# Multi-Fidelity Machine Learning for Extending the Range of High-Fidelity Molecular Dynamics Data

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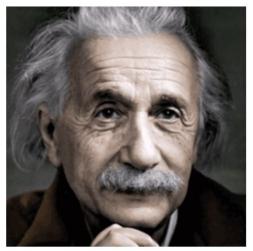
# Multi-Fidelity Machine Learning for Extending the Range of High-Fidelity Molecular Dynamics Data

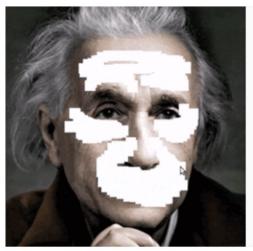
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#### Image Inpainting: Filling in the gaps with Machine Learning



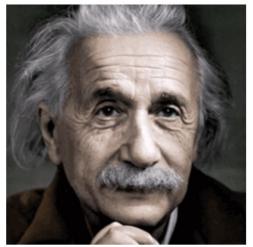


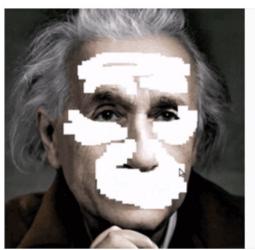
Utilize machinelearning to make a prediction

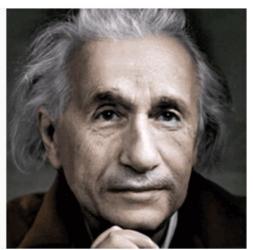
Original Image

Masking

#### Image Inpainting: Filling in the gaps with Machine Learning







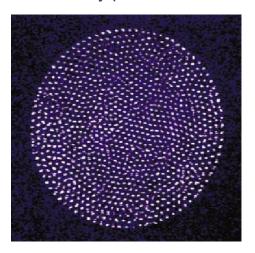
Original Image

Masking

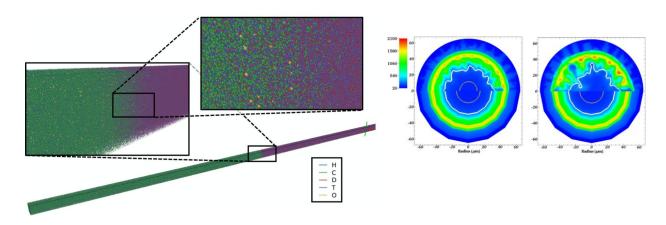
Predicted image

# Atomic Transport in Disparate Regimes

Self-diffusion in magnetized dusty plasmas



Atomic-scale mixing in nuclear fusion simulations and experiments

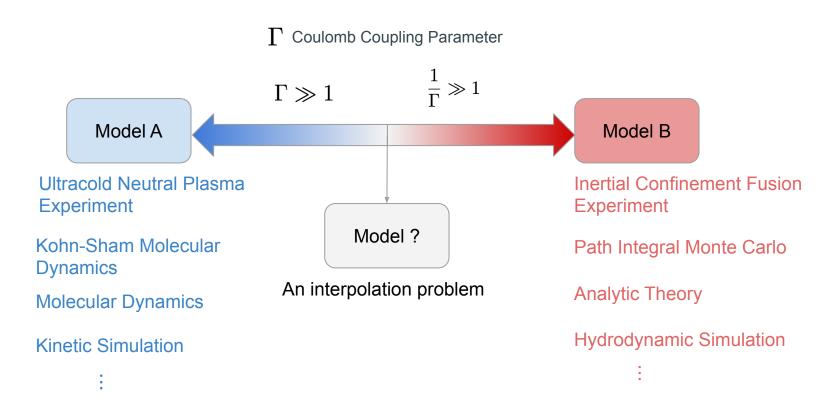


<sup>1)</sup> Murillo, Physics of Plasmas 11:5 2964-2971 (2004)

<sup>2)</sup> Stanton et. al, Phys. Rev. X 8(2) (2018)

<sup>3)</sup> Rana et. al Phys. Rev. E 95(1) (2017)

