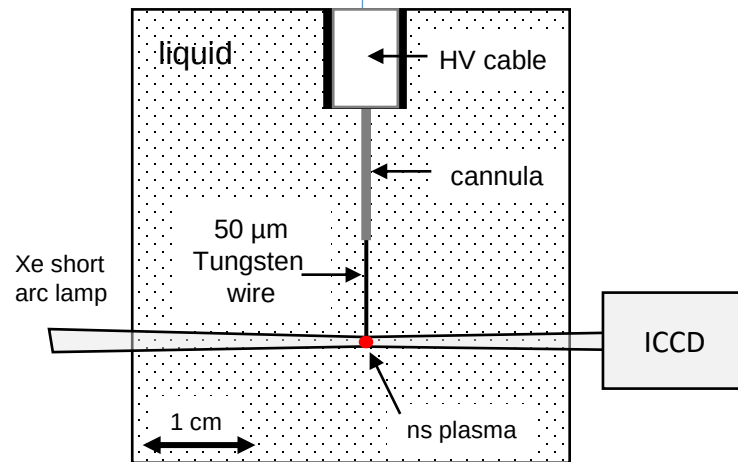
P. Grosse, B. Roldan et al.

Reference plasma based low pressure creation of CuO nanocubes

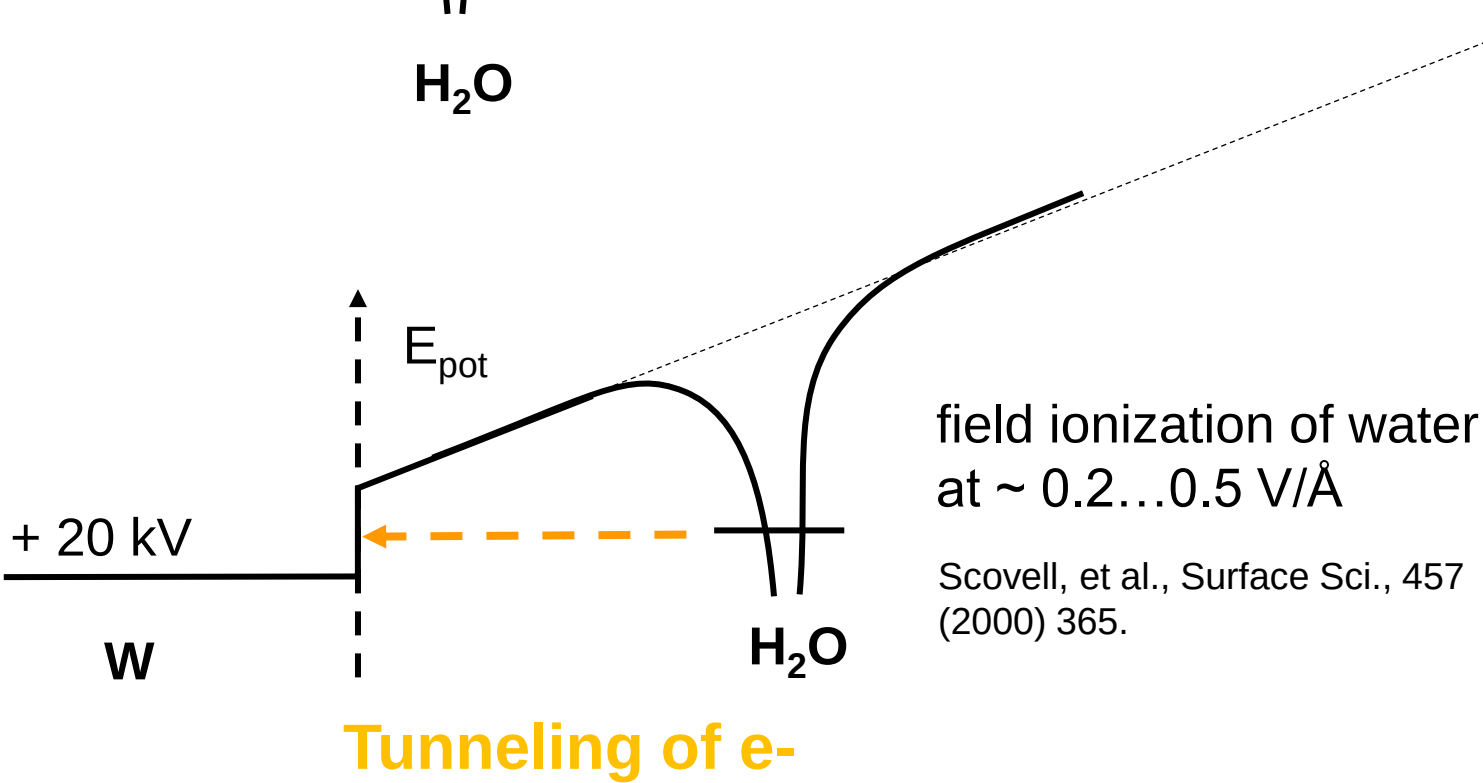
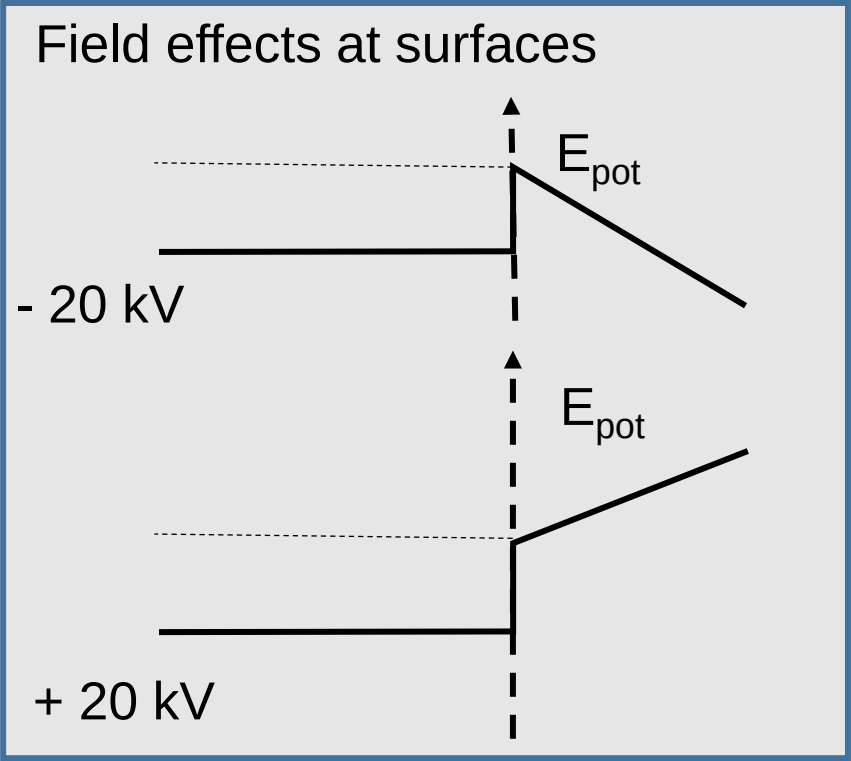
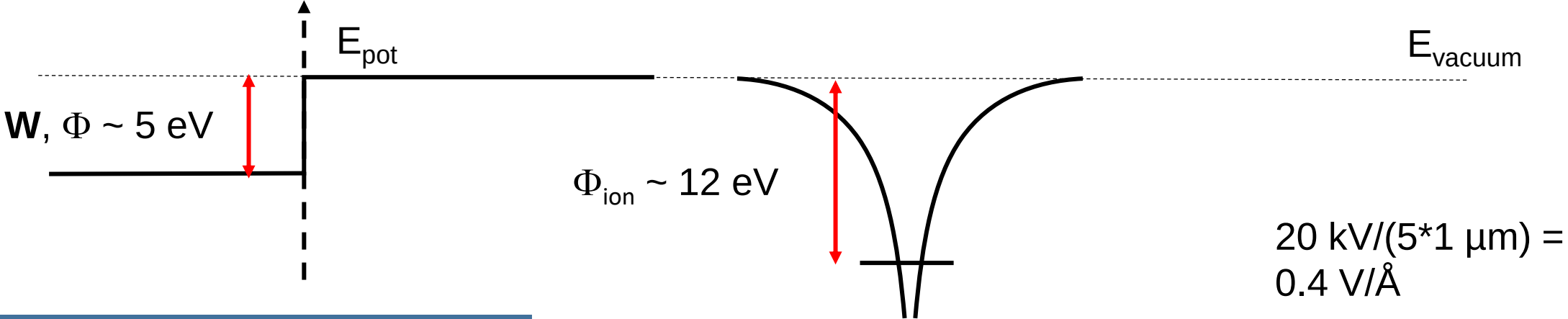
Dissipated energy during plasma ignition within the first 10 ns – comparison to experiments



In ns plasmas at very high initial pressure, most of the energy is transferred to the sound wave



Field emission effects



Streamer velocities in distilled water

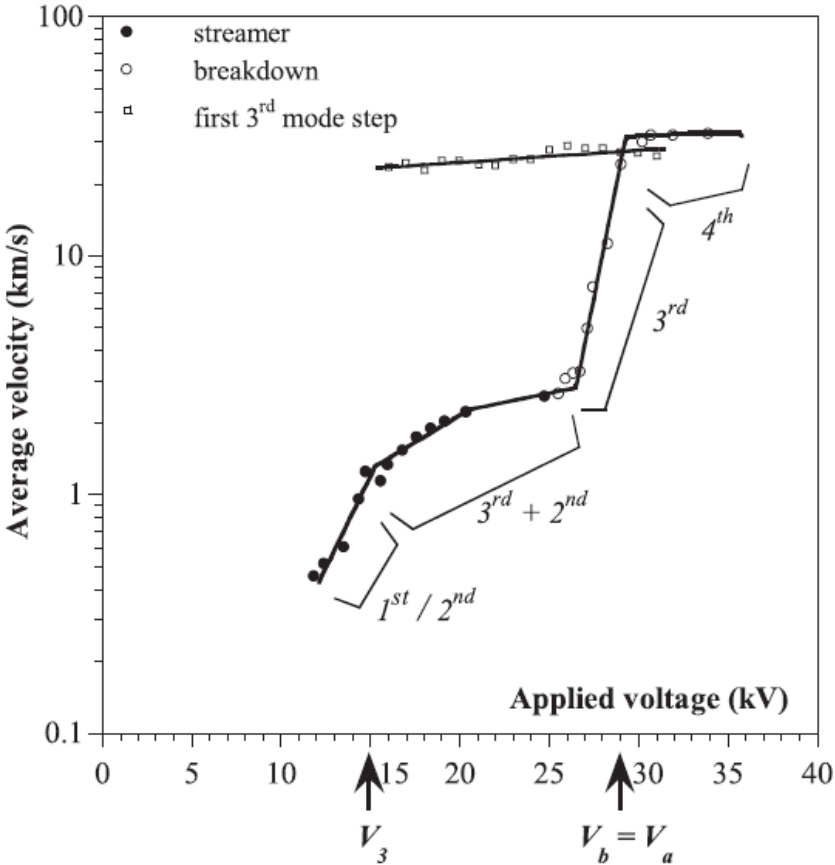
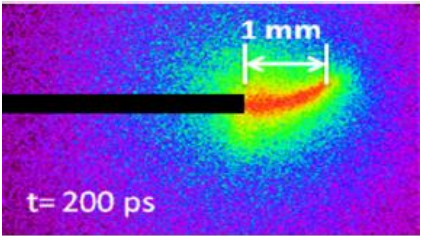


Figure 15. Average streamer propagation velocity v_{av} versus voltage in distilled water [52]. $d = 3\text{ cm}$, $r_p = 1\text{ }\mu\text{m}$.

Lesaint et al. JPD 49 144001 (2016)
 Starikovskiy et al. PSST 20, 24003 (2011)

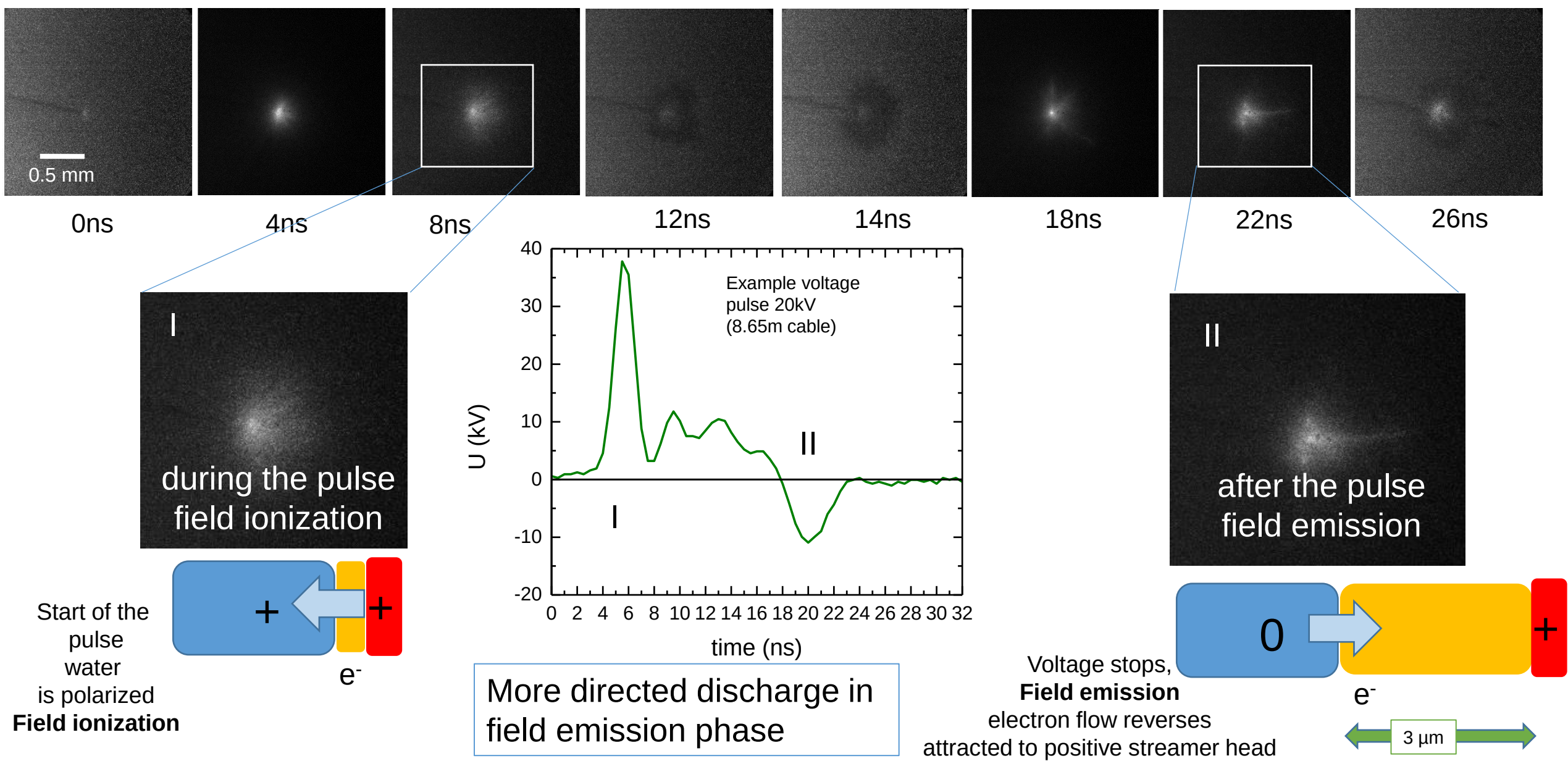
A: 1st mode $v_{av} = 100\text{ m/s}$ 6 kV / 6 mm	B: 2nd mode $v_{av} = 2\text{ km/s}$ 30 kV / 6 mm	C: 2nd mode $v_{av} = 2\text{ km/s}$ 160 kV / 10 cm	D: 3rd + 2nd modes $v_{av} = 10\text{ km/s}$ 304 kV / 10 cm	E: 4th mode $v_{av} = 100\text{ km/s}$ 424 kV / 10 cm
0.5 mm	1 mm	2 cm	2 cm	2 cm

Propagation velocity of streamer in liquids (long pulses)
 3 km/s ... 100 km/s in 10 ns $\Delta x = 3\text{ }\mu\text{m} \dots 0.1\text{ mm}$
 Propagation velocity of streamer in liquids (short pulses)
 1000...5000 km/s in 10 ns $\Delta x = 1\text{ mm} \dots 5\text{ mm}$

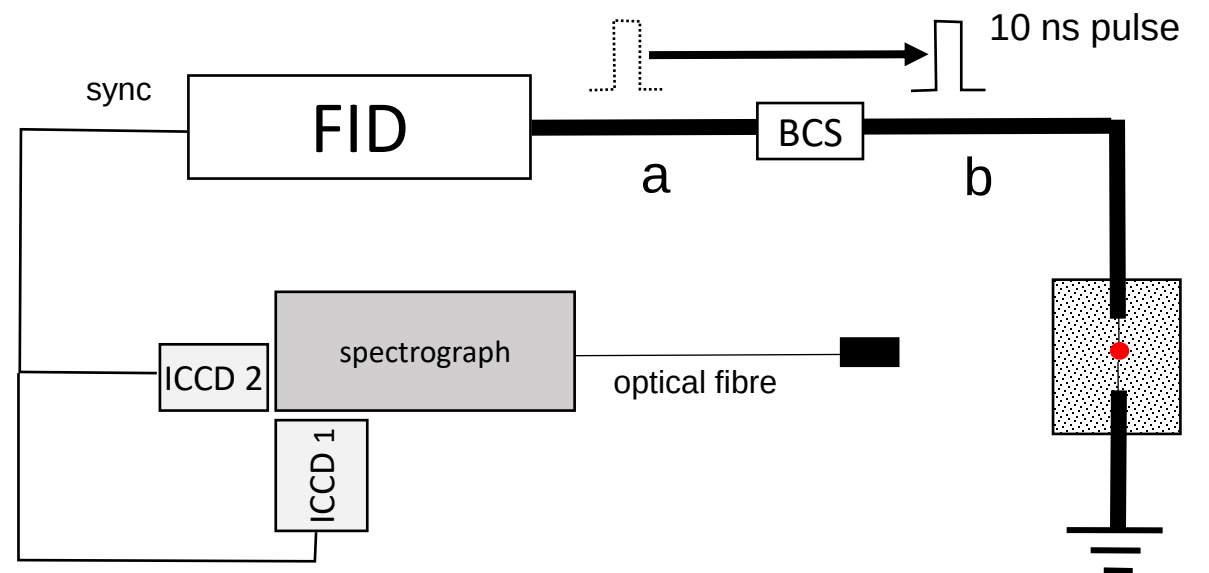
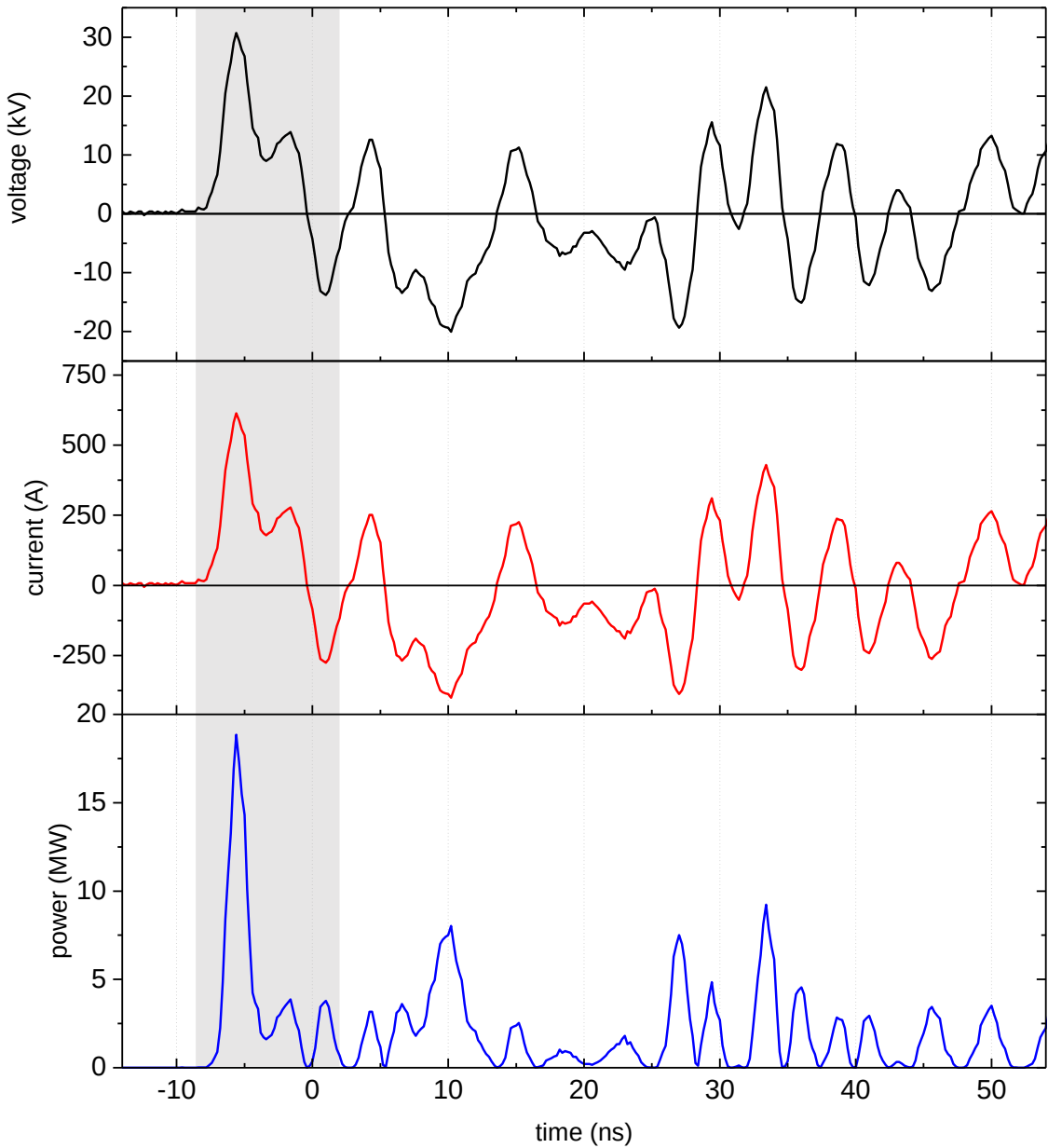