#### Physical Models are Often Asymptotically Accurate



# Interpolation with Gaussian Process Regression (GPR)

Radial Basis Function kernel

$$k(x_i, x_j) = a \exp\left(-\frac{\|x_i - x_j\|^2}{b}\right) \longrightarrow K(X, X)$$

A measure of similarity between data points

a,b are optimizable hyper-parameters

Kernel matrix

Training domain Prediction domain

$$f^* = K(X_*, X)K(X, X)^{-1}f$$
 Prediction m x n n x n n x 1

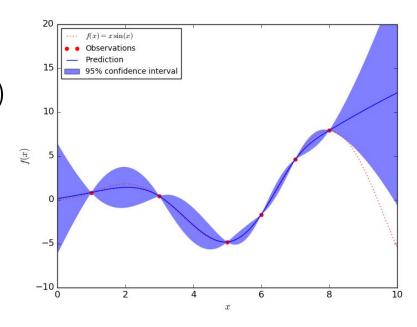
$$\sigma^2 = K(X_*, X_*) - K(X_*, X)K(X, X)^{-1}K(X, X_*)$$

 $m \times m$ 

 $m \times n$ 

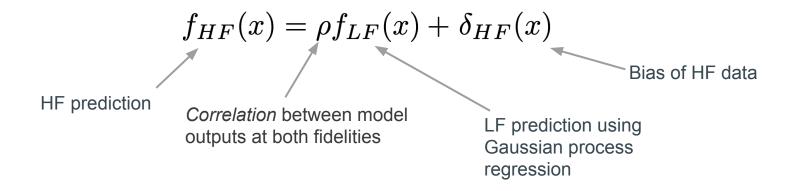
 $n \times n$ 

 $n \times m$ 



Covariance Uncertainty matrix

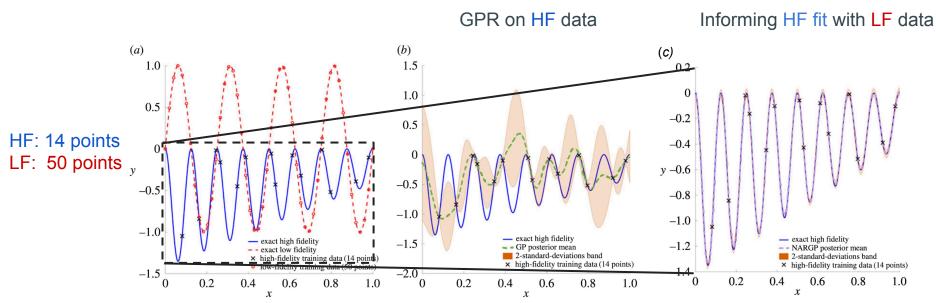
### Linear Autoregressive Mult-Fidelity (MF) Model



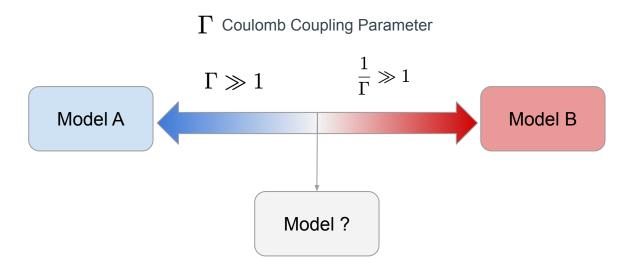
### Informing High-Fidelity Fits with Low-Fidelity Data

Model A: high-fidelity (HF) - expensive to generate data, very accurate

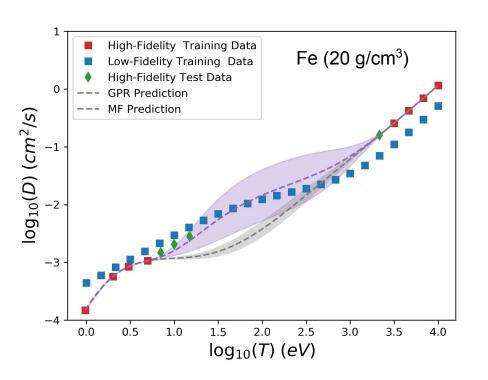
Model B: low-fidelity (LF) - cheap to generate data, low accuracy