Comparison Streamer
 in air $\sim 1000\text{ km/s}$

Plasma pulse from field ionization to field emission (gate time 2 ns, 22 kV)



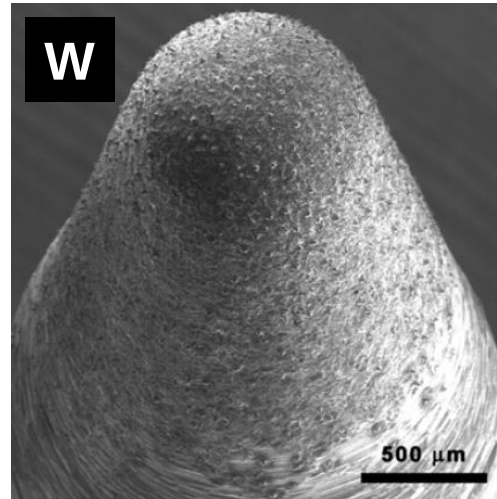
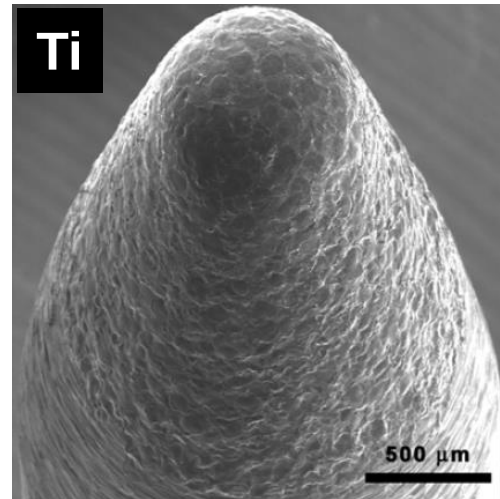
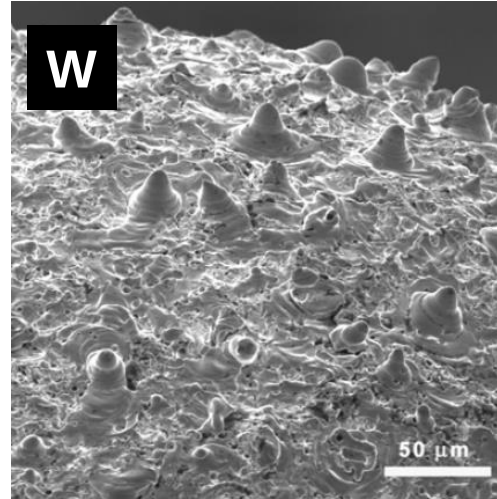
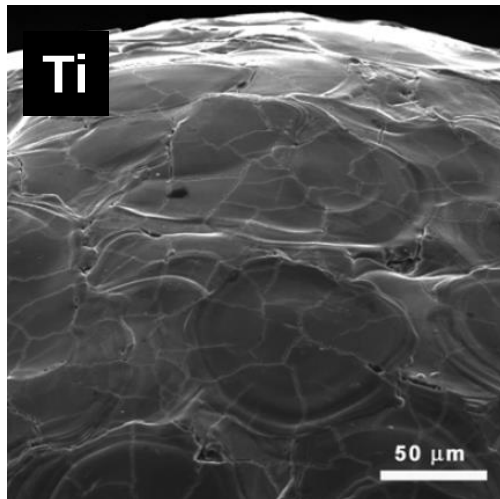
Current and Voltage signals for 10 ns 20 kV pulses using the 8.65 m cable



Tungsten vs. Titanium* tip (500 μm tip radius vs. 50 μm tip radius)

Spark 5..10 μs

3 J $1.5 \times 10^7 \text{ J/m}^2$



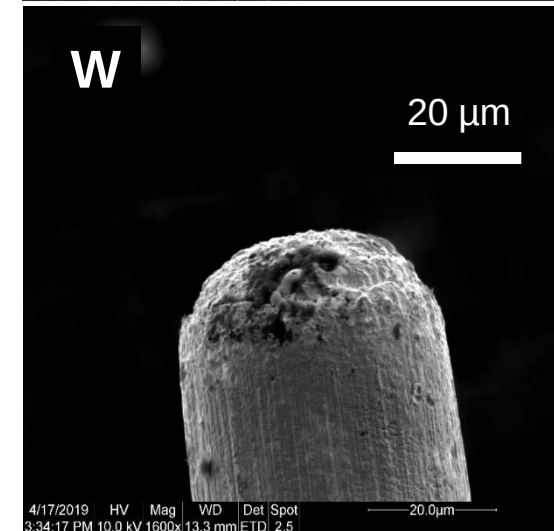
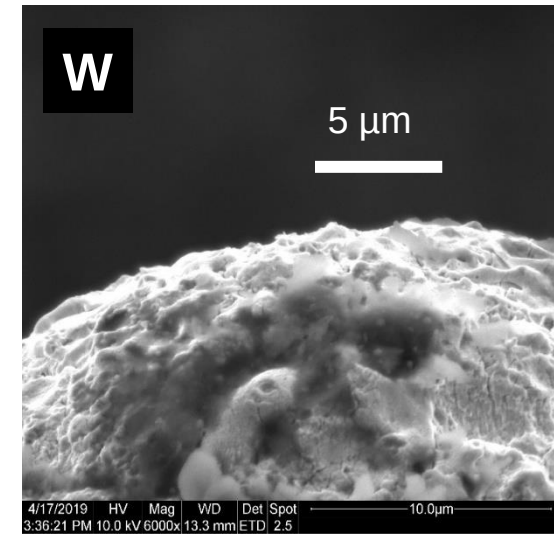
- similar energy per m^2 dissipated
- Sequence of melting and solidification

thermal conductivity @ 1000 $^{\circ}\text{C}$ melting temp.

- Ti – 22 W/m K, 2000 K
- W – 115 W/m K, 3700 K
- Pt – 82 W/m K, 2500 K
- In case of W only small melting tips (for Pt, T, larger molten areas)
- similar to cathode spot in lamps