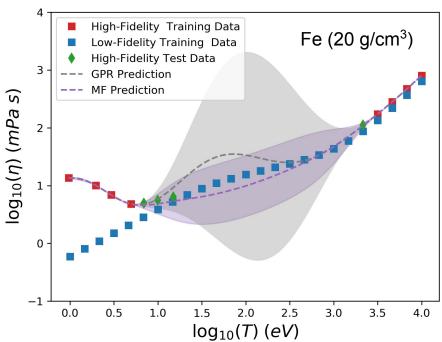


### Physical Models are Often Asymptotically Accurate



### Predicting Transport Coefficients with Multiple Models



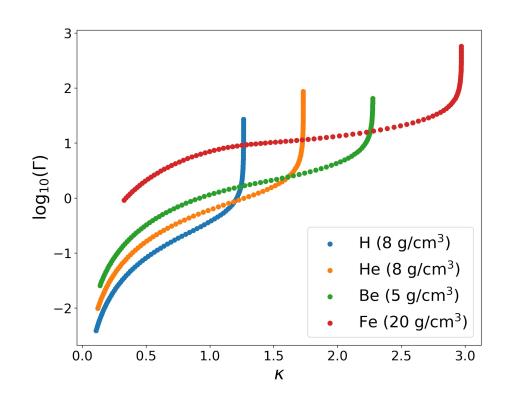


# Projecting $\{Z, n_i, T\}$ to 2-Dimensions

$$\kappa = \frac{a_i}{\lambda_s} \qquad \text{Inverse electron} \\ \text{screening length}$$

$$\Gamma = rac{\langle Z 
angle^2 e^2}{a_i T}$$
 Coulomb coupling parameter

 $A(\kappa,\Gamma)$  pair defines a Yukawa system.



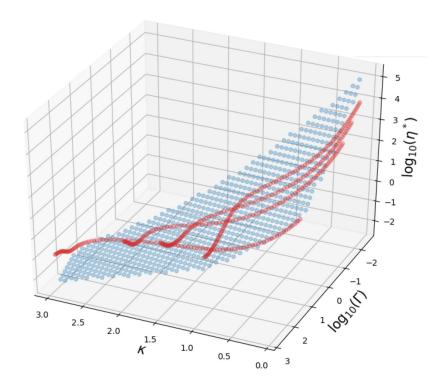
# Multi-Fidelity Modeling in 3D

 $\kappa$  x-axis

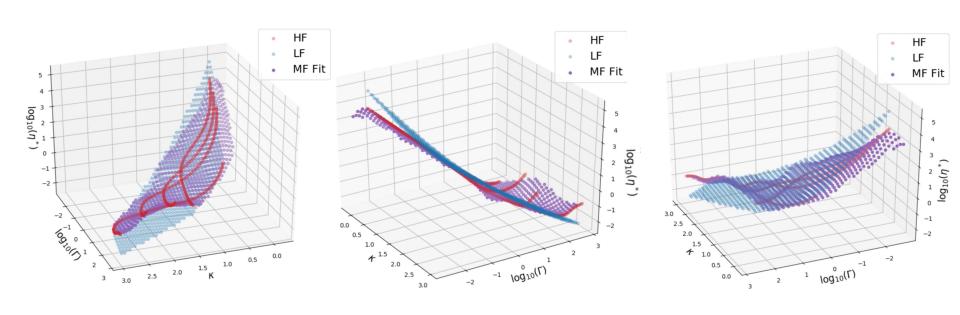
 $\Gamma$  y-axis (log-scale)

$$\eta^* = \eta/(\rho_i \ a_i \ \omega_p^2)$$
 z-axis (log-scale)

- Low-Fidelity Model
- High-Fidelity Model



## Multi-Fidelity Modeling in 3d Backup, Backup



#### Contributions

- Multi-fidelity models span large scales and preserve asymptotics
- Table interpolation improved when curse of dimensionality becomes problematic
- Confidence intervals aid in experimental design