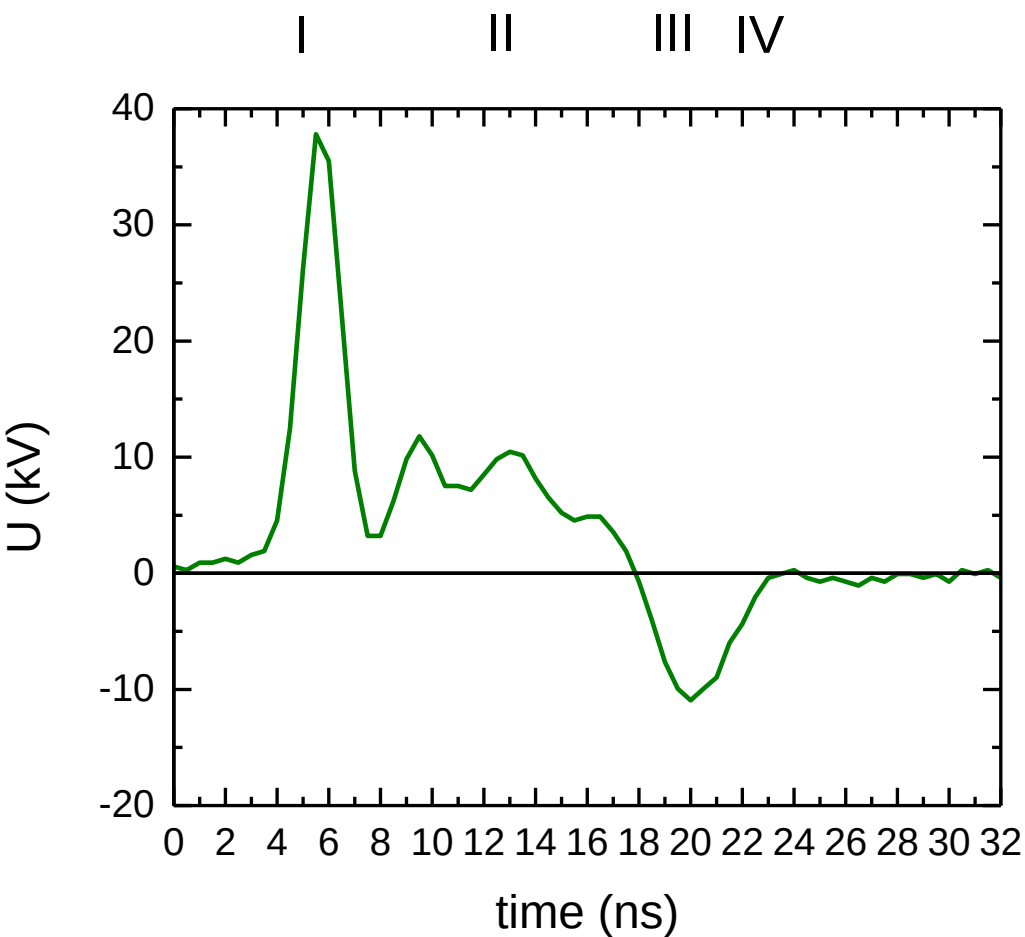
ns pulse 10 ns

0.03 J $1.5 \times 10^7 \text{ J/m}^2$

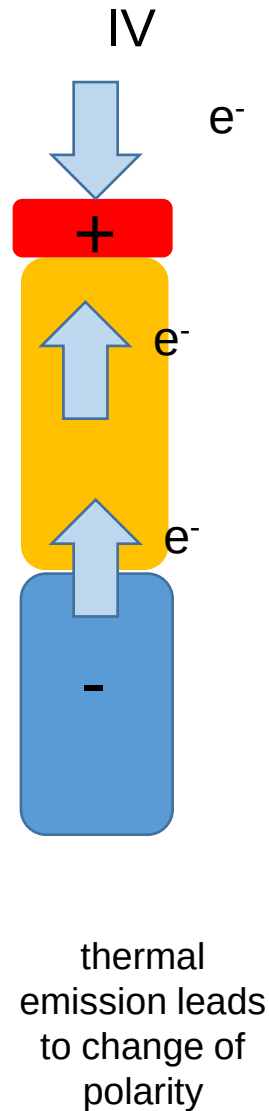
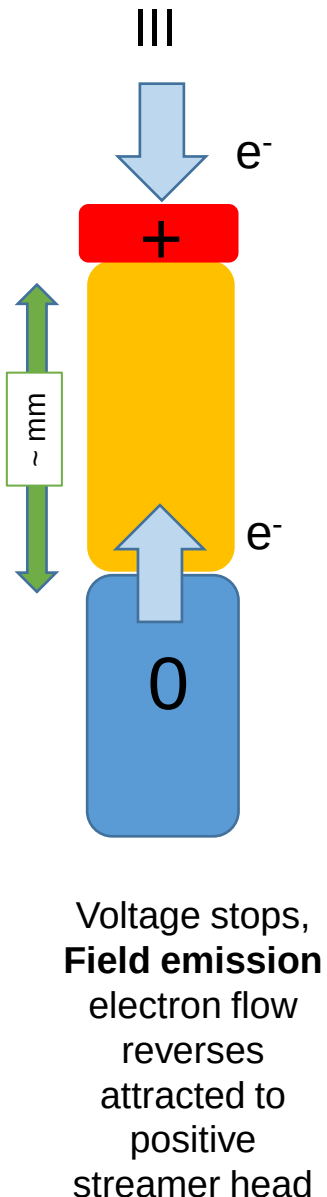
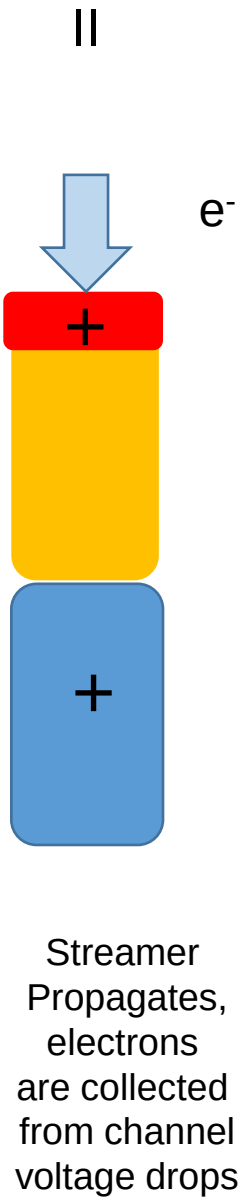
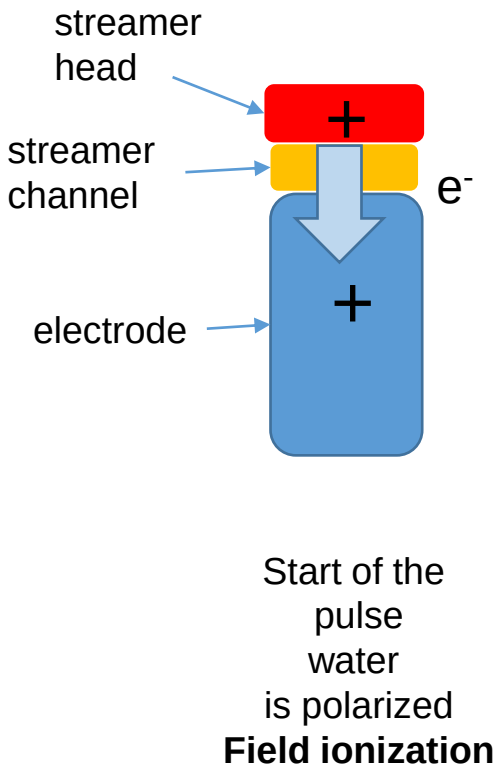


*P. Lukes et al. PSST 20, 3401 (2011)

Sequence of the propagating discharge



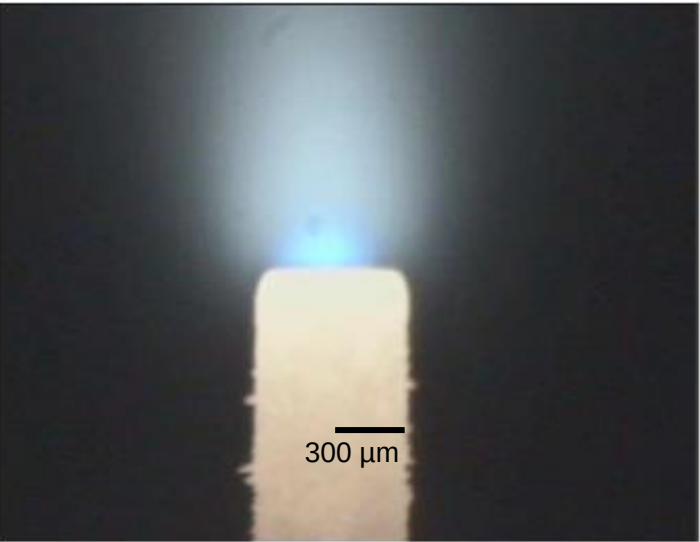
Propagation velocity of streamer in liquids
3 ... 1000 km/s
in 10 ns
 $\Delta x = \sim \text{mm}$



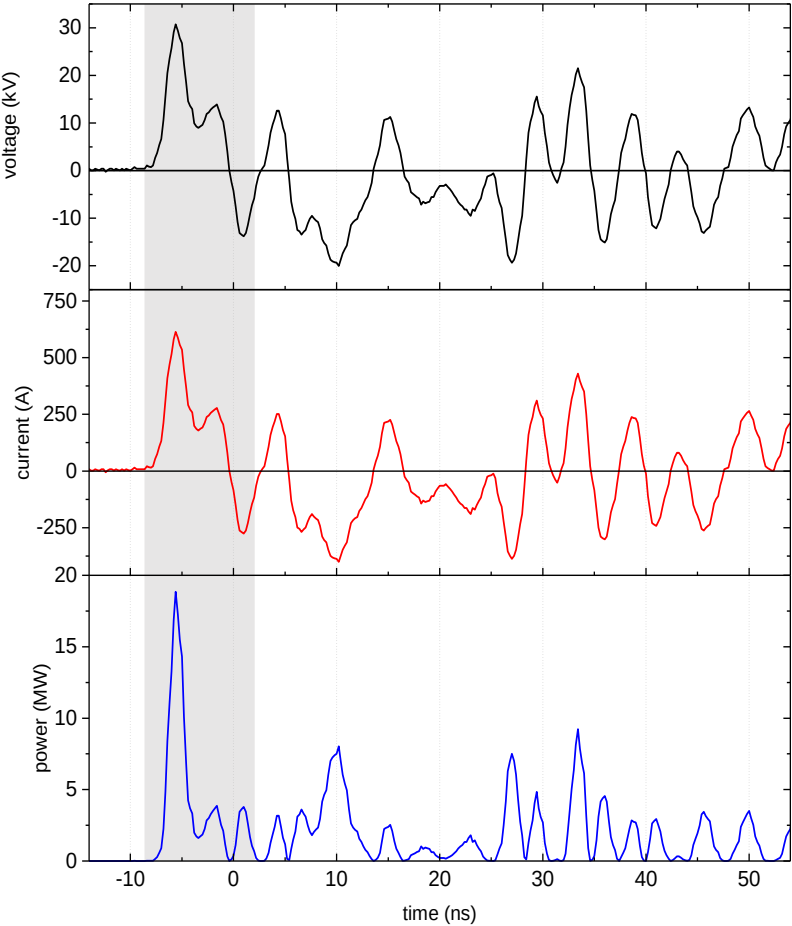
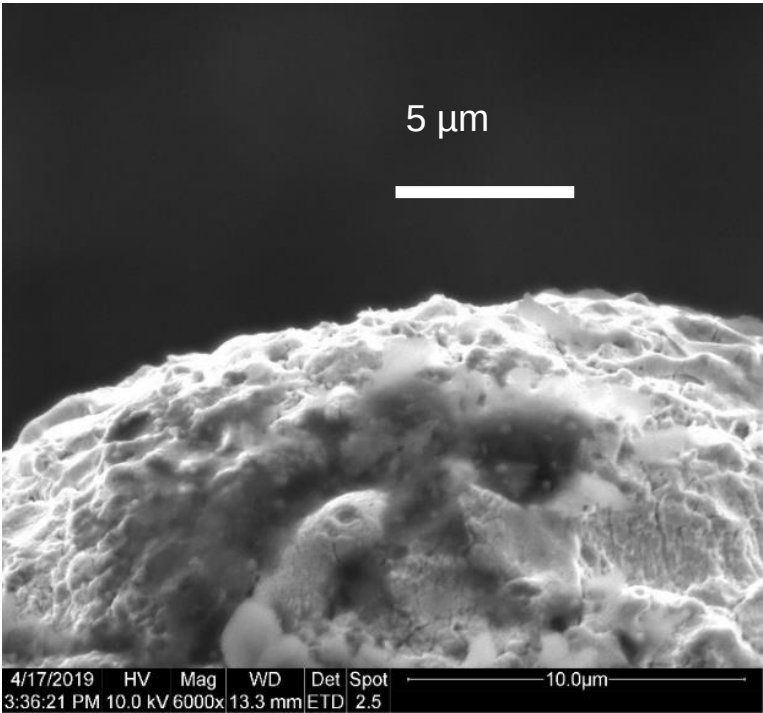
Comparison to cathode spots at high pressure lamps

@500 A on a 2 μm radius spot
= magnetic field pressure of 1 GPa

Pinch effects at W tips



(d) $i_{\text{arc}} = 15.0 \text{ A}$

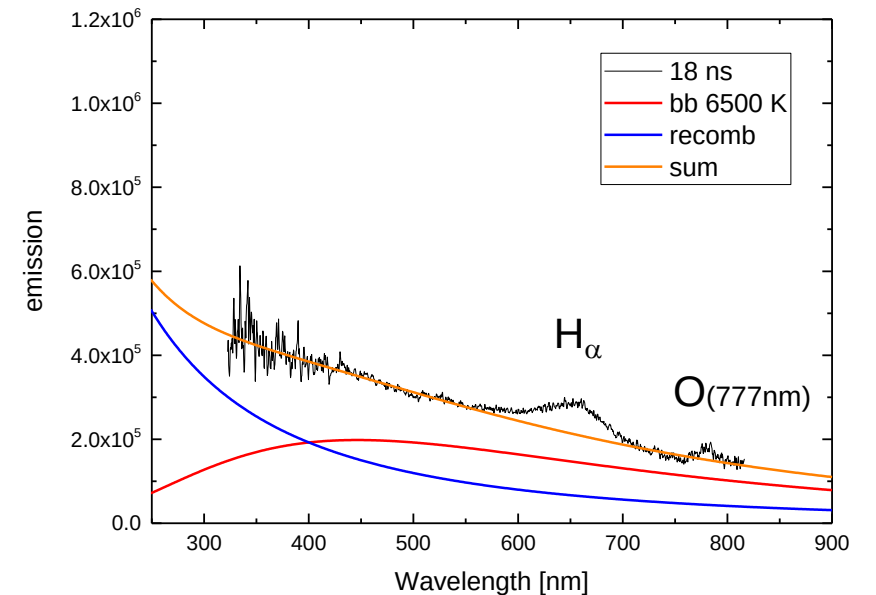
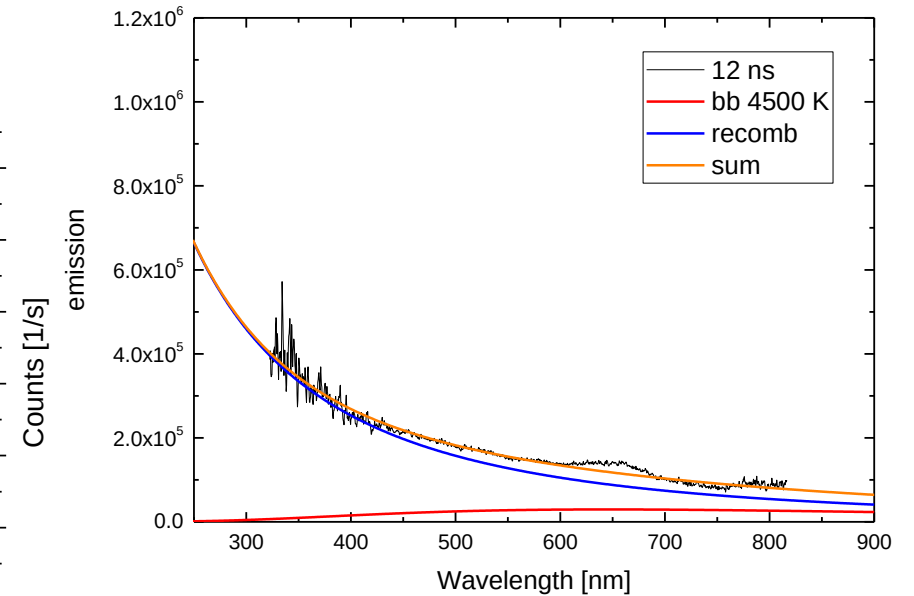
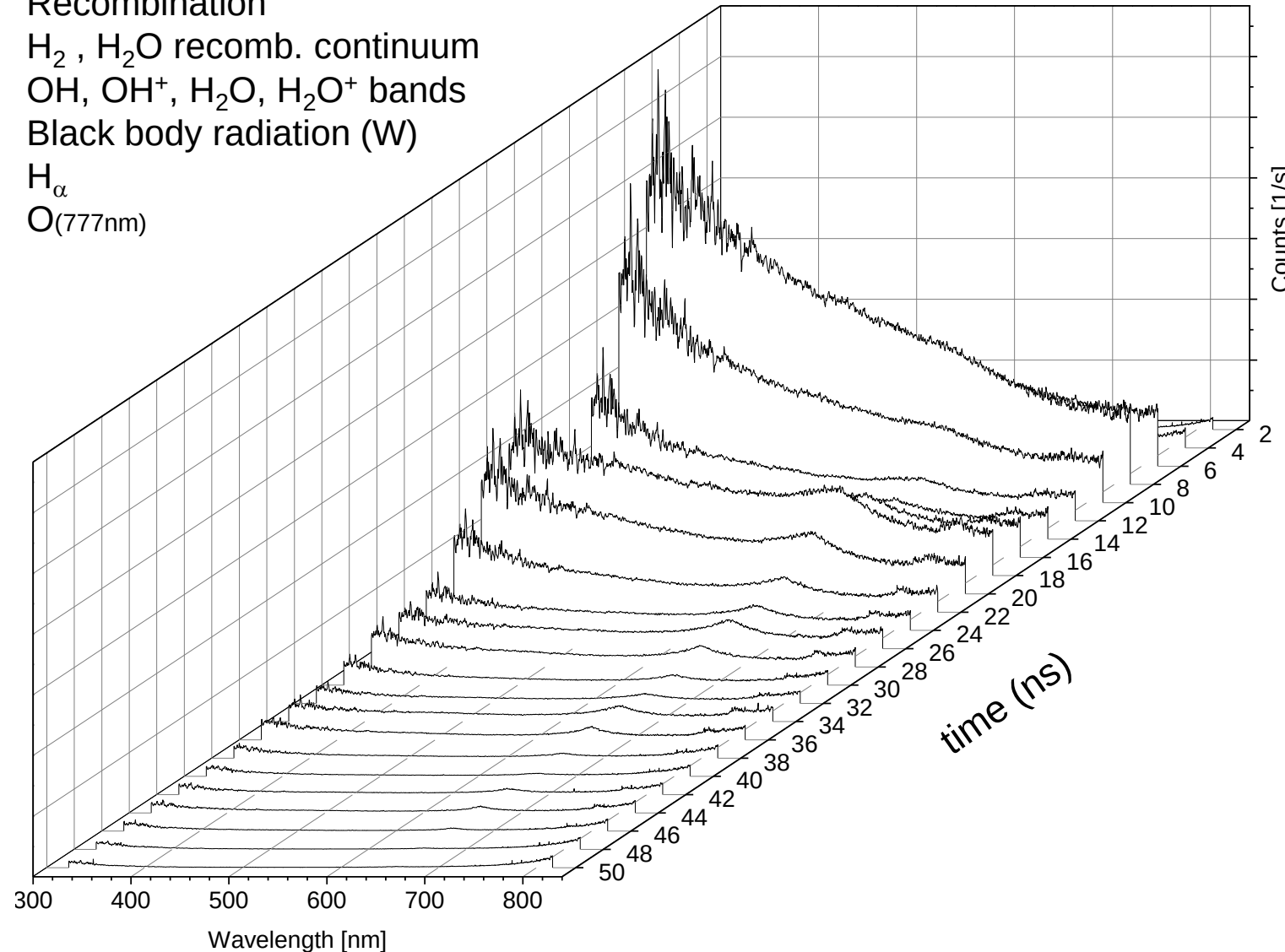


A. Bergner et al. PSST 23, 054005 (2014)

Temperatures from emission spectra of the plasma

Spectrum (first 50 ns, time resolution 2 ns)

- Recombination
- H_2 , H_2O recomb. continuum
- OH, OH^+ , H_2O , H_2O^+ bands
- Black body radiation (W)
- H_α
- $\text{O}(777\text{nm})$

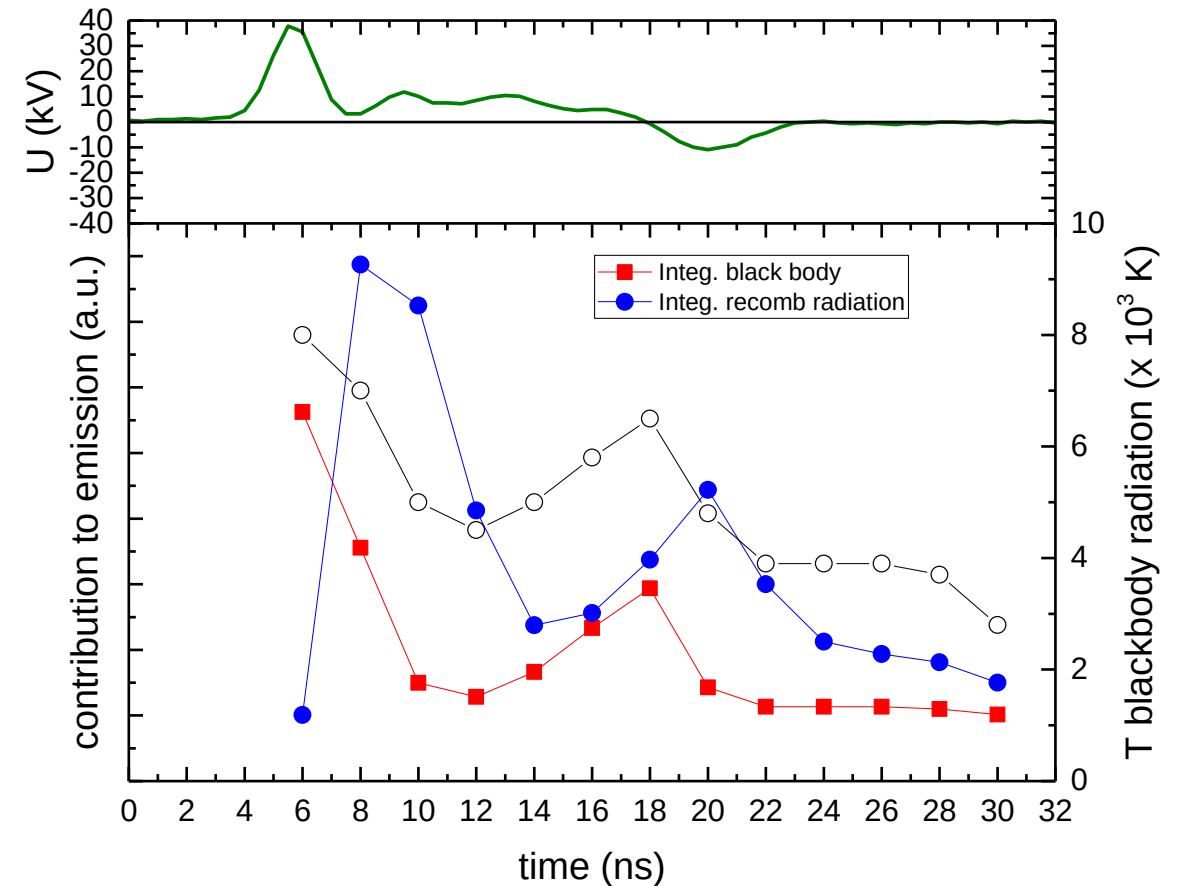
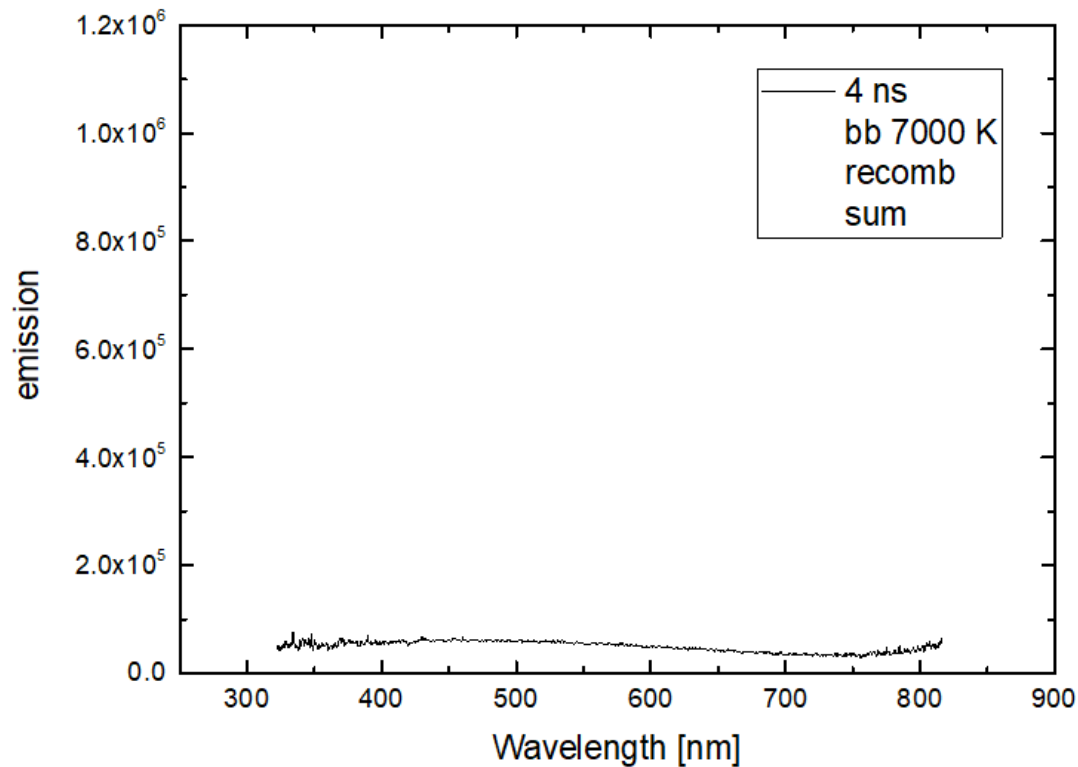


Temperatures from emission spectra of the plasma

- Power absorption at the beginning of the pulse and due to reversal of the voltage
- Black body radiation, followed by $1/\lambda^x$ spectrum.

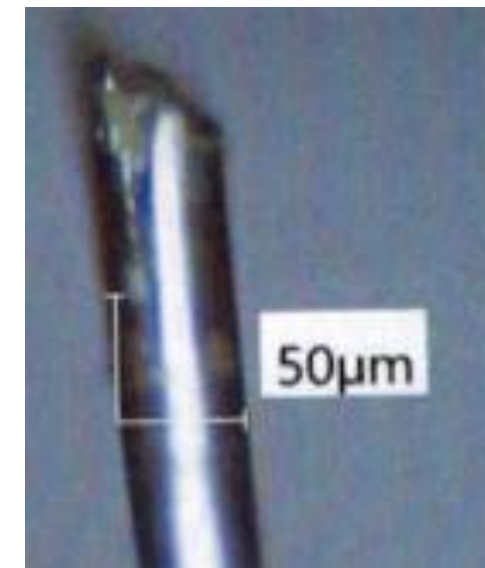
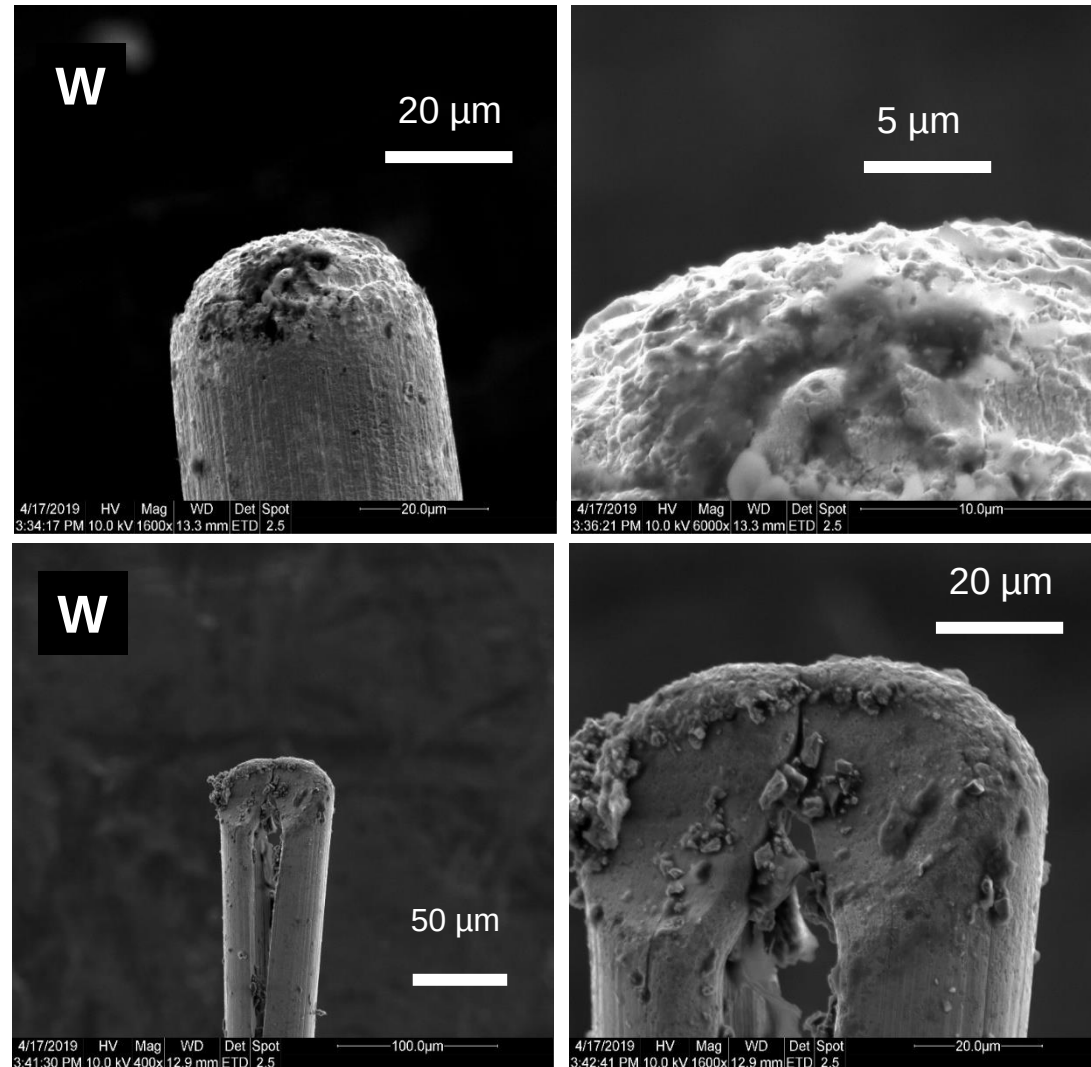
For 20 kV Experiment

$T_0 < 8000 \text{ K @ } 0 \text{ ns}$



Tungsten tip

- Long term operation possible
- W as high melting temperature 3700 K
- W therm. conduct. 115 W / m K
- W oxidizes, melting temperature 1800 K
- Crystallites are formed

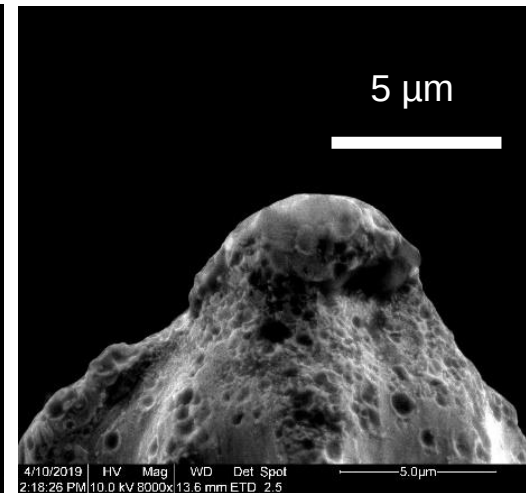
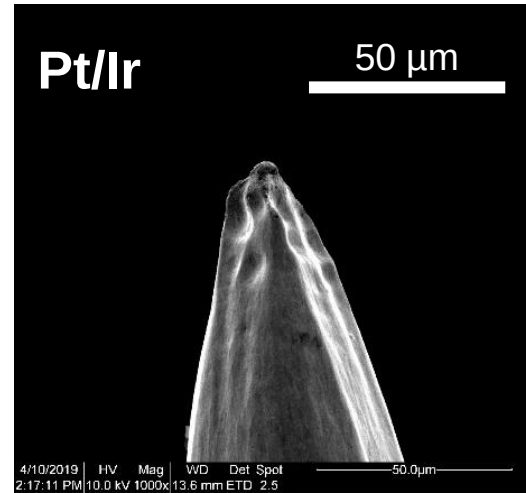


Short term use, < 7 h

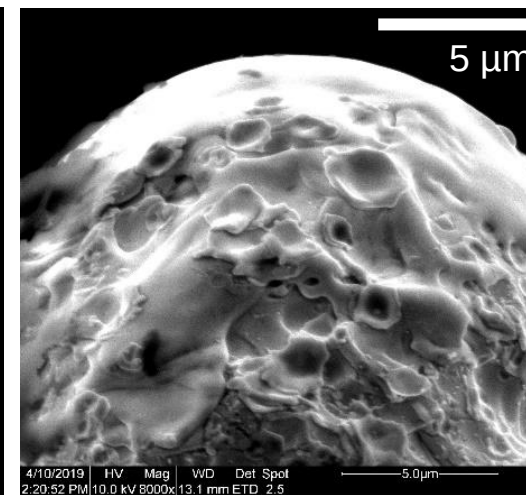
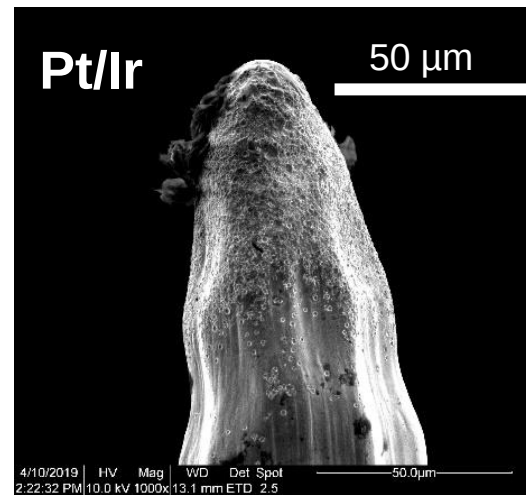
long term use, ~ 30 h

Platinum / Iridium tip (from AFM/SEM microscopes with 5..10 nm tip radius)

- Only short term operation possible
- After 1 h no plasma ignition possible anymore
- Pt melting temperature 2100 K
- Pt thermal conduct. 82 W/ m K
- Ir melting temperature 2700 K
- only Ir oxidizes

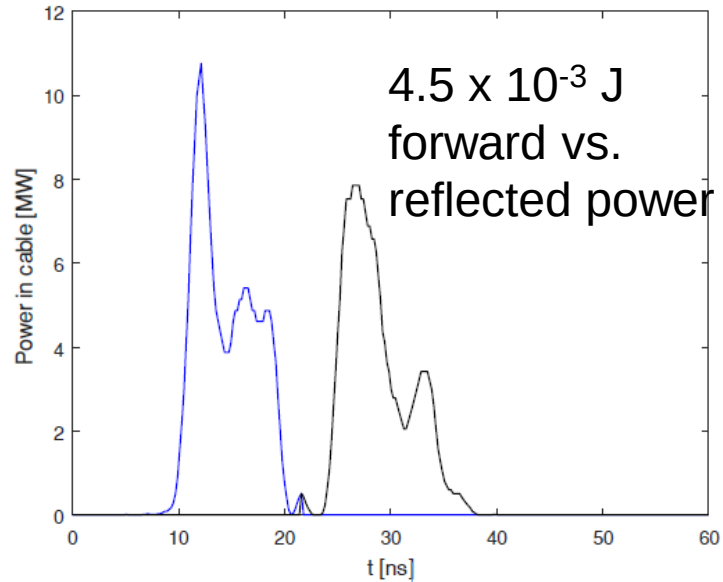


Short term use, 2 min

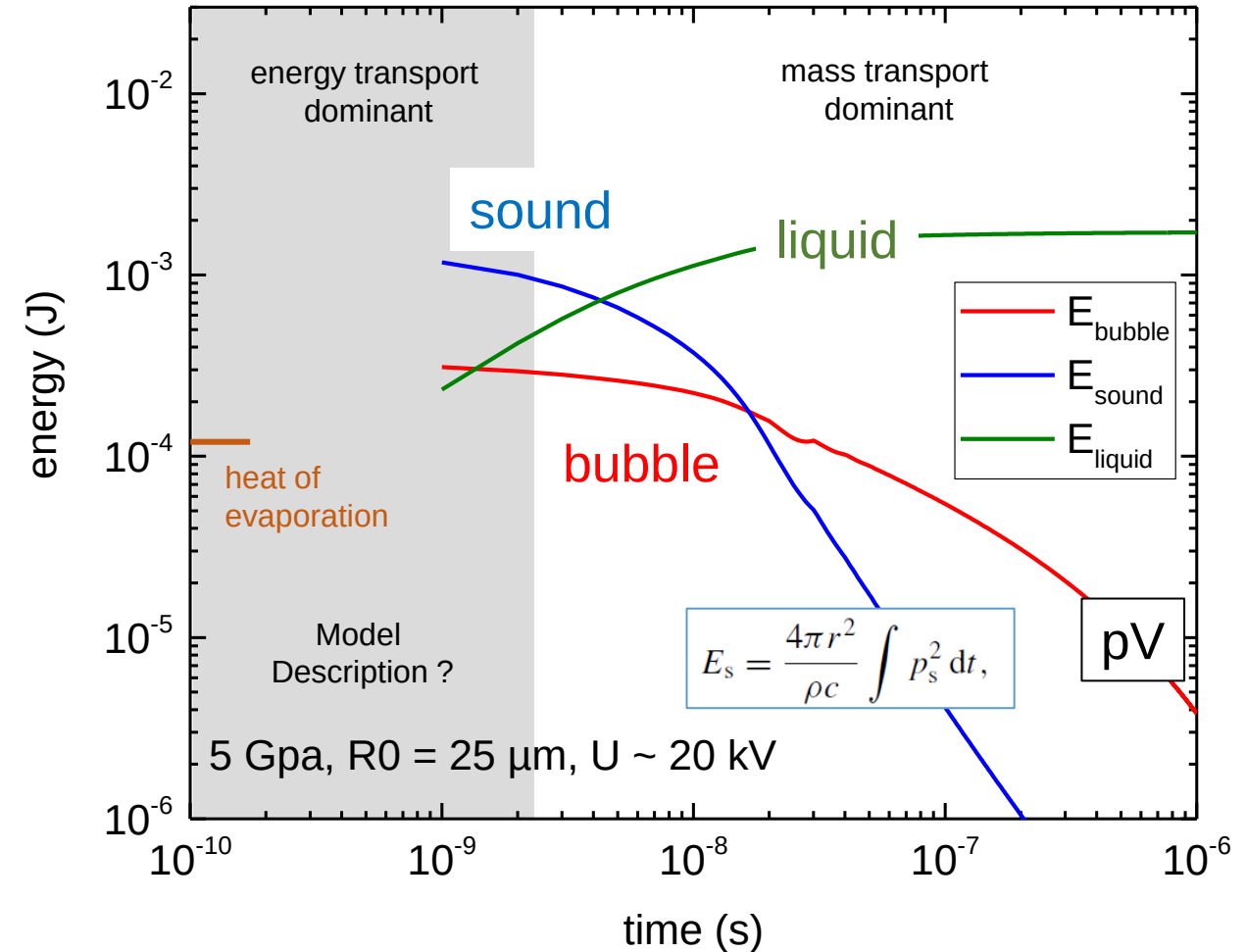
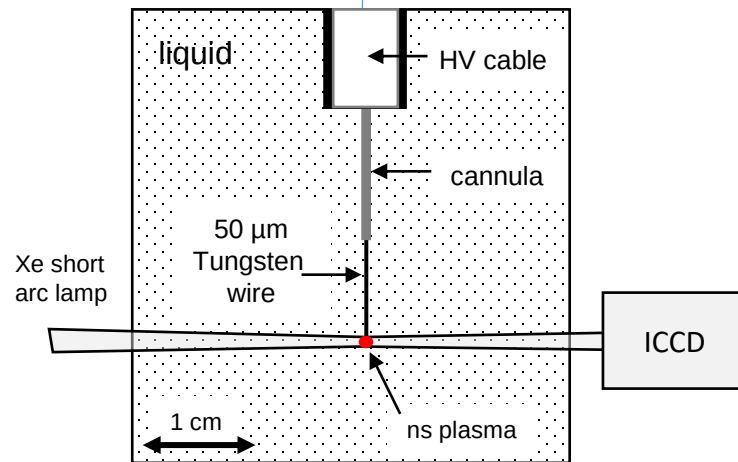


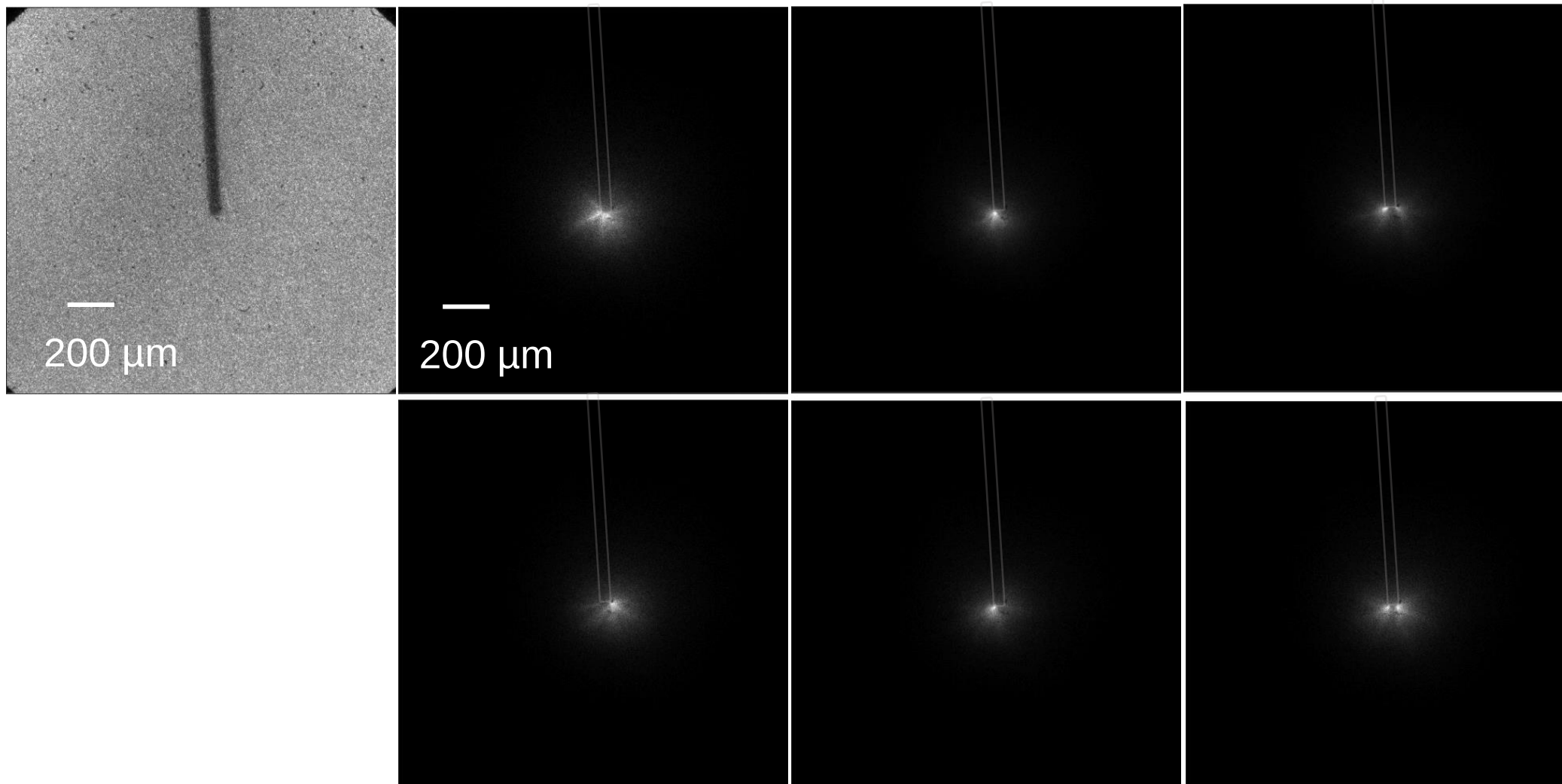
long term use, ~ 1 h

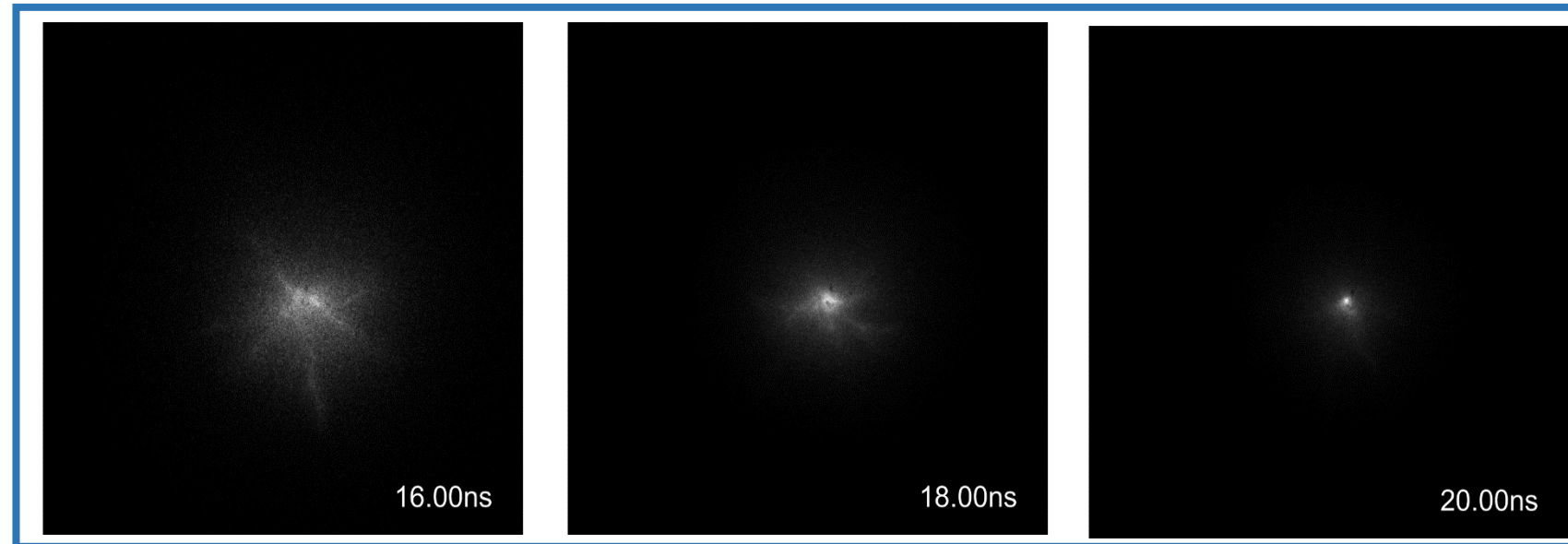
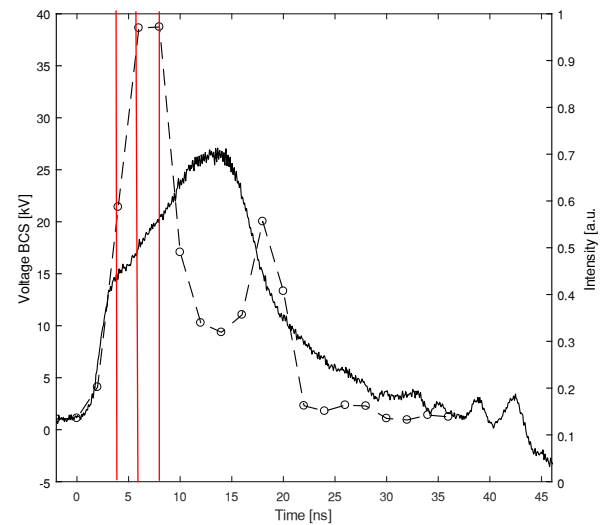
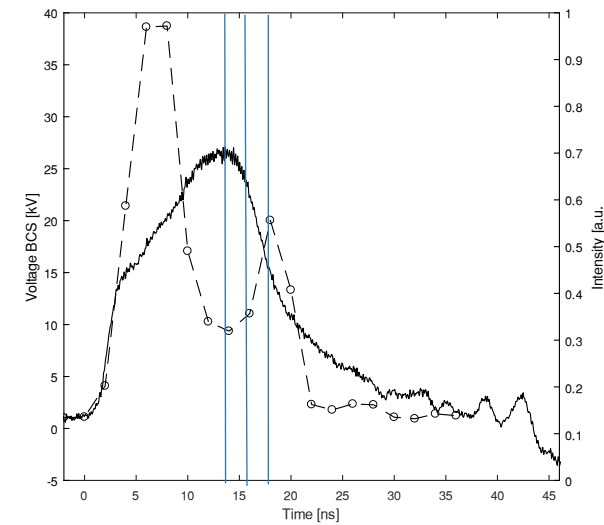
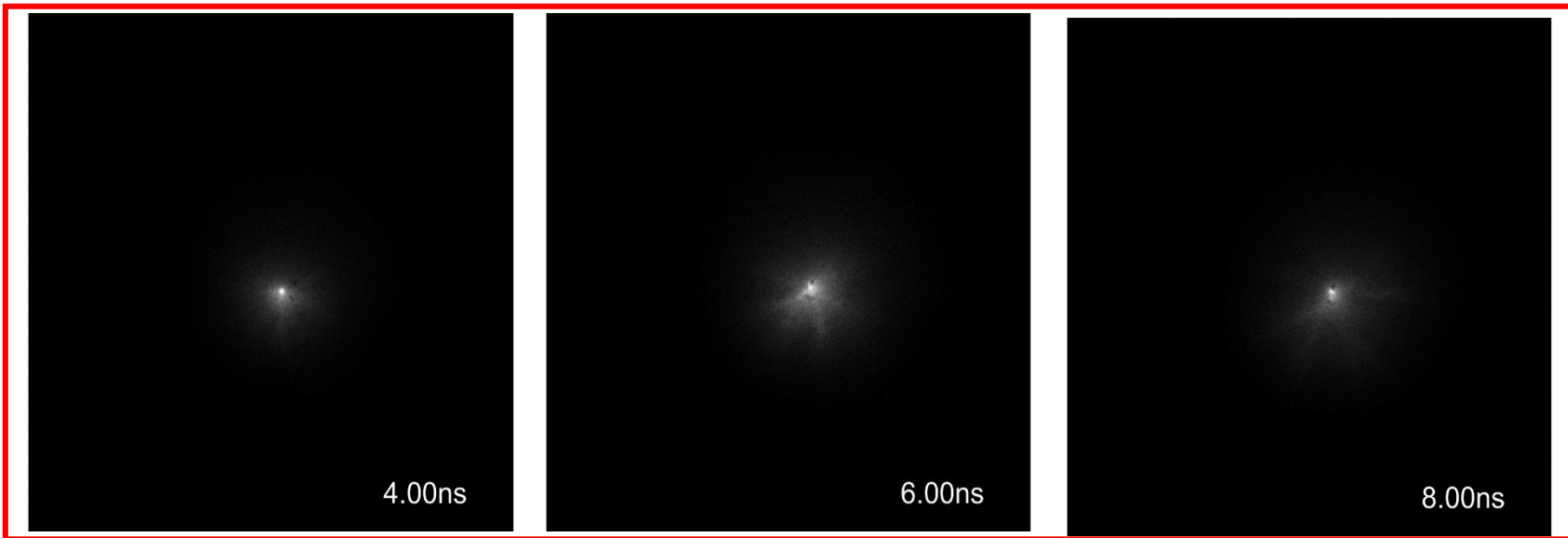
Dissipated energy during plasma ignition within the first 10 ns – comparison to experiments



In ns plasmas at very high initial pressure, most of the energy is transferred to the sound wave







Nature of the $1/\lambda^x$ background in emission – cathode spots on the tungsten electrode

